

~~SECRET~~

DECLASSIFIED

SPECIAL PROJECTS GROUP
Technical Report No. 112

STRESS ANALYSIS OF 1/12 SCALE HOVERING AND TRANSITION MODEL

September 1957

Declassified on June 14, 2001 by the
Air Force Declassification Office
IAW EO 12958

Issued by:

Avro Aircraft Limited
Malton, Ontario, Canada

Written by:

G. Jacquemin
G. Jacquemin
Avro Aircraft Limited

Approved by:

D. C. Ferguson
D. C. Ferguson
Sr. Stress Engineer
Special Projects Group
Avro Aircraft Limited

The number of pages included in this report including Title Page,
Table of Contents, and Illustrations, is 212

~~SECRET~~

DECLASSIFIED

57RD2-19677

DECLASSIFIED

~~SECRET~~

II

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELTABLE OF CONTENTS.

SECTION	TITLE	PAGE.
1	SUMMARY	1
2	INTRODUCTION	1
3	DESCRIPTION OF INSTALLATION	4
4	LOAD ANALYSIS	17 *
5	MODEL STRESS ANALYSIS	63
6	LOAD GAGE DESIGN	83
7	MODEL SUPPORT STRUCTURE STRESS ANALYSIS	116
8	FAIRING STRESS ANALYSIS	142
9	DEFLECTIONS	154
10	CALIBRATION	162
APPENDIX A	WEIGHTS	183

* LOAD ANALYSIS : MODEL PAGE 17
 " " : MODEL SUPPORT " 41
 " " : FAIRING " 55

WRITTEN BY

G. Jacques

CHECKED BY

DECLASSIFIED

DATE

pt. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

III

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELLIST OF ILLUSTRATIONS

FIG.	TITLE	PAGE
1	GENERAL ARRANGMENT OF INSTALLATION	10
2	$\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL	11
3	DETAILS OF MODEL SUPPORT - A	12
4	" " " " - B	13
5	CONTROL ARM	14
6	VERTICAL FAIRING	15
7	HORIZONTAL FAIRING.	16
8	$\frac{1}{12}$ SCALE MODEL - SCHEMATIC DIAGRAM	64
9	MODEL - DETAILS OF OUTER EDGE	72
10	GAGE SECTION	83
11	NOMINAL MINIMUM CLEARANCE	154
12	CALIBRATION RIG.	173

WRITTEN BY

G. Jaeger

CHECKED BY

DECLASSIFIED

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

IV

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELINDEX OF DRAWINGS

DWG. N°	DESIGNATION
1-SK-30290	Installation of $\frac{1}{12}$ scale model and balance in 20' tunnel
4-SK-30290	G.A. of instrumentation
6-SK-30290	G.A. of Calibration rig
7-SK-30290	Ass'y details of rear load member and fairing to control arm and fairing.
8-SK-30290	Attachment of main ass'y supply pipes to tunnel front load members
10-SK-30290	G.A. of model
15-SK-30290	Ass'y of load gauges and supply pipes to model
41-SK-30290	Main ass'y of supply pipes
355-SK-30290	Fairing assembly.

<u>WRITTEN BY</u>	<u>CHECKED BY</u>	<u>DATE</u>	<u>ISSUE</u>	<u>AIRCRAFT</u>

DECLASSIFIED

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODELINDEX OF REFERENCES.AVRO SPECIAL PROJECT GROUP TECHNICAL REPORTS.

- AVRO/SPG/TR 29 : AIR CUSHION EFFECT TESTS - PART 2
AVRO/SPG/TR 33 : AIR CUSHION EFFECT TESTS - PART 3
AVRO/SPG/TR 9B : TEST SPECIFICATIONS FOR THE $\frac{1}{2}$ SCALE
HOVERING & TRANSITION MODEL.

GENERAL REFERENCES.

- AN-C-5. - MARCH 1955 -
- THEORY OF PLATES & SHELLS - S. TIMOSHENKO.
- RESISTANCE DES MATERIAUX APPLIQUEE A L'AVIATION - P. VALLAT.
PUBLISHED BY I MENARD - EDATEURS - 8 RUE DES REGANS - TOULOUSE - FRANCE.

WRITTEN BY

CHECKED BY

DATE

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~ DECLASSIFIEDSTRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL1-0 SUMMARY

The strength and stiffness of the $\frac{1}{12}$ scale hovering and transition model, its supporting structure and fairings are analyzed.

The stressing of all parts except the ring load gages is carried out with an ultimate load factor of 4.

The strength of all components has been found satisfactory and the deflections small enough to be negligible.

Balance calibration procedure is outlined and pertinent data provided.

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	W. F. Ferguson	Sept. 1957		

~~SECRET~~ DECLASSIFIED

~~SECRET~~ DECLASSIFIEDSTRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.2-0 INTRODUCTION

As a part of the system 606 A test program, a $\frac{1}{12}$ scale model of the P.V. 704 aircraft has been designed for installation in the 20' diameter Moore Memorial Wind Tunnel at Wright-Patterson Airforce Base. The purpose of the model is to study the take-off, hovering and transition to forward flight characteristics of the aircraft. The proposed tests are outlined in AVRO/SPG/TR 98 - Test Specifications for the $\frac{1}{12}$ scale Hovering and transition model. The development of loads and the stressing of the model, model support structure and fairings are contained in this report.

The model is circular in planform: 35.3" DIA, with intake and jet exhaust flows simulated. These flows are supplied through large diameter pipes which also serve to support the model on the wind tunnel balance. In order the the balance is not affected by the supply pressures, these pipes come into the tunnel in a horizontal plane to supply the vertical pipes supporting the model.

The wind tunnel balance is a three components balance measuring lift, pitching moment and drag. However, due to the distances involved compared with the size of the model and the relatively light aerodynamic and heavy tare loading of the installation, sufficiently accurate readings of drag and moments cannot be obtained. For this reason, and to provide for the measurement of rolling moments, a second, body fixed balance system

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	DET signature	Sept. 1957		

~~SECRET~~ DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL2-0 INTRODUCTION - CONT'D.

is provided near the model.

This second balance employs ring type load gages to measure drag forces and pitching and rolling moments. Lift forces are also indicated on this balance, but since they include forces due to the model supply pressure, readings of lift will be taken on the tunnel balance only.

Aerodynamic loads on the model and support structure fairings are estimated using standard aerodynamic theory; the model lift, drag and moment coefficients being estimated from the results of previous tests. Hovering loads are based on Aero reports: AVRO/SPG/TR 29 & AVRO/SPG/TR 33. An ultimate load factor of 4 is used throughout.

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaques	W. Ferguson	Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL3-0 DESCRIPTION OF INSTALLATION -3-1 GENERAL -

Fig 1 shows the general arrangement of the installation. The model is suspended from a vertical arm below a horizontal tube attached to the main balance struts. The incidence of the model is adjusted by using the rear balance strut acting on a control arm extending from the horizontal tube.

In order to remove the airload from the model mounting, the whole installation is enclosed in a fairing supported independently of the balance system on the strut fairings.

Additional streamlining of the horizontal tube fairing is provided but has not been shown on fig 1 for clarity.

3-2 MODEL -

The model is composed of two disk-shaped steel turnings joined together to form a hollow circular wing; and three profiled turnings joined to form a circular center body (Fig 2).

The two halves of the wing are held apart by 24 radial ribs and attached together by screws into these ribs and into each other around the outer edge of the model. Each half contains three sets of holes distributed around three circles concentric with the model center as shown in fig 8. The holes are covered by segmented plates containing matching holes of a smaller diameter. Several sets of plates with different hole sizes are provided in order to vary the sizes of the final openings.

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemont	De T. J. J. J.	Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL-

3-0

DESCRIPTION OF INSTALLATION

3-2

MODEL - CONT'D.

The peripheral outlets are 336 holes: .242" dia. distributed along a circle of rad. 16.825". They are covered with segment plates having holes of dia. ranging in steps from .242" to .126" dia. Plates are also provided to close the holes completely.

The propulsive outlets are 48 holes: 1.40" dia distributed along a circle of rad. 15.80". They are covered by the segment nozzle plates which direct the airflow aft at about 20° to the wing surface. Plates are also provided to close the holes completely.

Both of these outlets are covered by the same plates. Various arrangement of propulsion and control being provided by changing the plates.

The center outlets are 96 holes: .453" dia distributed along a circle of rad. 11.312". They are covered with segment plates having holes of dia ranging in steps from .453" to .228". Plates are also provided to close the holes completely.

The wing is clamped by bolts between two of the center body turnings. The upper turning (A in fig 2) is in the shape of a dummy intake and ramp and is attached to the outer model support tube. The center turning (B in fig 2) forms the lower intake ramp and connects with an inner tube to form a duct leading to the wing. High pressure air is admitted through this duct to exhaust through the openings described above to simulate the aircraft propulsive system.

The lower turning (C in fig 2) forms the lower intake roof and forms a duct leading to the center tube

WRITTEN BY

G. Jacques

CHECKED BY

J. Ferguson

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -3-0 DESCRIPTION OF INSTALLATION3-2 MODEL CONT'D.

Chen tube is partially evacuated to draw air through the intake to simulate lower intake airflow. The lower burning is attached to the center supply tube by a suspension rod and to center burning by six soldered tubes. These tubes also direct some of the high pressure air through a central nozzle in the lower burning to simulate the aircraft Viper exhausts.

This model is intended to simulate take-off, hovering and transition configurations close to a simulated ground board. For this reason, only the lower intake is used.

Hovering conditions will be tested for the model horizontal and tilted up to 20° .

Transition will be tested for angles of attack ranging from -10° to $+45^\circ$.

Ground distance will be adjusted from zero to about 2 dia.

3-3 MODEL SUPPORT STRUCTURE -

The model is attached at the end of a vertical arm (fig. 3) by a suspension rod and 4 ring gages measuring pitching and rolling moments and loads parallel to the model.

The vertical arm is made up of two concentric tubes which are connected to the model through elastic joints at the

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. J. Jorgensen	MC Jorgensen	Sept. 1957		

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL3-0 DESCRIPTION OF INSTALLATION -3-3 MODEL SUPPORT STRUCTURE - CONT'D.

measuring gage section. The outside tube carries the pressure supply to the model while the inner tube carries the suction.

The lower part of the arm is removable together with the model and gage section by disconnecting a flange on the outside tube. The top & bottom of the inner tube in the removable section are connected to the upper part of the inner tube and to the model by sliding couplings so that all loads transmitted to the upper part of the arm are carried by the outer tube.

The model suspension rod is attached to the outer tube by means of a cruciform bracket at the level of the connecting flange. This bracket also supports the lower part of the inner tube.

The vertical arm is welded at its upper end to the horizontal tube and to the control arm.

The horizontal tube supplies pressure to the nozzles of the model on one side and suction to the intake of the model on the other side. It is supported at both ends by ball-bearing assemblies (Fig 4). Bolted to the end of the main balance struts. It is attached to the external parts by means of bellows allowing free movement of the ends and is fixed against side motion at the pressure side ball-bearing. It is free to slide on the suction side to allow for thermal expansion. A tension rod takes the load due to pressure and suction in the tubes. This rod is attached at its outer end to a 3 armed bracket welded inside the horizontal tube coming through the tunnel wall on the pressure side.

WRITTEN BY

G. Jacques

CHECKED BY

H. Ferguson

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL3-0 DESCRIPTION OF INSTALLATION3-3 MODEL SUPPORT STRUCTURE - CONT'D.

A similar bracket at the other end contains ball-bearings to avoid twisting of the rod when changing the angle of incidence of the model.

The control arm (fig. 5) is a welded steel structure in the shape of an I beam with height decreasing toward the rear balance strut.

3-4 FAIRINGS -

The vertical arm of the fairing (fig. 6) is a streamlined light alloy structure with wooden ribs and formers. The two lower parts of this fairing are removable to give access to the measuring gage section. It is attached at its upper end to the steel fairing of the control arm and to the horizontal tube fairing (fig. 7).

The horizontal tube fairing is another steel tube concentric with the model support tube and supported at each end on plain bearings attached to the sides of boxes extending below the main balance strut fairings. In the section between tunnel wall and main balance strut, the fairing and the inner tube are assembled as a rigid unit. They are supported by the tunnel walls and the box extending below the main balance strut fairings.

The control arm fairing is a steel box and is attached by a linkage to the rear balance strut fairing.

All fairings are completely independant of

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	H. Ferguson	Sept. 1957		

~~SECRET~~ DECLASSIFIEDSTRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL.3.0 DESCRIPTION OF INSTALLATION -3.4 FAIRINGS - CONT'D.

the balance system and clearances are provided to ensure that no contact will occur through possible deflection of the structure or misalignments.

A follow-up mechanism maintains the alignment between the model support struts and the fairings when changing the angle of attack of the model.

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemin	De Feyerme	Sept. 1957		

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

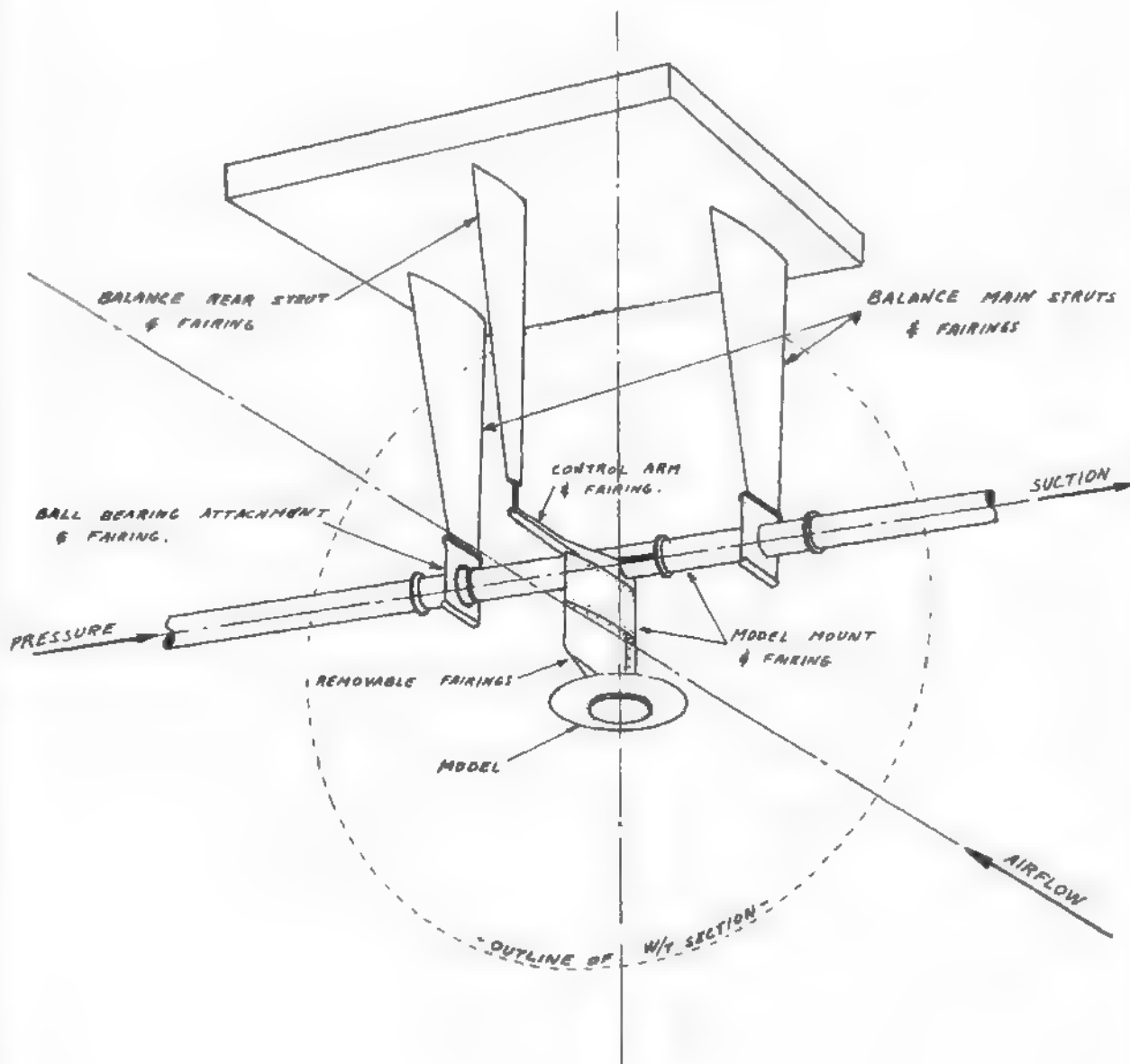
STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL

FIG 1 - GENERAL ARRANGEMENT OF INSTALLATION

WRITTEN BY

G. Jacques

CHECKED BY

W. Ferguson

DATE

Sept. 1957

ISSUE

AIRCRAFT

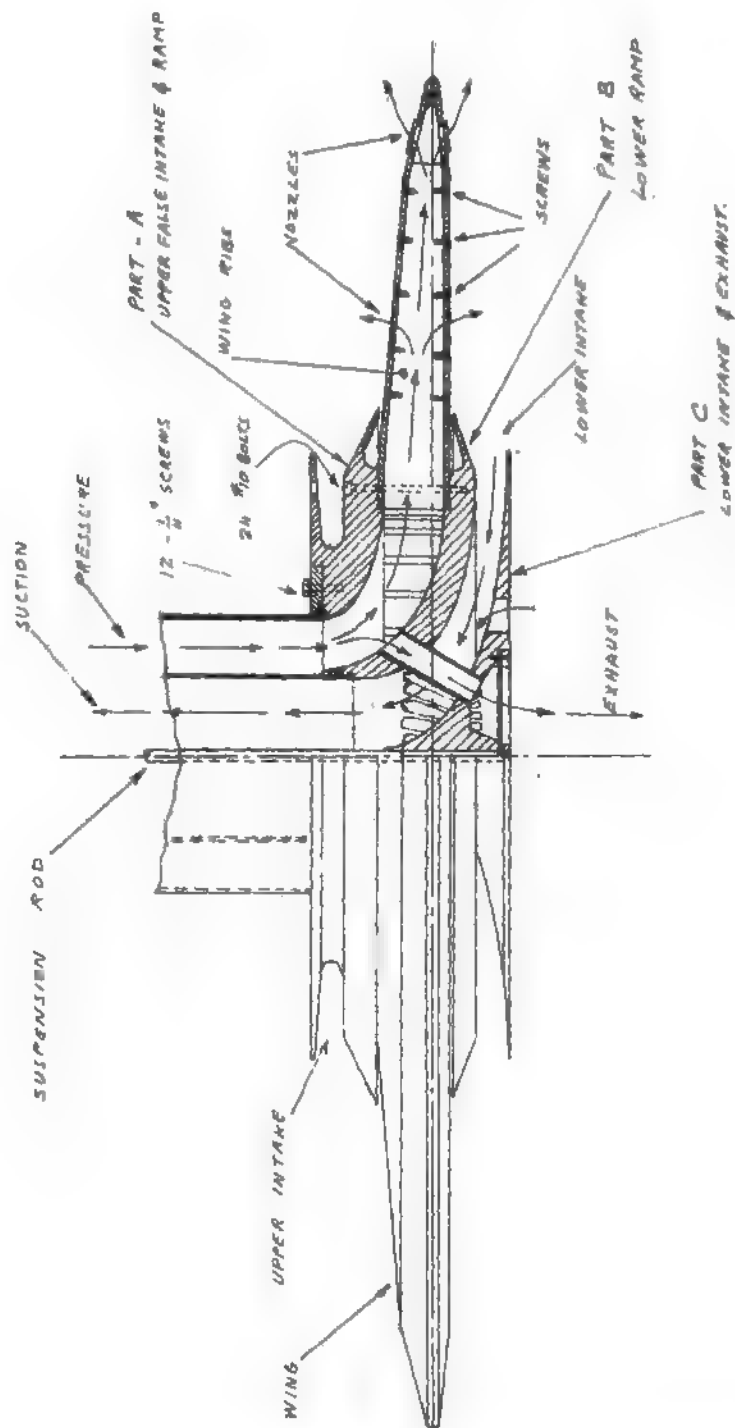
~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

11

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELFIG-2 - $\frac{1}{12}$ SCALE HOVERING AND TRANSITION MODEL

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	W 729477	Sept. 1957		

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

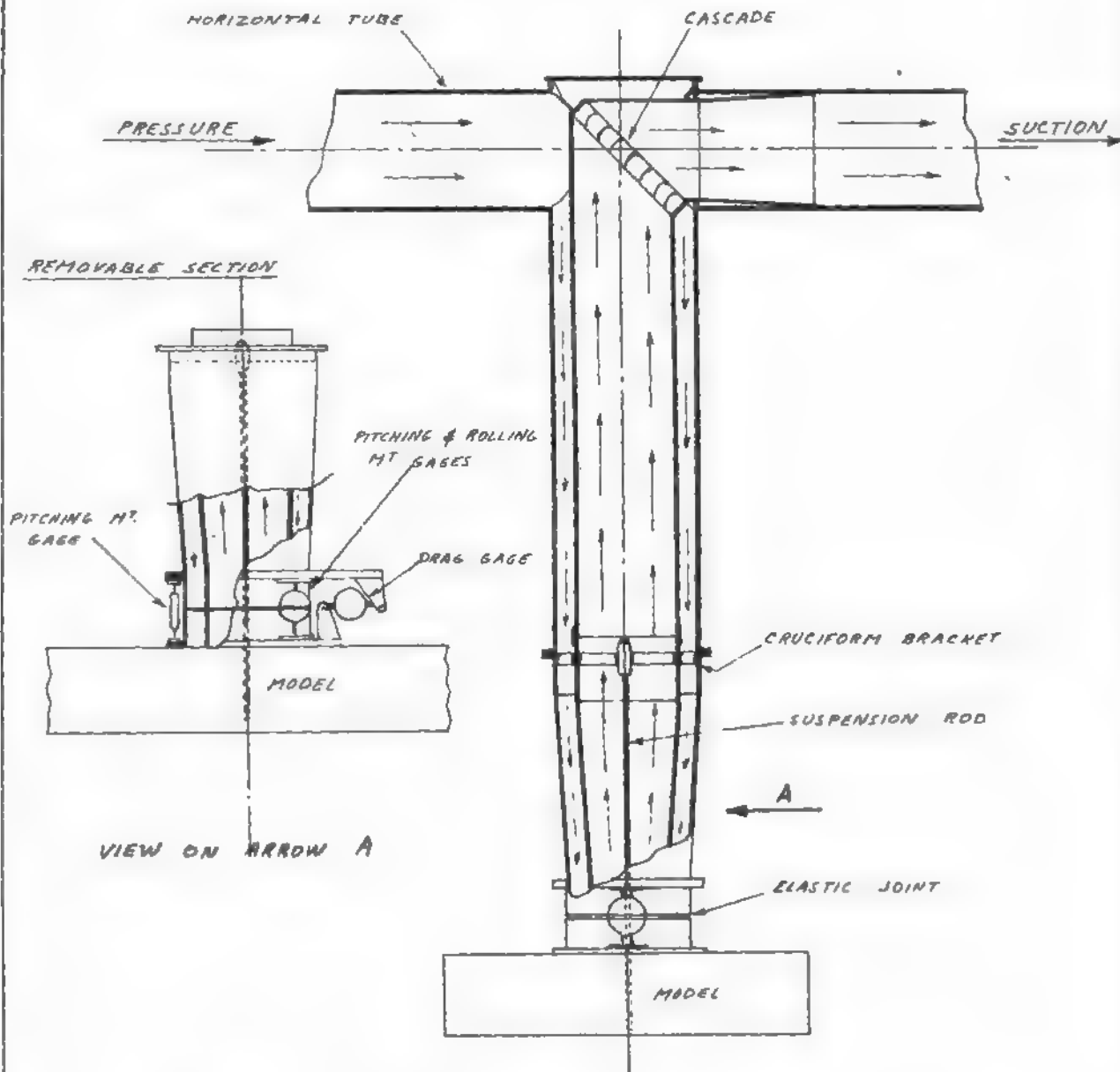
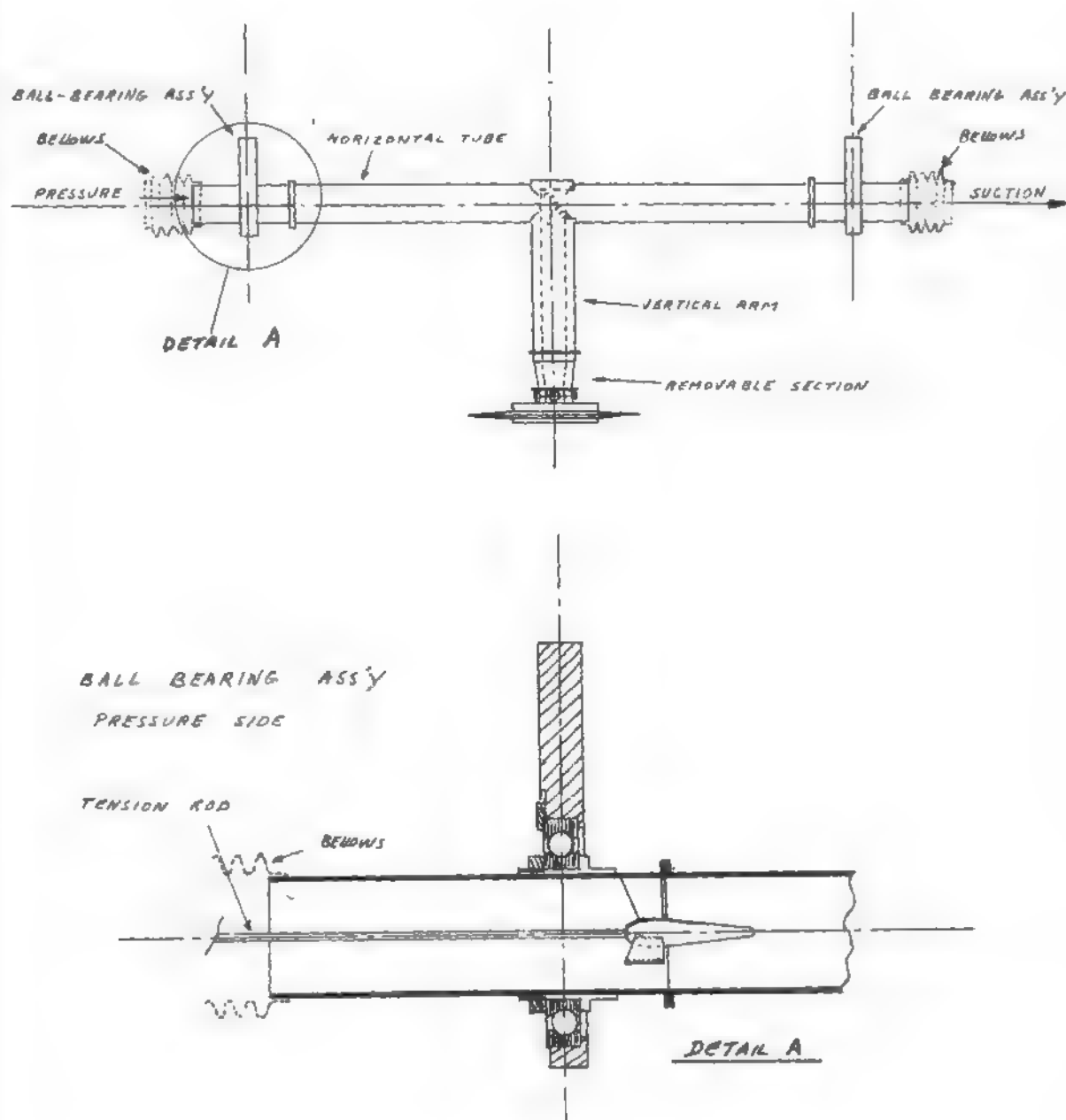


FIG-3 - DETAILS OF MODEL SUPPORT - A

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaquemin	MR 71	Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELFIG. 4 - DETAILS OF MODEL SUPPORT - B

WRITTEN BY

G. Jacquemin

CHECKED BY

J. E. Flynn

DATE

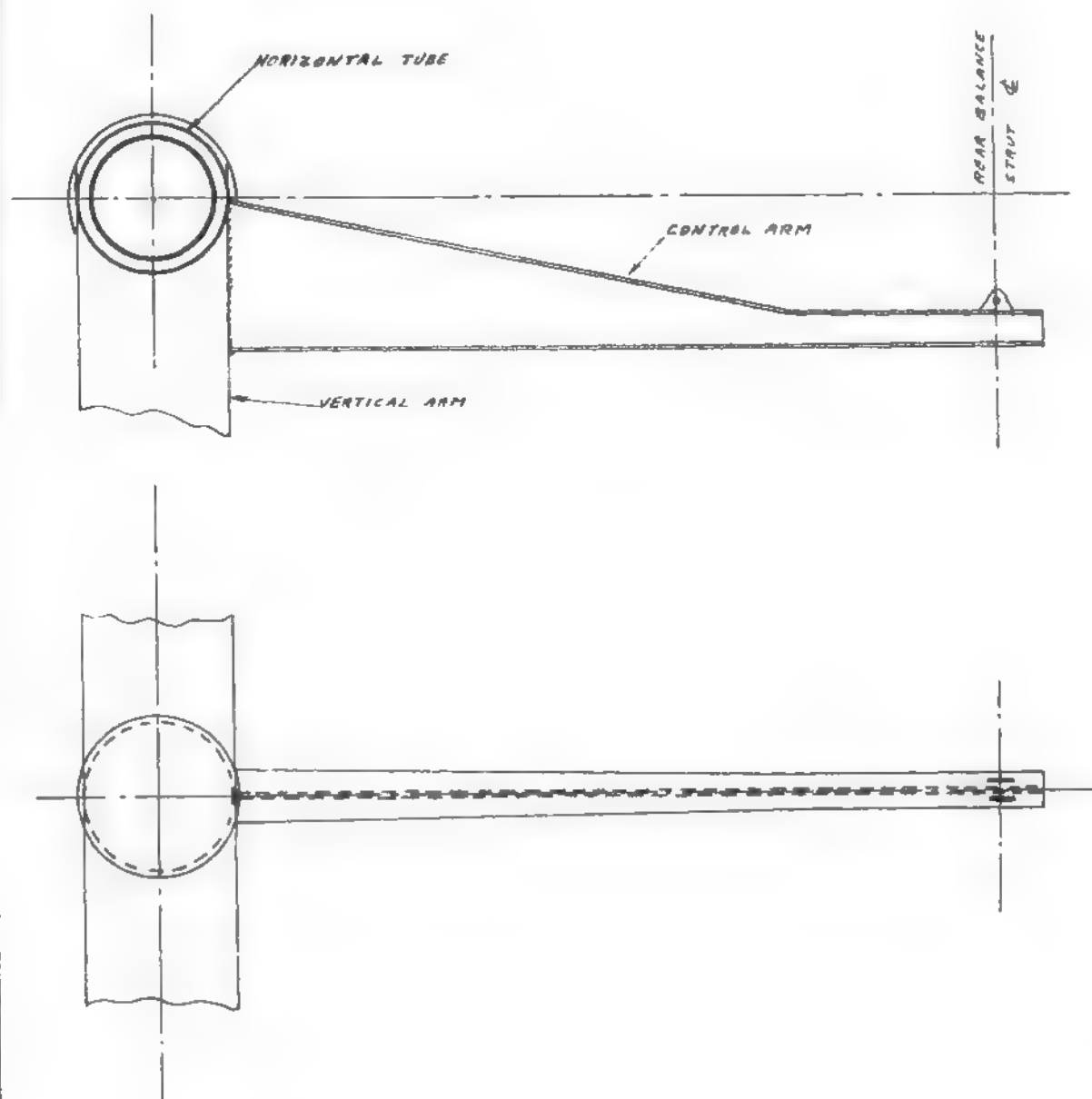
Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

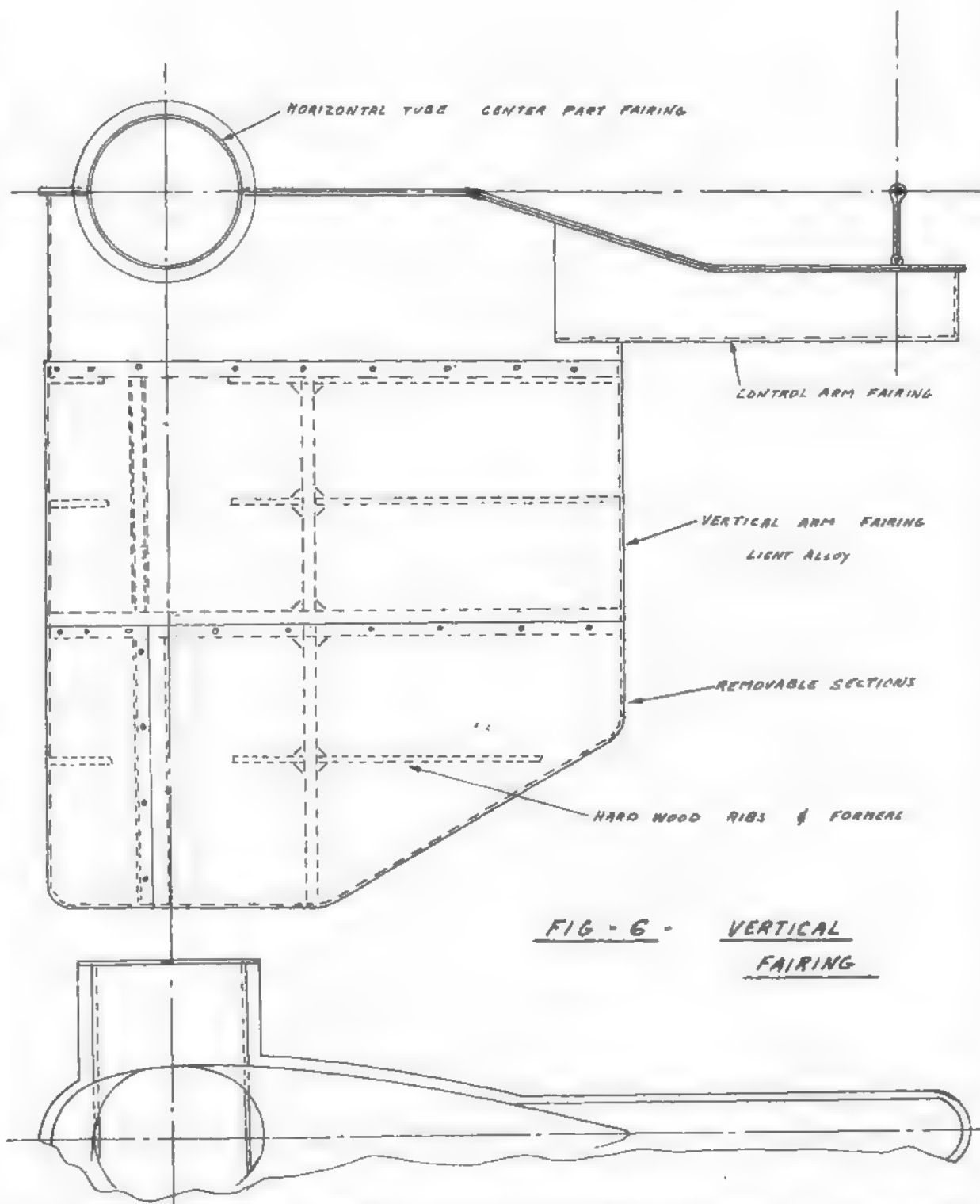
DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELFIG. 5 - CONTROL ARM

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
<i>G. Jaeger</i>	<i>PC Ferguson</i>	Sept. 1957		

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL-

WRITTEN BY

G. Jacques

CHECKED BY

R. F. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

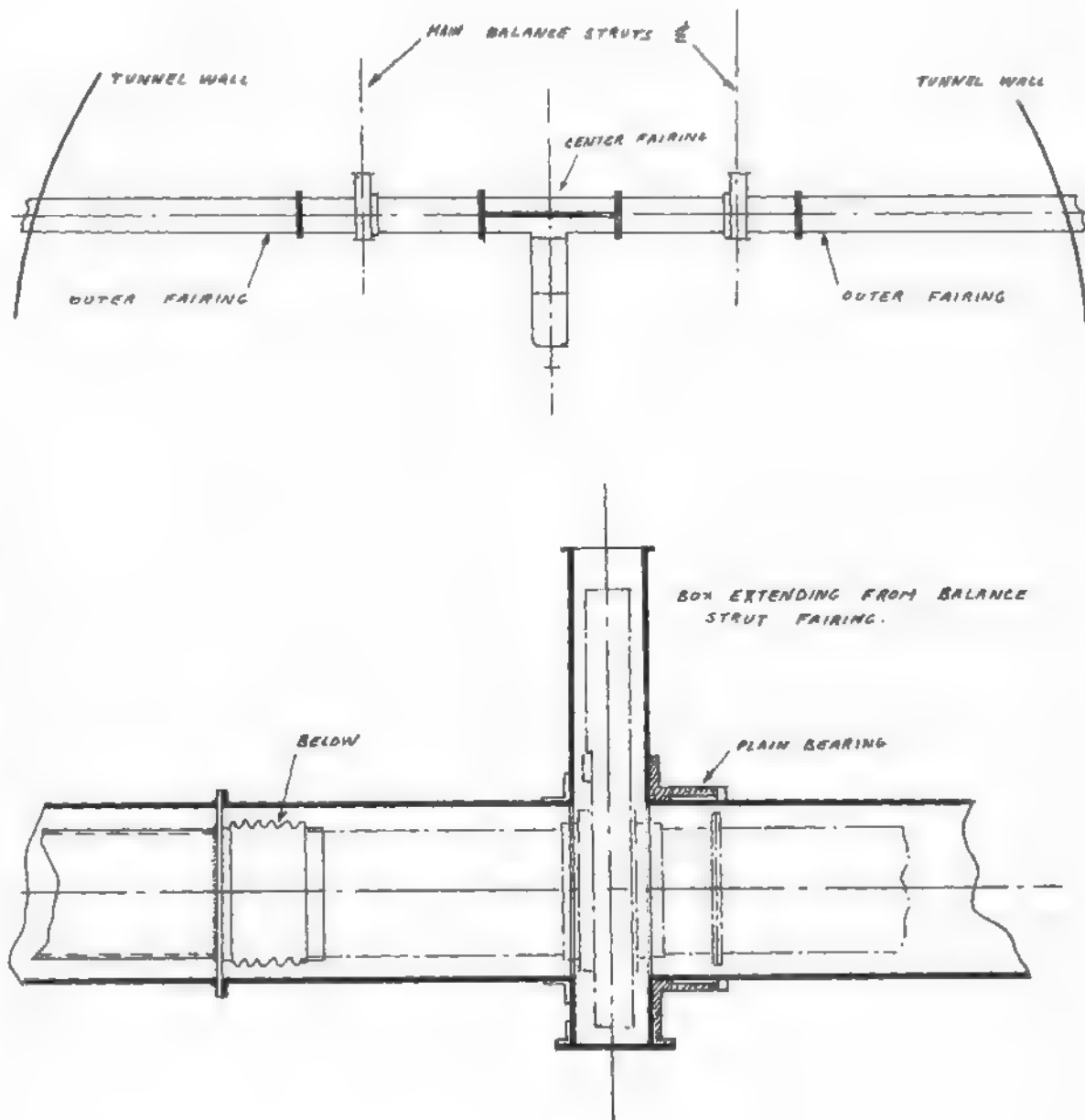
STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

FIG - 7 - HORIZONTAL FAIRING.

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemin	W. J. J. J. J.	Sept. 1957		

- STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -4-0LOAD ANALYSIS4-1LOADING CONSIDERATIONS-4.1.1 General

The model forces are taken by the ring load measuring gages and transferred through the model support to the 3 balance struts.

The fairing loads, both static and aerodynamic are taken by the 3 balance strut fairings.

4.1.2 Loads on the model

The model loads include: weight, aerodynamic loads, jet reaction and pressure forces on the ducting.

jet reaction. In the hovering cases, the jet reaction is entirely directed downward. In the flying cases, the jet reaction may be divided between lifting and propelling thrust. In all cases, it must be assumed that the jets will be operating with the tunnel stopped, thus the loads will not be relieved by air drag or lift. Pressure and suction on the ducting area at the inlet of the model will add a force normal to the plane of the model. These pressures and suction will be assumed uniform over the area thus having no moment about the center of the model. It should be noted that this may not be true in practice. However, since the moment is likely to be relatively small and owing to difficulties in obtaining reliable estimates, this moment has been neglected in the analysis. Also, the full delivery pressure and suction have been used while some drop is to be expected.

Aerodynamic loading. The model can be placed in the tunnel at angles α varying between -10° & 45° with a preferential range from -10° to 20° . The tunnel is to

WRITTEN BY

G. Jacques

CHECKED BY

L. C. F. 1957

DATE

Sept. 1957

ISSUEAIRCRAFT

~~SECRET~~

DECLASSIFIED

18

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -4-0 LOAD ANALYSIS.4-1 LOADING CONSIDERATIONS - CONT'D.

be operated at $q = 30$ PSF for the preferential range and its speed will be reduced for the range 20° to 45° so that the airloads do not exceed those produced in the preferential range thus allowing the use of smaller ring load measuring gages at the model attachment.

Since accurate values of C_L , C_D & C_m are not available, these parameters have been taken on the high side in order to ensure that the stressing of the model will amply cover all possible cases.

4-1-3 Model supporting structure The model supporting structure takes the model loading plus the static loads due to its own weight and pressure loads in the ducting

4-1-4 Fairings. The fairing loading is both static and aerodynamic: i.e. fairing weight and air drag. In addition, it has been assumed that a deviation of the airflow in the tunnel would not induce more than a 5° angle of attack to the vertical fairing hence producing a side load on the attachment of the fairing

4-1-5 Load Factor

A load factor $n = 4$ is applied to all parts of the structure except on the ring load measuring gages which are stressed for their operating conditions as per report AVRO/SPG/TR 87.

WRITTEN BY

G. Jacques

CHECKED BY

10/1/57

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS.4-2 MODEL LOADS4-2-1 LOADING CASES

HOVERING CASES

α	T	q psf	LIFT $E_L = \frac{L}{T}$	MOMENT $E_M = \frac{M}{Tb}$	SIDE LOAD $E_S = \frac{S}{T}$
0°	FULL	0	2.0	0	0
20°	FULL	0	2.0	.15	.30

Ref: AVRO/SPG/TR 29 & AVRO/SPG/TR 33

TRANSITION CASES

α	T	P	q psf	C_L	C_D	$C_m \frac{1}{4}$
-10°	0	FULL	30	-.30	.08	-.60
0°	0	0	30	.05	.05	-.20
0°	FULL	FULL	0			
20°	0	FULL	30	2.1	.60	.18
35°	0	FULL	30	2.8	1.20	.32
45°	0	FULL	18	3.0	1.70	* .98

* As determined from assumed distribution

Values of C_L , C_D & $C_m \frac{1}{4}$ are based on estimates from previous testingSYMBOLS

T: THRUST.

P: SUPPLY PRESSURE

q: TUNNEL DYNAMIC PRESSURE

 E_L , E_M , E_S : THRUST EFFICIENCIES IN HOVERING CASES C_L , C_D , $C_m \frac{1}{4}$: AERODYNAMIC COEF.

NOTE. TRANSITION CASES WERE SELECTED FOR MOST ADVERSE LOADS ON THE GAGES RATHER THAN ACTUAL TEST CASES.

WRITTEN BY

G. Jacques

CHECKED BY

11/12 p.m.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.H-0 LOAD ANALYSISH-2-1 LOADING CASESLOADS DUE TO INTERNAL PRESSURE:

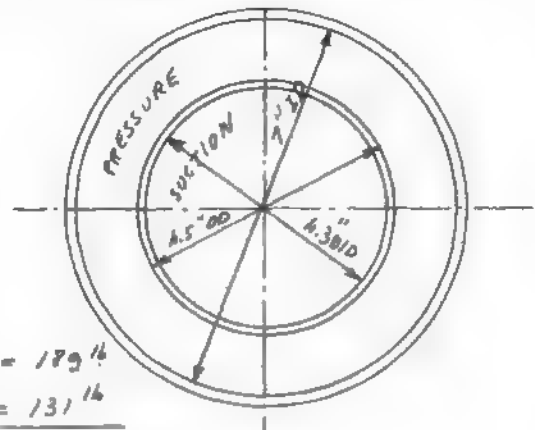
- max. model pressure: 30.74 PSI. (simulated hot thrust with hot nozzle area)
- max. operating pressure* : 22.96 PSIa in jet flow circuit
4.98 PSIa in intake flow circuit

*. based on: - simulated hot thrust with cold nozzle area

- pressure loss in jet flow circuit = 5x dynamic head based on ave. internal flow area and nozzle total head.
- pressure loss in intake flow circuit = 1.5x dynamic head based on intake flow area and intake total head.

$$\text{SUCTION AREA: } \frac{\pi}{4} 4.3^2 = 14.5 \text{ in}^2$$

$$\text{PRESSURE AREA: } \frac{\pi}{4} (7^2 - 4.5^2) = 22.6 \text{ in}^2$$

LOADS DUE TO PRESSURE.

$$\begin{aligned} \text{Force due to static pressure: } (22.96 - 14.7) 22.6 &= 189 \text{ lb} \\ \text{Force due to momentum flow:} &= 131 \text{ lb} \\ \text{net force} &= 320 \text{ lb} \end{aligned}$$

LOADS DUE TO SUCTION

$$\begin{aligned} \text{Force due to static pressure} &= (4.98 - 14.7) 14.5 = -138 \text{ lb} \\ \text{Force due to momentum flow:} &= 104 \text{ lb} \\ \text{net force:} &= -34 \text{ lb} \end{aligned}$$

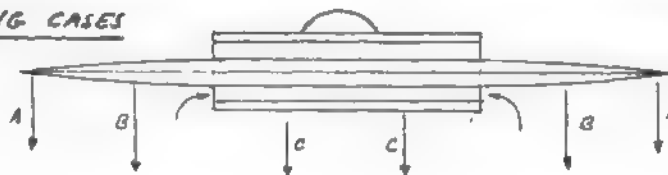
$$\text{net load on model: } 320 - 34 = 286 \text{ lb}$$

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	PC 1/1/57	Sept. 1957		

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4.0. LOAD ANALYSIS4.2.2. HOVERING CASESHORIZONTAL

Lift provided by A or B or A+B: 150 lb

Lift provided by C: 11 lb

Ground efficiency $\frac{L}{T} = 2.0$

Total lift on the model: $2.0 \times (150 + 11) = \underline{\underline{322 \text{ lb}}}$

- In the absence of more accurate data, $\frac{1}{2}$ of this load will be taken as concentrated at the jets, the other $\frac{1}{2}$ as a uniform pressure on the undersurface.

Wing area: $35.33 \frac{\pi}{4} = 978 \text{ in}^2$

Pressure: $\frac{161}{978} = .165 \text{ PSI}$

WRITTEN BY

G. Jacques

CHECKED BY

10/1/57

DATE

Sept. 1957

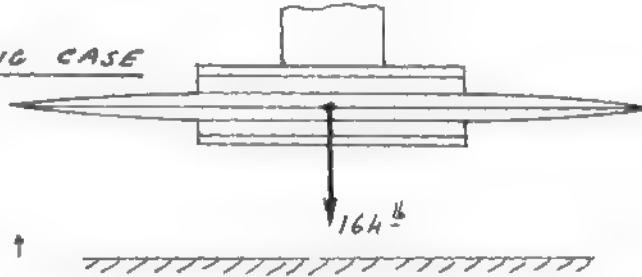
ISSUE

AIRCRAFT

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELA-0 LOAD ANALYSISA-2.2 HOVERING CASEHORIZONTAL
NET LOADS

LIFT : 322 lb ↑
 WEIGHT : 200 lb ↓
 PRESS : 286 lb ↓

$$\text{NET LOAD : } 200 + 286 - 322 = 164 \text{ lb } \downarrow$$

WRITTEN BY

G. Jacques

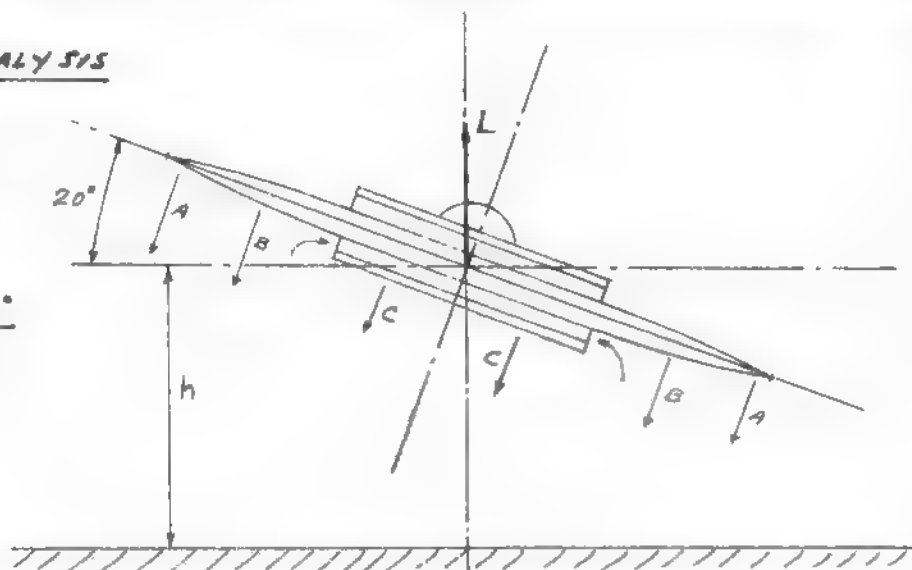
CHECKED BY

1:1 1957

DATE

Sept. 1957

ISSUEAIRCRAFT~~SECRET~~ DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELH-0 LOAD ANALYSISH-2.2 - HOVERING CASEHOVERING AT 20°
AIR LOADS

Efficiencies

LIFT IN GROUND. $E_L = \frac{L}{T} = 2.0$

$\therefore L = 2T$

MOMENT $E_M = \frac{M}{Tb} = .15$

$\therefore M = .15 Tb$

SIDE LOAD $E_S = \frac{S}{T} = .30$

$\therefore S = .30 T$

 Ref:
 AVRO/SPG/TR29
 AVRO/SPG/TR33

$$\left. \begin{array}{l} \text{Lift provided by A or B or A+B} \quad 150 \text{ lb} \\ \text{Lift provided by C} \quad 11 \text{ lb} \end{array} \right\} 161 \text{ lb}$$

Total Lift on the model: $2 \times 161 = 322 \text{ lb}$ normal to the floor.In the absence of more accurate data lift distribution will be taken as for hovering case at $\alpha = 0^\circ$.

Moment: $.15 \times 161 \times 15.3 = 383 \text{ in-lb}$

Side load: $.30 \times 161 = 48.3 \text{ lb}$ in any direction in the plane of the floor.

WRITTEN BY

G. Jacquin

CHECKED BY

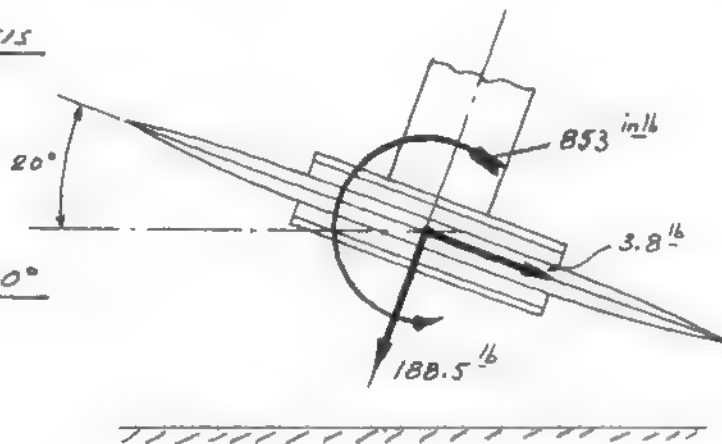
1-C / S

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS4-2-2 - HOVERING CASEHOVERING AT 20°
NET LOADSLIFT: 322^{lb} normal to the floor. ↑SIDE LOAD: 48.3^{lb} in any direction. Here taken as shown →MOMENT: 853^{in/lb} ↺WEIGHT: 200^{lb} normal to the floor ↓PRESSURE: 286^{lb} normal to the model ↓

Total force normal to the model:

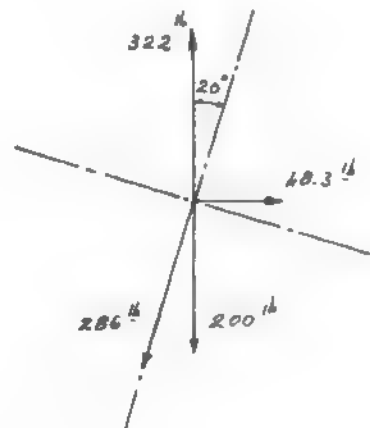
$$286 + 200 \cos 20^\circ - 322 \cos 20^\circ + 48.3 \sin 20^\circ =$$

$$286 + 188 - 302 + 16.5 = 188.5 \text{ } ^{\text{lb}} \downarrow$$

Total force parallel to the model:

$$200 \sin 20^\circ - 322 \sin 20^\circ + 48.3 \cos 20^\circ =$$

$$68.4 - 110 + 45.4 = 3.8 \text{ } ^{\text{lb}} \rightarrow$$



WRITTEN BY

G. Jacques

CHECKED BY

H. J. V. V.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

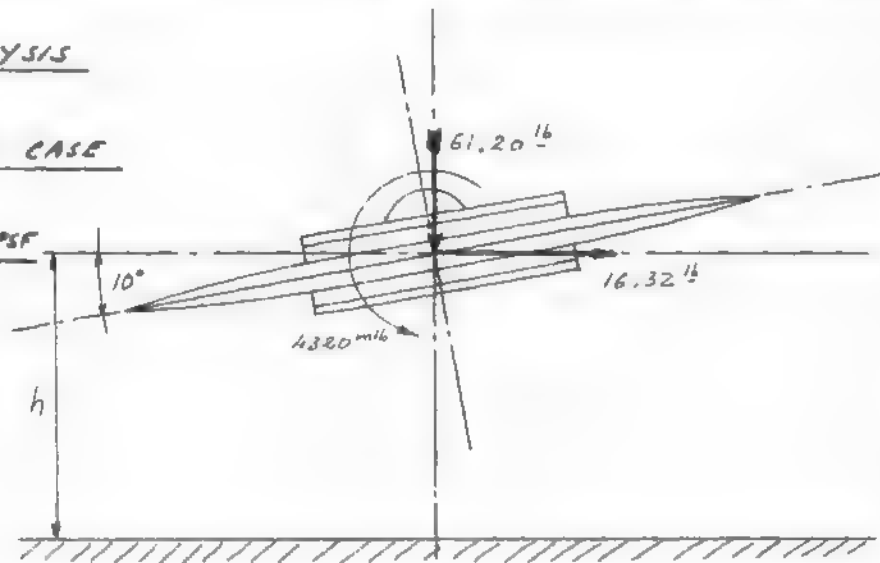
25

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS4-2-3 TRANSITION CASE-10° CASE - $q = 30$ PSFAIR LOADS

$C_L = -.30$

$C_D = .08$

$C_M = -.60$

Tunnel q 30 PSFWing area 6.8 ft²

Wing chord 2.94 ft

LIFT: $-.30 \times 6.8 \times 30 = -61.20 \text{ lb}$

DRAG: $.08 \times 6.8 \times 30 = 16.32 \text{ lb}$

MOMENT: $-.60 \times 2.94 \times 6.8 \times 30 = -360 \text{ ft lb} = -4320 \text{ in lb}$

WRITTEN BY

G. Jacquemont

CHECKED BY

1-11-57

DATE

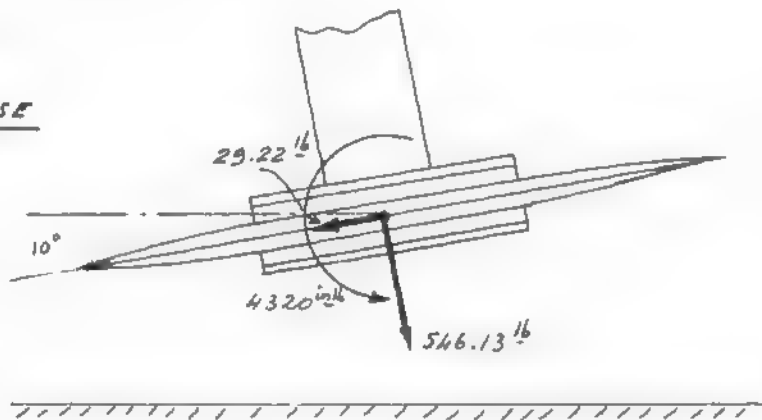
Sept. 1957

ISSUEAIRCRAFT~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{18}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS4-2-3 TRANSITION CASE10° CASE - $q = 30$ PSFNET LOADS

LIFT: $-61.20 \frac{lb}{ft^2}$ ↓
 DRAG: $16.32 \frac{lb}{ft^2}$ →
 MOMENT: $4320 \frac{in-lb}{ft^2}$ G
 WEIGHT: $200 \frac{lb}{ft^2}$ ↓
 PRESSURE: $286 \frac{lb}{ft^2}$ ↓

TOTAL FORCE NORMAL TO THE MODEL:

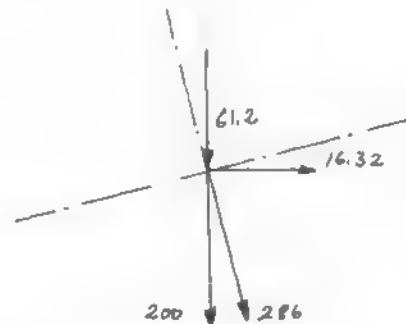
$$286 + 200 \cos 10^\circ + 61.2 \cos 10^\circ + 16.32 \sin 10^\circ =$$

$$286 + 197 + 60.30 + 2.83 = 546.13 \frac{lb}{ft^2}$$

TOTAL FORCE PARALLEL TO THE MODEL:

$$-200 \sin 10^\circ - 61.2 \sin 10^\circ + 16.32 \cos 10^\circ =$$

$$-34.7 - 10.6 + 16.08 = -29.22 \frac{lb}{ft^2}$$



WRITTEN BY

G. Jacquemin

CHECKED BY

10/12/57

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS4-2-3 TRANSITION CASEZERO THRUST : $\alpha = 0$ AIR LOADS

$$C_L = .05$$

$$C_D = .05$$

$$C_{M_{\frac{c}{4}}} = -.20$$

$$\text{Tunnel } q = 30 \text{ PSF}$$

$$\text{Wing area } 6.8 \text{ ft}^2$$

$$\text{LIFT : } .05 \times 6.8 \times 30 = 10.2 \text{ lb}$$

$$\text{DRAG : } .05 \times 6.8 \times 30 = 10.2 \text{ lb}$$

$$\text{MOMENT : } 2.94 \times -.20 \times 6.8 \times 30 = -120 \text{ ft lb} = -1440 \text{ in lb}$$

WRITTEN BY

G. Jacquemin

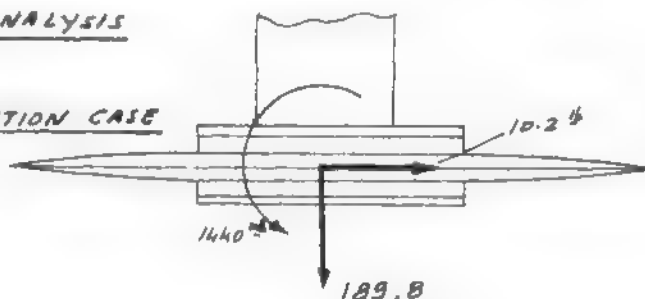
CHECKED BY

ME / a q-u-e-n

DATE

Sept. 1957

ISSUEAIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELA-0 - LOAD ANALYSISA-2-3 TRANSITION CASEZERO THRUST : $\alpha = 0$ NET LOADS

LIFT : $10.2^{lb} \uparrow$
 DRAG : $10.2^{lb} \rightarrow$
 MOMENT : $1440^{in^{lb}} \curvearrowleft$
 WEIGHT : $200^{lb} \downarrow$

TOTAL FORCE NORMAL TO MODEL :

$$+ 200 - 10.2 = 189.8^{lb}$$

TOTAL FORCE PARALLEL TO MODEL :

$$10.2^{lb}$$

WRITTEN BY

G. Jacques

CHECKED BY

11/10/57

DATE

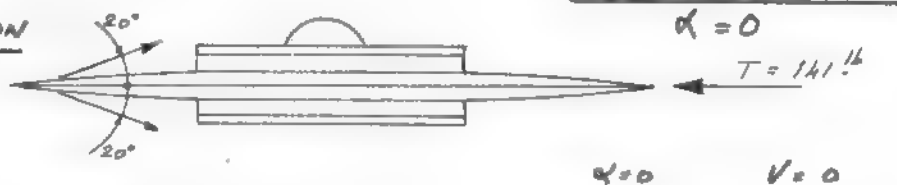
Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{18}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS4-2-3 TRANSITION CASE

Thrust: $150 \cos 20^\circ = 141 \text{ lb}$

WRITTEN BY

G. Jacquemin

CHECKED BY

1072 0110

DATE

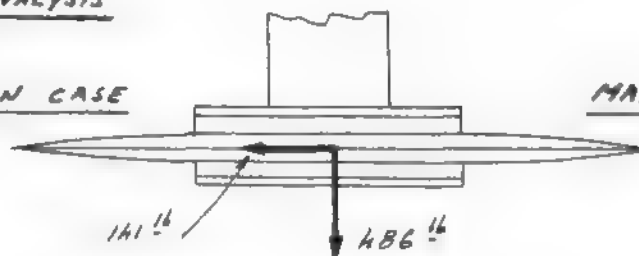
Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELA-0 LOAD ANALYSISA-2.3 TRANSITION CASEMAX THRUST CASE $\alpha = 0$

NET LOADS

THRUST : 141 lb \leftarrow WEIGHT : 200 lb \downarrow PRESSURE : 286 lb \downarrow

TOTAL FORCE NORMAL TO MODEL

$$200 + 286 = 486 \text{ lb } \downarrow$$

TOTAL FORCE PARALLEL TO MODEL

$$141 \text{ lb } \leftarrow$$

WRITTEN BY

G. Jacques

CHECKED BY

1/27/57 G. Jacques

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

4.0 - LOAD ANALYSIS

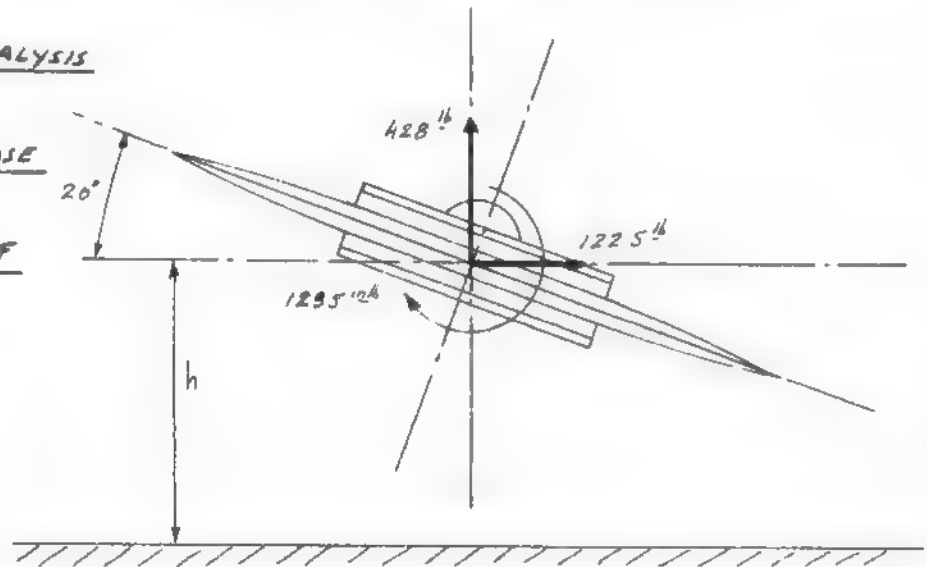
H-2-3 TRANSITION CASE

20° CASE - q = 30 PSF
AIRLOADS

$C_4 \cdot 2.1$

$C_D \cdot .60$

$C_{H_2} = .18$



Tunnel 9 : 30 PSF

Wing area: 6.8 ft²

Wing chord 2.94 ft

LIFI $2.1 \times 6.8 \times 30 = 428^{16}$

DRAG: $.60 \times 6.8 \times 30 = 122.5^{16}$

MOMENT: $-18 \times 6.8 \times 30 \times 2.94 = 108 \text{ ft-k} = 1295 \text{ in-k}$

WRITTEN BY

G. Jacquemini

CHECKED BY

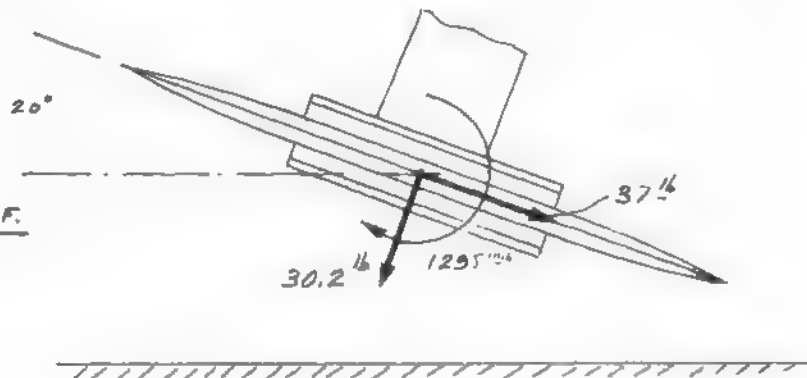
114

DATE _____

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS4-2-3 TRANSITION
CASE20° CASE - $q = 30$ PSF.
NET LOADS

LIFT : 428 lb \uparrow
 DRAG : 122.5 lb \rightarrow
 MOMENT : 1295 in-lb \curvearrowright
 WEIGHT : 200 lb \downarrow
 PRESSURE : 286 lb \downarrow

TOTAL FORCE NORMAL TO THE MODEL:

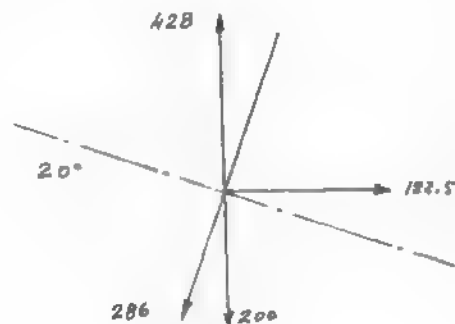
$$286 + 200 \cos 20^\circ - 428 \cos 20^\circ - 122.5 \sin 20^\circ =$$

$$286 + 188 - 402 - 41.8 = 30.2 \text{ lb} \downarrow$$

TOTAL FORCE PARALLEL TO THE MODEL

$$200 \sin 20^\circ - 428 \sin 20^\circ + 122.5 \cos 20^\circ =$$

$$68.4 - 146.4 + 115 = 37 \text{ lb} \rightarrow$$



WRITTEN BY

G. Jaeger

CHECKED BY

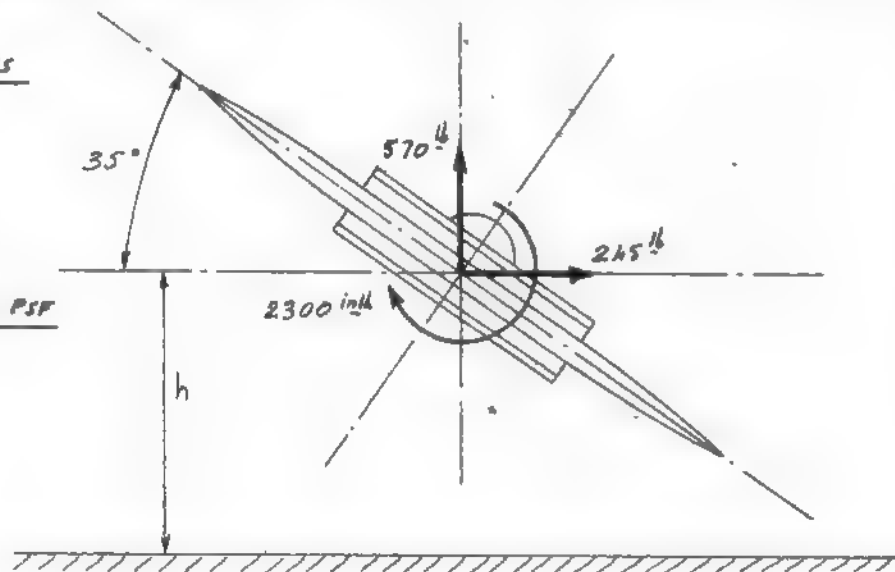
K. E. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELH-O. LOAD ANALYSISH-2-3 - TRANSITION
CASE35° CASE - $q = 30$ PSFAIRLOADS $C_L : 2.8$ $C_D : 1.20$ $C_{M_{cg}} : .32$ Tunnel $q : 30$ PSFWing area : 6.8 ft^2 Wing chord : 2.94 ft LIFT: $2.8 \times 6.8 \times 30 = 570 \text{ lb}$ DRAG: $1.20 \times 6.8 \times 30 = 245 \text{ lb}$ MOMENT: $.32 \times 6.8 \times 30 \times 2.94 = 192 \text{ ft lb} = 2300 \text{ in lb}$ WRITTEN BY

G. Jaeger

CHECKED BY

1.1 / 2 / 1957

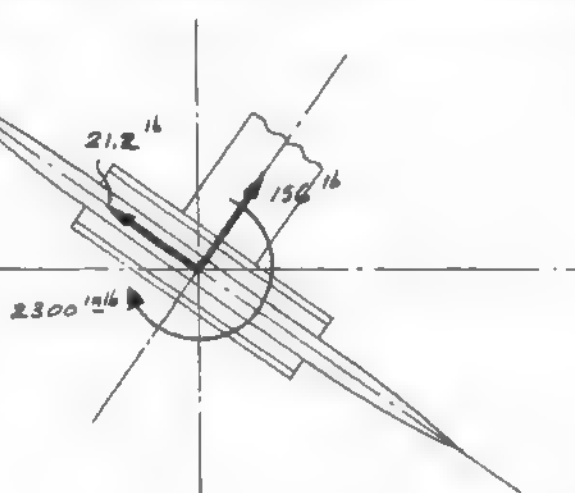
DATE

Sept. 1957

ISSUEAIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -4-0 LOAD ANALYSIS4-2-3 TRANSITION CASE35° CASE - $q = 30$ PSF.NET LOADS

LIFT : 570 ^{lb} ↑
 DRAG : 245 ^{lb} →
 MOMENT: 2300 ^{in-lb} ⊙
 WEIGHT : 200 ^{lb} ↓
 PRESSURE: 286 ^{lb} ↙



TOTAL FORCE NORMAL TO THE MODEL

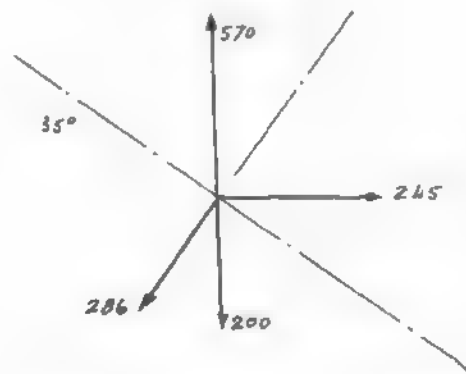
$$286 + 200 \cos 35^\circ - 570 \cos 35^\circ - 245 \sin 35^\circ =$$

$$286 + 164 - 466 - 140 = -156 \text{ } ^{\text{lb}} \uparrow$$

TOTAL FORCE PARALLEL TO THE MODEL

$$200 \sin 35^\circ - 570 \sin 35^\circ + 245 \cos 35^\circ =$$

$$104.8 - 327 + 201 = -21.2 \text{ } ^{\text{lb}} \leftarrow$$



WRITTEN BY

G. Jacques

CHECKED BY

H. J. J. J.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-0 LOAD ANALYSIS4-2-3 TRANSITION CASE45° CASE - $q = 80$ PSF

AIRLOADS

$$C_L = 3.0$$

$$C_D = 1.7$$

Wing area: 6.8 ft^2

TUNNEL AT 30 ft

LIFT.

$$3.0 \times 6.8 \times 30 = \underline{\underline{612 \text{ lb}}}$$

DRAG.

$$1.7 \times 6.8 \times 30 = \underline{\underline{347 \text{ lb}}}$$

Assuming max. distribution as shown
Center of Pressure.

$$X = \frac{M}{V}$$

Volume element:

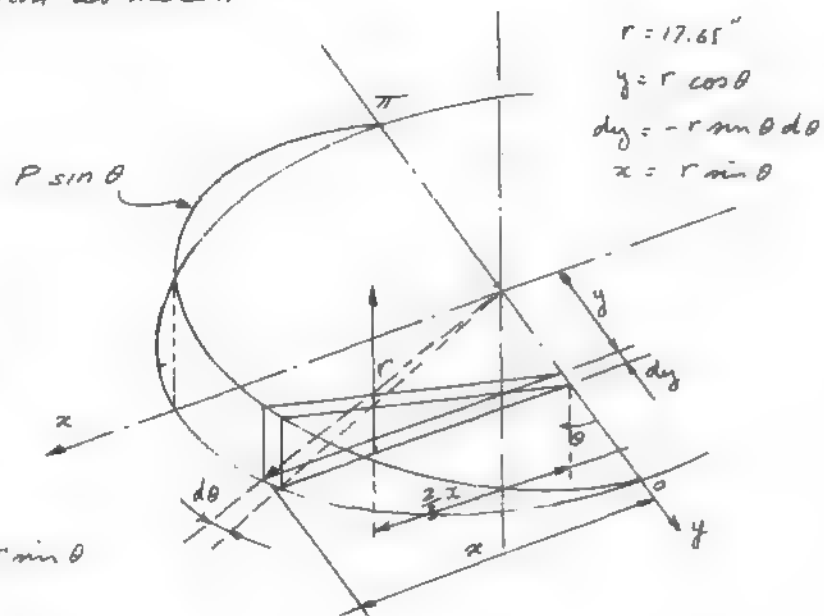
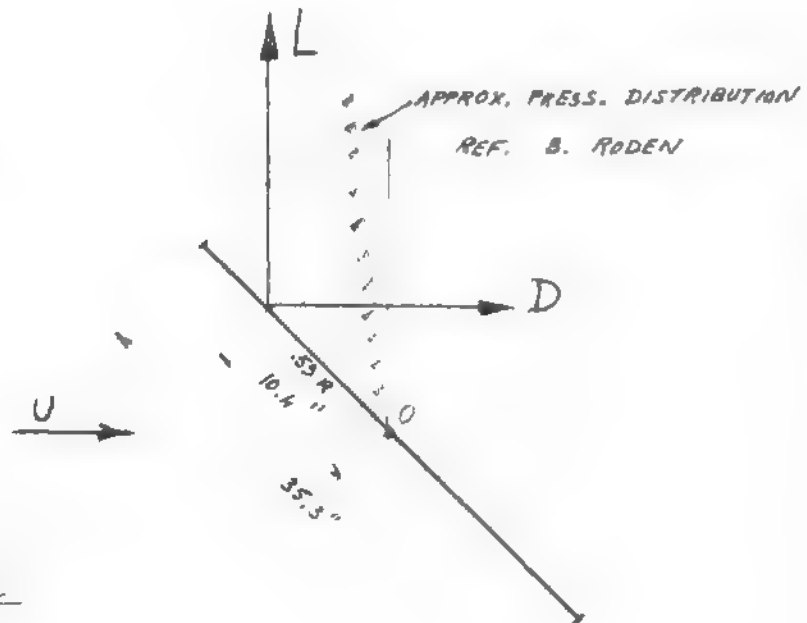
$$dV = \frac{1}{2} \pi dy P \sin \theta$$

$$dV = -\frac{P}{2} r^2 \sin^3 \theta d\theta$$

$$\therefore V = \int_{\pi}^0 -\frac{P}{2} r^2 \sin^3 \theta d\theta$$

$$dM = -\frac{P}{2} r^2 \sin^3 \theta d\theta \frac{2}{3} r \sin \theta$$

$$dM = -\frac{P}{3} r^3 \sin^4 \theta d\theta$$



WRITTEN BY

G. Jacques

CHECKED BY

Frederickson

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

$$M = \int_{\pi}^0 -\frac{P}{3} r^3 \sin^4 \theta d\theta \quad \text{LOAD ANALYSIS}$$

$$\therefore X = \frac{-\int_{\pi}^0 \frac{P}{3} r^3 \sin^4 \theta d\theta}{-\int_{\pi}^0 \frac{P}{2} r^2 \sin^3 \theta d\theta} = \frac{\frac{2}{3} r \int_{\pi}^0 \sin^4 \theta d\theta}{\int_{\pi}^0 \sin^3 \theta d\theta} = \frac{3}{16} \pi r = .59 r.$$

$$V = \frac{2}{3} P r^2 \quad \text{where } V \text{ is component normal to the disc}$$

$$\therefore X = .59 \frac{35.3}{2} = 10.4''$$

Moment of lift & drag about center of model

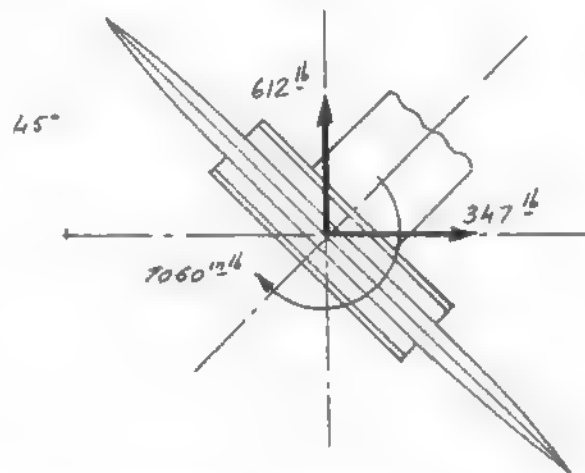
$$(612 + 347) \frac{10.4}{\sqrt{2}} = \underline{\underline{7060 \text{ in}^2 \text{ lb}}}$$

Component normal to surface of disc:

$$V = (612 + 347) \frac{1}{\sqrt{2}} = 678 \text{ lb} \quad \therefore P = \frac{3}{2} 678 \times \left(\frac{35.3}{2}\right)^2 = 5.26 \frac{\text{lb}}{\text{in}^2}$$

Component in the plane of the disc

$$(612 - 347) \frac{1}{\sqrt{2}} = 187.5 \text{ lb}$$



WRITTEN BY

G. Jacques

CHECKED BY

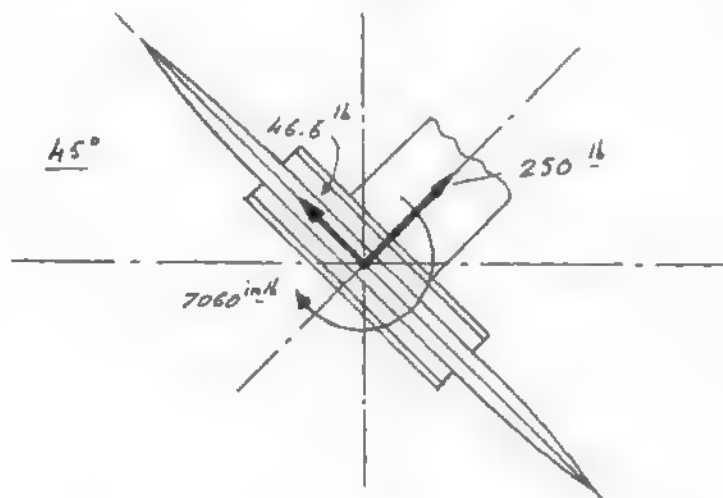
W. J. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELH-0 LOAD ANALYSISH-2-3 TRANSITION CASE45° CASE - $q = 30$ PSF.NET LOADS

LIFT: 612 lb ↑

DRAG: 347 lb →

MOMENT: 7060 in/lb ↺

WEIGHT: 200 lb ↓

PRESSURE: 286 lb ↓

TOTAL FORCE NORMAL TO THE MODEL:

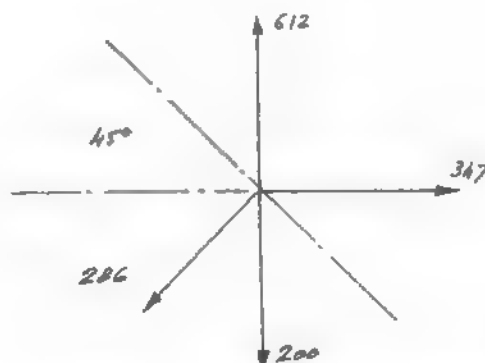
$$286 - 612 \cos 45^\circ + 200 \cos 45^\circ - 347 \sin 45^\circ =$$

$$286 - 433 + 141.4 - 245 = -250 \text{ lb } \times$$

TOTAL FORCE PARALLEL TO THE MODEL

$$200 \sin 45^\circ - 612 \sin 45^\circ + 347 \cos 45^\circ =$$

$$141.4 - 433 + 245 = -46.6 \text{ lb } \times$$



WRITTEN BY

G. Jacques

CHECKED BY

H. J. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.4-0 LOAD ANALYSIS4-2-3 TRANSITION CASE45° CASE - $q = 30$ PSF.Determination of $C_{M \frac{z}{2}}$ at $\alpha = 45^\circ$.

The moment about the center of the model is: 7060 $\frac{\text{in} \cdot \text{lb}}{\text{sec}^2}$
 This moment is due to aerodynamic forces alone. Hence the value of $C_{M \frac{z}{2}}$ is:

$$C_{M \frac{z}{2}} = \frac{M}{\frac{S}{2} q} = \frac{\frac{7060}{12}}{\frac{35.3}{12} \times 6.8 \times 30} = \frac{7060}{7200} = +.98$$

WRITTEN BY

G. Jaeger

CHECKED BY

H. F. Jaeger

DATE

Sept. 1957

ISSUE

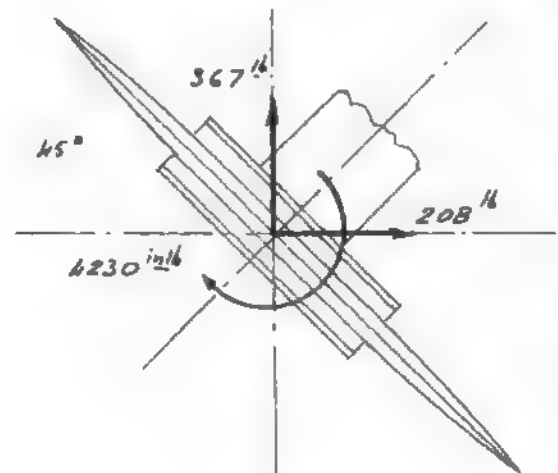
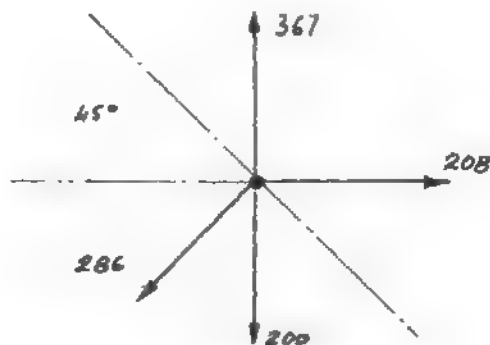
AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL-4.0 LOAD ANALYSIS4-2-3 TRANSITION CASE-CASE 45° TUNNEL OPERATING AT 18 1/2.

$$\text{Lift: } 612 \times \frac{18}{30} = 367 \text{ lb}$$

$$\text{Drag: } 347 \times \frac{18}{30} = 208 \text{ lb}$$

$$\text{Moment: } 7060 \times \frac{18}{30} = 4230 \text{ in lb}$$



FORCE NORMAL TO THE MODEL

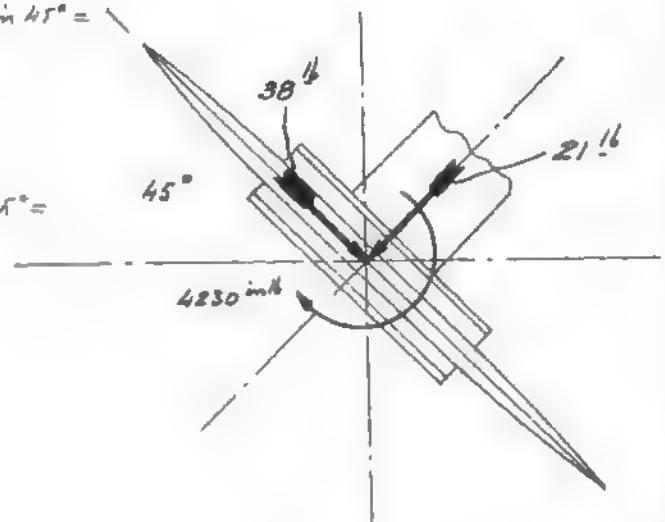
$$286 + 200 \cos 45^\circ - 367 \cos 45^\circ - 208 \sin 45^\circ =$$

$$286 + 141 - 259 - 147 = +21 \text{ lb}$$

FORCE PARALLEL TO THE MODEL

$$200 \sin 45^\circ + 208 \sin 45^\circ - 367 \sin 45^\circ =$$

$$141 + 147 - 259 = 38 \text{ lb}$$



WRITTEN BY

G. Jaques

CHECKED BY

J. Ferguson

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

40

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELA-0 LOAD ANALYSISA-2-4 SUMMARY OF CRITICAL LOADING CASES -

The critical case is the transition case for $\alpha = -10^\circ$ which give together the max. pitching moment and the max. downward load normal to the model

The max. drag load is obtained in the zero thrust case and the max. forward load in the max. thrust case

The max. upward load normal to the model occurs at $\alpha = 35^\circ$.

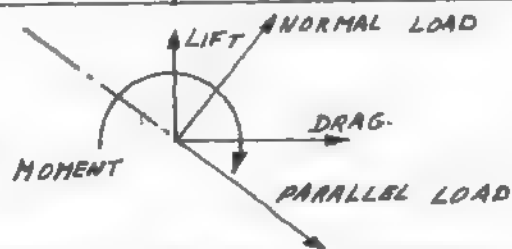
The lowering cases are not critical so; only the transition cases will be used to check the model support structure.

SUMMARY OF LOADING ON THE MODEL

LOADING CASES	AIRLOADS			NET LOADS.	
	LIFT lb	DRAG lb	MOMENT inlb	NORMAL LOAD lb	PARALLEL LOAD lb
HOVERING- $\alpha = 0^\circ$	322 ↑			164 ↓	
HOVERING- $\alpha = 20^\circ$	322 ↑	48.3 →	853 C	189.5 ↓	3.8 →
TRANSITION $\alpha = -10^\circ$	61.2 ↓	16.32 →	4320 C	546.13 ↓	29.22 ←
" ZERO THRUST	10.2 ↑	10.2 →	1440 C	189.8 ↓	10.2 →
" MAX. THRUST				486 ↓	141 ←
" $\alpha = +20^\circ$	428 ↑	122.5 →	1295 C	30.2 ↓	37 →
" $\alpha = +35^\circ$	570 ↑	245 →	2300 C	156 ↑	21.2 ←
" $\alpha = +45^\circ$ *	367 ↑	208 →	4230 C	21 ↓	38 →

* $q = 18$ PSF.

+VE SIGNS



WRITTEN BY

G. Jacques

CHECKED BY

1. J. G. J.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

41

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL-4.3 MODEL SUPPORT STRUCTURE LOADS4.3-1 LOADING CONSIDERATIONS

Since the model support structure is entirely shielded from the airflow, the only loads applied to it are its own weight and the loads coming from the model.

The model support structure is supported on the 3 balance struts. The two main balance struts take vertical and horizontal loads and the rear balance strut takes vertical load only.

Side loads on the model structure are due mostly to pressure in the delivery pipes. The side load due to model unblock has been estimated not to exceed 50 lb.

WRITTEN BY

G. Jaeger

CHECKED BY

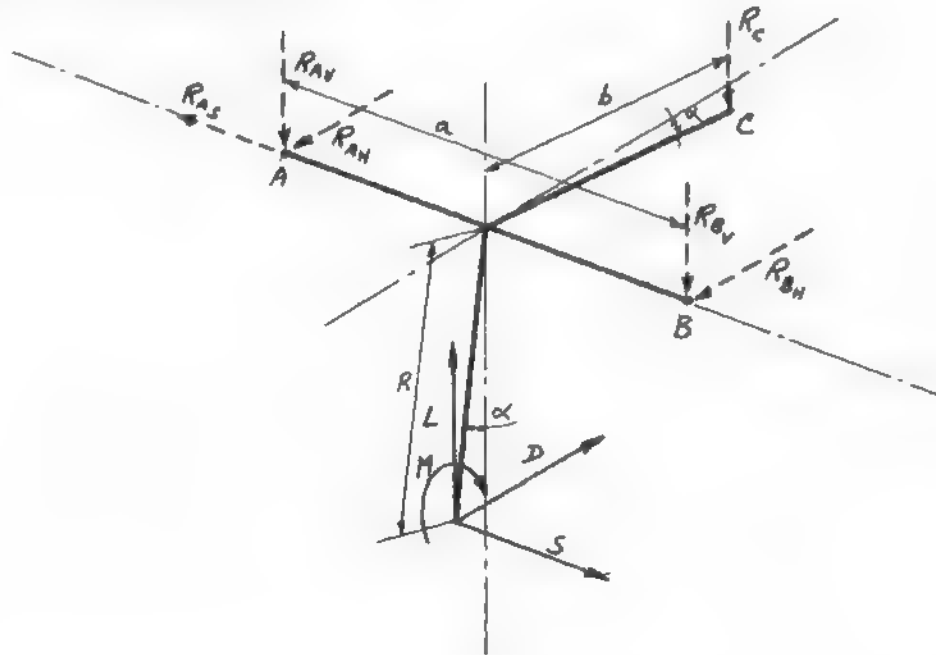
H. Ferguson

DATE

Sept. 1957

ISSUEAIRCRAFT~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-2 MODEL LOADS & REACTIONSEQUATIONS OF EQUILIBRIUM.

$$R_{AV} = \frac{L}{2} + \frac{M}{2b} - \frac{SR}{a} \cos \alpha + \left[\frac{LR \sin \alpha - DR \cos \alpha}{2b \cos \alpha} \right] = \frac{L}{2} + R \left[\frac{L}{2b} \tan \alpha - \frac{D}{2b} - \frac{S}{a} \cos \alpha \right] + \frac{M}{2b}$$

$$R_{BV} = \frac{L}{2} + R \left[\frac{L}{2b} \tan \alpha - \frac{D}{2b} + \frac{S}{a} \cos \alpha \right] + \frac{M}{2b}$$

$$R_C = -\frac{R}{b} \left[L \tan \alpha - D \right] - \frac{M}{b}$$

$$R_{AH} = \frac{D}{2} - \frac{SR}{a} \sin \alpha$$

$$R_{BH} = \frac{D}{2} + \frac{SR}{a} \sin \alpha$$

$$R_{AS} = S$$

WRITTEN BY

G. Jacquin

CHECKED BY

A. C. J. G. J. G. J.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-2 MODEL LOADS & REACTIONSEQUATIONS OF EQUILIBRIUM - CONT'D.

We have. $a = 80"$ $b = 48"$ $R = 50"$

furthermore $S = 50^{\text{lb}}$ assumed for all cases.
and $\alpha = -10^\circ, 0^\circ, 20^\circ \text{ \& } 45^\circ$

Then, Substituting

$$R_{AV} = \frac{L}{2} + \frac{M}{96} + .522 L \tan \alpha - .522 D - 31.25 \cos \alpha$$

$$R_{BV} = \frac{L}{2} + \frac{M}{96} + .522 L \tan \alpha - .522 D + 31.25 \cos \alpha$$

$$R_C = -1.042 [L \tan \alpha - D] - \frac{M}{48}$$

$$R_{AH} = \frac{D}{2} - 31.25 \sin \alpha$$

$$R_{BH} = \frac{D}{2} + 31.25 \sin \alpha$$

$$R_{AS} = 50^{\text{lb}}$$

LOADING CONDITIONS

α	-10°	0	0 MAX. THRUST	20°	45° g = 18 PF.
L	-61.20	10.2	0	428	367
D	16.32	10.2	-141	122.5	208
M	-4320	-1440	0	1295	4230
$\sin \alpha$	-.1737	0	0	.342	.707
$\cos \alpha$.985	1.0	1.0	.940	.707
$\tan \alpha$	-.176	0	0	.364	1.0

Ref. SECTION 4-2-4

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. J. J. J.	1-15-57	Sept. 1957		

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

44

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS.4-3-2 MODEL LOADS & REACTIONS.CALCULATION OF LOADS.-10° CASE.

$$R_{AV} = -\frac{61.2}{2} - \frac{4320}{96} + .522(-61.2)(-.176) - (.522 \times 16.32) - (31.25 \times .985)$$

$$= -30.6 - 45 + 5.62 - 8.52 - 30.8 = \underline{-109.30} \text{ lb} \quad \uparrow$$

$$R_{BV} = -30.6 - 45 + 5.62 - 8.52 + 30.8 = \underline{-47.70} \text{ lb} \quad \uparrow$$

$$R_C = -1.042 \left[-61.2 \times -.176 - 16.32 \right] - \frac{4320}{48} = +5.80 + 90 = \underline{+95.80} \text{ lb} \quad \downarrow$$

check on total vertical load: $-109.30 - 47.70 + 95.80 = 61.2 \text{ lb} @ 61.2 \text{ lb}$ OK

$$R_{AH} = \frac{16.32}{2} - 31.25(-.1737) = 8.16 + 5.43 = \underline{13.59} \text{ lb} \quad \leftarrow$$

$$R_{BH} = \frac{16.32}{2} + 31.25(-.1737) = 8.16 - 5.43 = \underline{2.73} \text{ lb} \quad \leftarrow$$

check on total horizontal load: $13.59 + 2.73 = 16.32 @ 16.32 \text{ lb}$ OK

$$R_{AS} = \underline{50} \text{ lb} \quad \nearrow$$

WRITTEN BY

G. Jaeger

CHECKED BY

A. J. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

45

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.A-3 MODEL SUPPORT STRUCTURE LOADSA-3-2 MODEL LOADS & REACTIONS.CALCULATION OF LOADS - CONT'D0° CASE.

$$R_{AV} = \frac{10.2}{2} - \frac{1440}{96} + .522 \times 10.2 \times 0 - .522 \times 10.2 - 31.25 \times 1.0 =$$

$$5.1 - 15 + 0 - 5.32 - 31.25 = \underline{\underline{-46.47^{lb} \uparrow}}$$

$$R_{BV} = 5.1 - 15 + 0 - 5.32 + 31.25 = \underline{\underline{+16.03^{lb} \downarrow}}$$

$$R_C = -1.042 [10.2 \times 0 - 10.2] - \frac{-1440}{48} =$$

$$+10.62 + 30 = \underline{\underline{+40.62^{lb} \downarrow}}$$

Check on total vertical load: $40.62 + 16.03 - 46.47 = 10.18 @ 10.20.$

$$R_{AH} = \frac{10.2}{2} - 31.25(0) = \underline{\underline{5.1^{lb} \rightarrow}}$$

$$R_{BH} = \frac{10.2}{2} + 31.25(0) = \underline{\underline{5.1^{lb} \leftarrow}}$$

Check on total horizontal load: $5.1 + 5.1 = 10.2 @ 10.2$

$$R_{AS} = \underline{\underline{50^{lb} \nearrow}}$$

WRITTEN BY

G. Jacques

CHECKED BY

1.2 Feb 40 11

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-2 MODEL LOADS & REACTIONS.CALCULATION OF LOADS - CONT'D.0° CASE - MAX. THRUST -

$$R_{AV} = \frac{0}{2} - \frac{0}{96} + .522 \times 0 \times 0 - .522(-141) - (31.25 \times 1)$$

$$= + 73.5 - 31.25 = \underline{\underline{42.25 \text{ lb}}} \downarrow$$

$$R_{BV} = 73.5 + 31.25 = \underline{\underline{104.5 \text{ lb}}} \downarrow$$

$$R_C = -1.042 \left[0 \times 0 - (-141) \right] - \frac{0}{48} = \underline{\underline{-147 \text{ lb}}} \uparrow$$

Check on total Vert. load: $104.5 + 42.25 - 147 = -.25 \text{ @ } 0$

$$R_{AH} = \frac{-141}{2} - 31.25 \times 0 = \underline{\underline{-70.5 \text{ lb}}} \rightarrow$$

$$R_{BH} = \frac{-141}{2} + 31.25 \times 0 = \underline{\underline{-70.5 \text{ lb}}} \rightarrow$$

Check on total Horizontal load: $-70.5 - 70.5 = -141 \text{ lb @ } -141 \text{ lb}$

$$R_{AS} = \underline{\underline{50 \text{ lb}}} \swarrow$$

WRITTEN BY

G. Jaeger

CHECKED BY

/ /

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

47

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELA-3 MODEL SUPPORT STRUCTURE LOADSA-3-2 MODEL LOADS & REACTIONSCALCULATION OF LOADS - CONT'D.20° CASE -

$$R_{AV} = \frac{428}{2} + \frac{1535}{96} + (.522 \times 428 \times .364) - (.522 \times 122.5) - (31.25 \times .94) =$$

$$= 214 + 16 + 81.3 - 64 - 29.4 = \underline{217.9} \text{ lb} \quad \downarrow$$

$$R_{BV} = \frac{428}{2} + \frac{1535}{96} + (.522 \times 428 \times .364) - (.522 \times 122.5) + (31.25 \times .94) =$$

$$= 214 + 16 + 81.3 - 64 + 29.4 = \underline{276.7} \text{ lb} \quad \downarrow$$

$$R_C = -1.042 [428 \times .364 - 122.5] - \frac{1535}{48} = -34.9 - 32 = \underline{-66.9} \text{ lb} \quad \uparrow$$

Check on Total Vertical Load: $217.9 + 276.7 - 66.9 = 427.7 \text{ lb} \quad @ 428$

$$R_{AH} = \frac{122.5}{2} - 31.25 \times .342 = 61.25 - 10.68 = \underline{50.57} \text{ lb} \quad \leftarrow$$

$$R_{BH} = \frac{122.5}{2} + 31.25 \times .342 = 61.25 + 10.68 = \underline{71.93} \text{ lb} \quad \leftarrow$$

Check on total horizontal load: $50.57 + 71.93 = 122.5 \quad @ 122.5$

$$R_{AS} = \underline{50} \text{ lb} \quad \nwarrow$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	11/1/57	Sept. 1957		

~~SECRET~~

DECLASSIFIED

AVRO/SPG/TR 112

~~SECRET~~

48

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-2 MODEL LOADS & REACTIONSCALCULATION OF LOADS - CONT'D.45° CASE -

$$R_{AV} = \frac{367}{2} + \frac{4230}{96} + (.522 \times 367 \times 1.0) - (.522 \times 208) - (31.25 \times .707) =$$

$$183.5 + 44 + 192 - 108.5 - 22.1 = \underline{\underline{288.9^{lb}}} \quad \downarrow$$

$$R_{BV} = \frac{367}{2} + \frac{4230}{96} + (.522 \times 367 \times 1.0) - (.522 \times 208) + (31.25 \times .707) =$$

$$183.5 + 44 + 192 - 108.5 + 22.1 = \underline{\underline{333.1^{lb}}} \quad \downarrow$$

$$R_C = -1.042 \left[(367 \times 1) - 208 \right] - \frac{4230}{48} = -166 - 88.2 = \underline{\underline{-254.2^{lb}}} \quad \uparrow$$

Check on total vertical load: $288.9 + 333.1 - 254.2 = 367.8$ @ 367

$$R_{AH} = \frac{208}{2} - (31.25 \times .707) = 104 - 22.1 = \underline{\underline{81.9^{lb}}} \quad \leftarrow$$

$$R_{BH} = \frac{208}{2} + (31.25 \times .707) = 104 + 22.1 = \underline{\underline{126.1^{lb}}} \quad \leftarrow$$

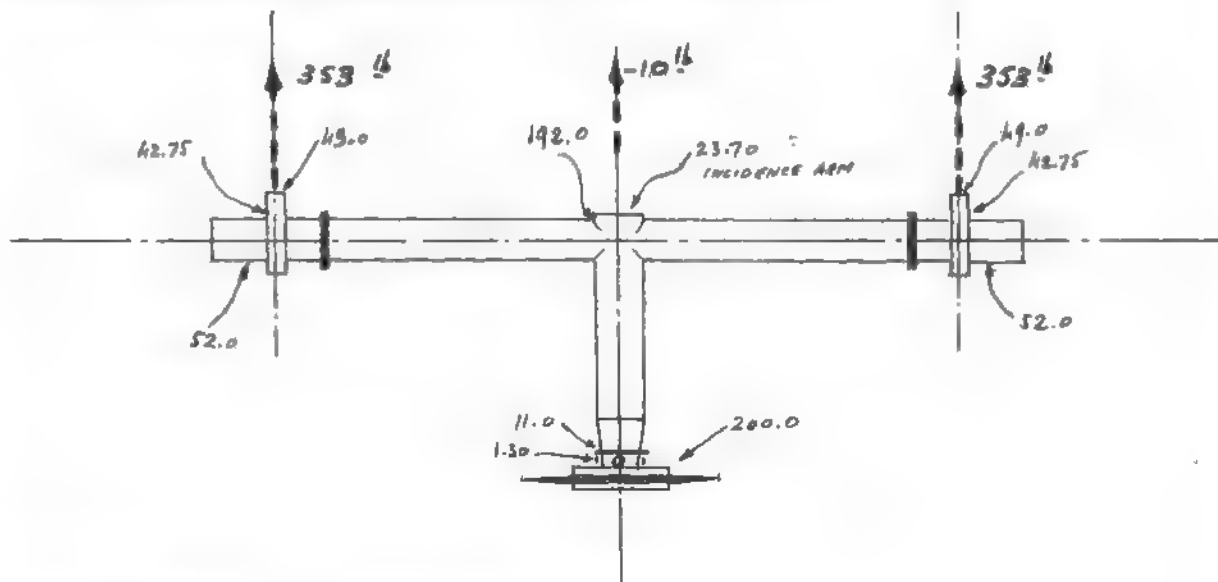
Check on total horizontal load: $81.9 + 126.1 = 208$ @ 208

$$R_{AS} = 50^{lb} \quad \swarrow$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemin	1 - 1	Sept. 1957		

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.4-3 MODEL SUPPORT STRUCTURE LOADS4-3-3 LOADS DUE TO STATIC WEIGHT & REACTIONS.MODEL MOUNT - TOTAL WEIGHT, INCLUDING MODEL.TOTAL WEIGHT OF ASSEMBLY -

$$200 + 1.30 + 11.0 + 192 + 24.67 + 2(49 + 42.75 + 52) =$$

$$200 + 1.30 + 11.0 + 192 + 24.67 + 287.5 = \underline{\underline{715.80 \text{ lb}}}$$

Load on balance struts -

Main struts:

$$- \frac{715.8 - 10}{2} \approx - 353 \text{ lb}$$

Incidence strut:

$$- 24 \frac{20}{48} = - 10 \text{ lb}$$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

1. 7. 1. 1.

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-3 LOADS DUE TO STATIC WEIGHT & REACTIONSREACTION ON INCIDENCE STRUT FOR ANGLES $\neq 0$.MODEL MOUNT.-10°:

Moment about point O.

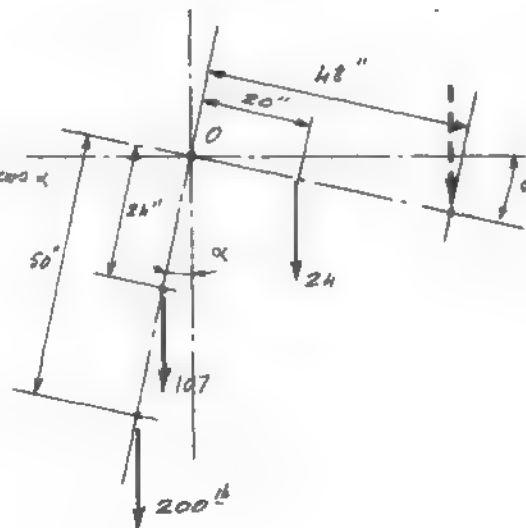
$$\begin{aligned}
 &-(107 \times 24 \sin \alpha) - (200 \times 50 \sin \alpha) + (24 \times 20) \cos \alpha \\
 &= -\sin \alpha (107 \times 24 + 200 \times 50) + 480 \cos \alpha \\
 &= -12570 \sin \alpha + 480 \cos \alpha
 \end{aligned}$$

Reaction at incidence strut:

$$\frac{-12570 \sin \alpha + 480 \cos \alpha}{48 \cos \alpha} = -262 \tan \alpha - 10$$

Reaction when $\alpha = -10^\circ$

$$-10 + 262 \tan(-10^\circ) = \underline{\underline{-56.2 \text{ lb}}}$$



Reactions on main struts:

$$-\left(\frac{715.8 - 56.2}{2}\right) = \underline{\underline{-329.8 \text{ lb}}}$$

+20°

Reaction at incidence strut:

$$262 \tan(\alpha) - 10 = 262 \tan(20^\circ) - 10 = \underline{\underline{85.2 \text{ lb}}}$$

Reactions on main struts

$$-\left(\frac{715.8 + 85.2}{2}\right) = \underline{\underline{-400.5 \text{ lb}}}$$

WRITTEN BY

G. Jacques

CHECKED BY

1 1 1

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-3 LOADS DUE TO STATIC WEIGHT & REACTIONSREACTION ON INCIDENCE STRUT FOR ANGLES $\alpha \neq 0$ CONT'D+ 45°

Reaction at incidence strut:

$$-262 \tan \alpha + 10 = -262 \tan 45^\circ + 10 = -252 \text{ lb}$$

Reactions on main struts.

$$= \frac{715.8 + 252}{2} = -483.9 \text{ lb}$$

SUMMARY OF STATIC STRUT REACTIONS-

α°	MAIN STRUT	INCIDENCE STRUT.
-10	-329.8	-56.2
0	-353.0	-10.0
20	-400.5	-85.2
45	-483.9	-252

ALL LOADS IN lb

WRITTEN BY

G. J. J. J.

CHECKED BY

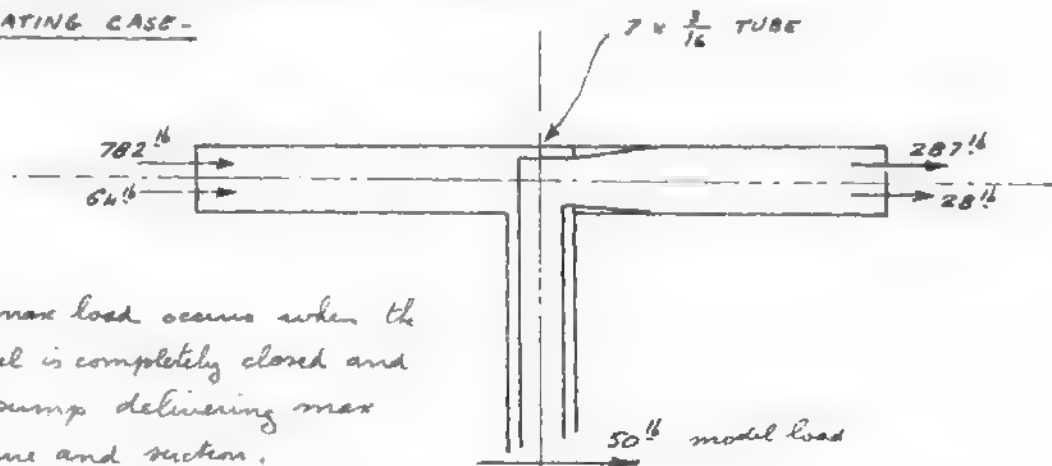
H. J. J. J.

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-4 LOADS DUE TO PRESSURE & SUCTION.HORIZONTAL LOAD ON MODEL SUPPORT.OPERATING CASE-

The max load occurs when the model is completely closed and the pump delivering max pressure and suction.

In the operating case, the load decrease to 782^{lb} static load and 64^{lb} reaction to mass flow on the pressure side and 287^{lb} static load and 28^{lb} reaction to mass flow on the suction side.

$$\text{Load: } 782 + 64 + 28 + 287 = \underline{1211 \text{ lb}}$$

PRESSURE CASE:

$$\text{TUBE AREA: } \left[7 - (2 \times .187) \right]^2 \frac{\pi}{4} = 34.5 \text{ in}^2$$

MAX. ABS. PRESSURE : 44.7 PSIA
MIN. ABS. PRESSURE : 6.34 PSIA

$$\text{TOTAL LOAD: } (44.7 - 6.34) 34.50 + 50 = \underline{1372 \text{ lb}}$$

WRITTEN BY

G. Jacques

CHECKED BY

/ /

DATE

Sept. 1957

ISSUE

AIRCRAFT

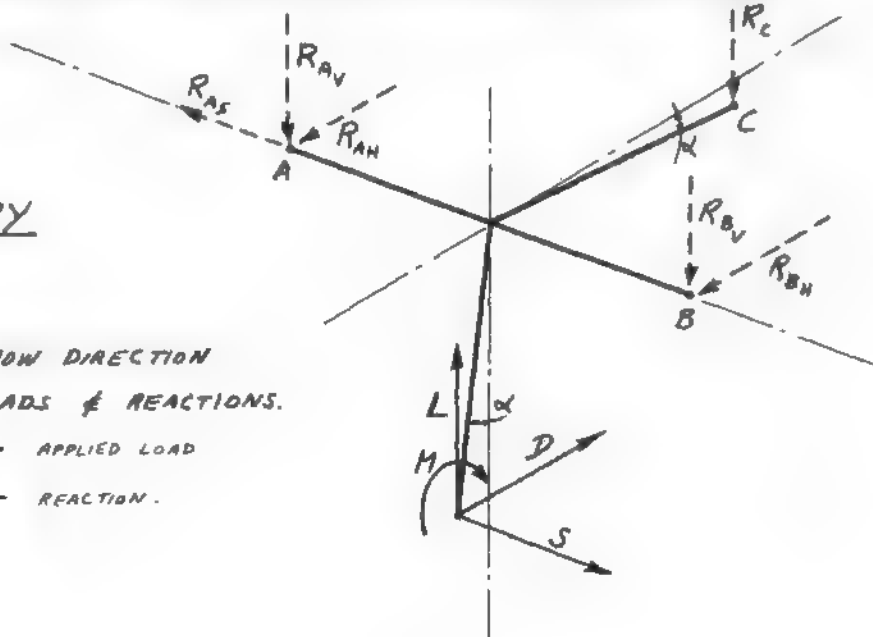
~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-3 MODEL SUPPORT STRUCTURE LOADS4-3-5 NET LOADS & REACTIONSBALANCE STRUTS LOADS DUE TO MODEL LOADS ONLY -SUMMARY

ARROWS SHOW DIRECTION
OF +VE LOADS & REACTIONS.

———— APPLIED LOAD
----- REACTION.



α	-10°	0	0 MAX. THRUST.	20°	45°
R_{AV}	-109.31	-46.47	42.25	217.9	288.9
R_{BV}	-47.71	16.03	104.5	276.7	333.1
R_C	-95.82	40.62	-147	-66.9	-254.2
R_{AH}	13.59	5.1	-70.5	50.57	81.9
R_{BH}	2.73	5.1	-70.5	71.93	126.1
R_{AS}	50	50	50	50	50
R_{AS} TOTAL OPERATING.			1211		
PRESS. CASE	1372	1372		1372	1372

-VE REACTION IS A DOWN OR FORWARD LOAD ON THE STRUT

WRITTEN BY

G. Jacques

CHECKED BY

I. C. Jacques

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

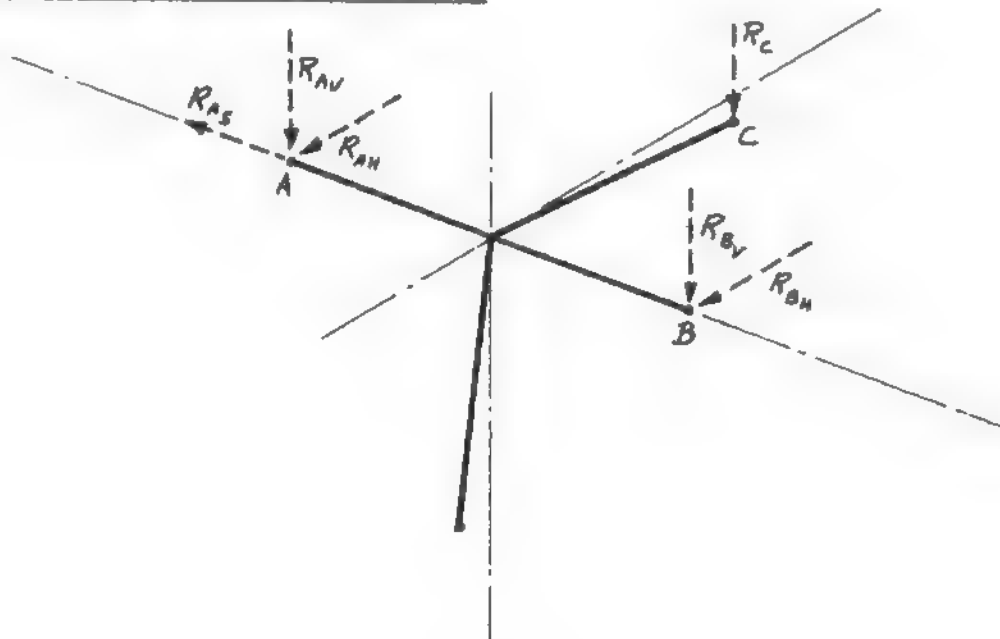
~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

4-3 MODEL SUPPORT STRUCTURE LOADS

4-3-5 NET LOADS & REACTIONS -

NET LOADS ON BALANCE STRUTS



α	-10°	0	0 MAX. THRUST.	20°	45° 18 g.
R_{AV}	- 439.11	- 399.47	- 310.75	- 182.6	- 195.0
R_{BV}	- 377.91	- 336.97	- 248.5	- 123.8	- 150.8
R_C	+ 39.62	+ 30.62	- 157.0	+ 18.3	- 2.2
R_{AN}	+ 13.59	+ 5.10	- 70.5	+ 50.57	+ 81.9
R_{BN}	+ 2.73	+ 5.10	- 70.5	+ 71.93	+ 126.1

- REACTION R_{AS} is not shown here as it is not taken by the struts (See Fairing loads).
- Reactions R_{AV} & R_{BV} and R_{AN} & R_{BN} are interchangeable depending on the direction of the side load on the model.
- In the above table : -ve reaction is a down or forward load on the strut.

~~SECRET~~

DECLASSIFIED

55

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-4FAIRING LOADS4-4-1LOADING CONSIDERATIONS

The fairings are loaded by aerodynamic drag force and static weight only. A side load due to lift on the vertical fairing caused by a deviation of the tunnel airflow has been considered.

A drag coef. $C_D = 1.0$ has been taken for the horizontal tube. Aerodynamic characteristics for the vertical fairing at an angle of incidence $\alpha = 5^\circ$ have been estimated by comparison with other thick airfoils.

The loads on the fairings are taken by the balance strut fairings, the main strut fairings taking vertical and horizontal loads and the rear strut fairing taking vertical load only.

The part of fairing tube between tunnel wall and balance struts are considered as simply supported beams their loading dividing between the 2 supports.

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

11

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED 56

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-4 FAIRING LOADS4-4-2 LOADS DUE TO AERODYNAMIC FORCES

For a Circular Cylinder, the drag coef. $C_D \approx 1.0$

Thus, for a 10" tube, the drag per running foot is

$$D = C_D S q = 1.0 \times .833 q = .833 q$$

Hence: at the max speed of the tunnel: ($q = 30 \text{ PSF}$)

$$D = 30 \times .833 = 25 \frac{\text{lb}}{\text{ft}}$$

and at the reduced speed: ($q = 18 \text{ PSF}$)

$$D = 18 \times .833 = 15 \frac{\text{lb}}{\text{ft}}$$

Length of tube between balance struts: 80"

Length of tube outside balance struts: $230 - 80 = 150"$

Thus, on balance strut fairings, the load is:

$$\begin{aligned} \text{at } 30q: \quad 25 \left[\frac{80}{2 \times 12} + \frac{150}{4 \times 12} \right] &= 25 (3.33 + 3.13) = \\ &= 25 \times 6.46 = \underline{164 \frac{\text{lb}}{\text{ft}}} \rightarrow \end{aligned}$$

and load on tunnel walls.

$$25 \frac{150}{4 \times 12} = 25 \times 3.13 = \underline{78.2 \frac{\text{lb}}{\text{ft}}} \rightarrow$$

$$\begin{aligned} \text{at } 18q: \quad \text{on strut fairings: } 15 \times 6.46 &= \underline{97 \frac{\text{lb}}{\text{ft}}} \rightarrow \\ \text{on tunnel wall: } 15 \times 3.13 &= \underline{46.9 \frac{\text{lb}}{\text{ft}}} \rightarrow \end{aligned}$$

Drag on vertical fairing

The drag coef for the streamlined shape will be taken at:

$$C_D = .20$$

$$\text{Frontal area } \frac{42 \times 11}{144} = 3.2 \text{ ft}^2$$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

F. J. G. G.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

H-H FAIRING LOADS.

4-4-2 LOADS DUE TO AERODYNAMIC FORCES

Frags on vertical pairing: cont'd.

Drag force $.20 \times 3.2 \times q = .64 q.$

High speed case. $q = 30$ PSF. $D = .64 \times 30 = 19.20$ ft.
Low speed case. $q = 18$ PSF. $D = .64 \times 18 = 11.50$ ft.

low speed case. $q_1 = 18 \text{ PSF}$. $D = .64 \times 18 = 11.50 \text{ lb}$

Load on stunt fairings:

9 = 20 PIF.

$$\frac{19.20}{2} = \underline{\underline{9.60^{16}}}$$

9-18 PSF.

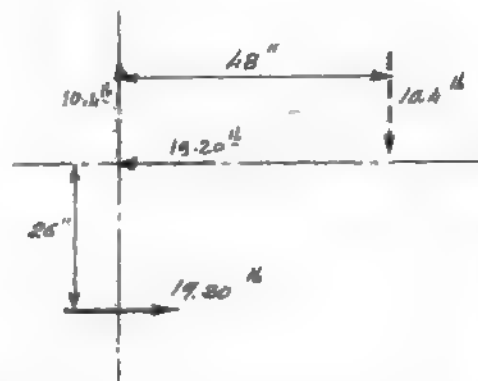
$$\frac{11.50}{2} = \underline{\underline{5.75}}^{\text{16}}$$

REACTION ON INCIDENCE STRUT FAIRING.

$\alpha = 0^\circ$

$$(30 \text{ g}) \quad 19.20 \frac{\text{g}}{\text{L}} = 10.4 \frac{\text{L}}{\text{L}}$$

$$(175) \quad 11.50 \cdot \frac{48}{26} = 6.22$$



$\alpha = 45^\circ$

At this angle the airload on the fairing will be approximately balanced by that on the crown fairing. Hence the reaction will be small and can be neglected.

$$\alpha = 20^\circ$$

Since the reaction at $\alpha = 0^\circ$ is only 10^{16} It will be conservative to assume the same value for $\alpha = 20^\circ$.

DECLASSIFIED

WRITTEN BY

G. Jacquemin

CHECKED BY

1972-1973

DATE _____

Sept: 1957

ISSUE

AIRCRAFT

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-4FAIRING LOADS4-4-2LOADS DUE TO AERODYNAMIC FORCES.SUMMARY OF LOADS ON STRUTS FAIRINGS & TUNNEL WALLS.HORIZONTAL LOADS:

ON MAIN STRUTS FAIRINGS:

$$q = 30 \text{ PSF} : 164 + 9.60 = \underline{173.6}^{\text{lb}}$$

$$q = 18 \text{ PSF} : 97 + 5.75 = \underline{102.75}^{\text{lb}}$$

ON TUNNEL WALL:

$$q = 30 \text{ PSF} : \underline{78.2}^{\text{lb}}$$

$$q = 18 \text{ PSF} : \underline{46.9}^{\text{lb}}$$

VERTICAL LOADS:

$$q = \begin{cases} \text{ON MAIN STRUTS : } \underline{5.2}^{\text{lb}} \\ 30 \text{ PSF} \left\{ \begin{array}{l} \text{ON REAR STRUT : } \underline{10.4}^{\text{lb}} \uparrow \end{array} \right. \end{cases}$$

direction of applied load.

$$q = \begin{cases} \text{ON MAIN STRUTS : } 3.11^{\text{lb}} \downarrow \\ 18 \text{ PSF} \left\{ \begin{array}{l} \text{ON REAR STRUT : } 6.22^{\text{lb}} \downarrow \end{array} \right. \end{cases}$$

" "

DECLASSIFIED

WRITTEN BY

G. Jacquemont

CHECKED BY

H. T. ...

DATE

Sept. 1957

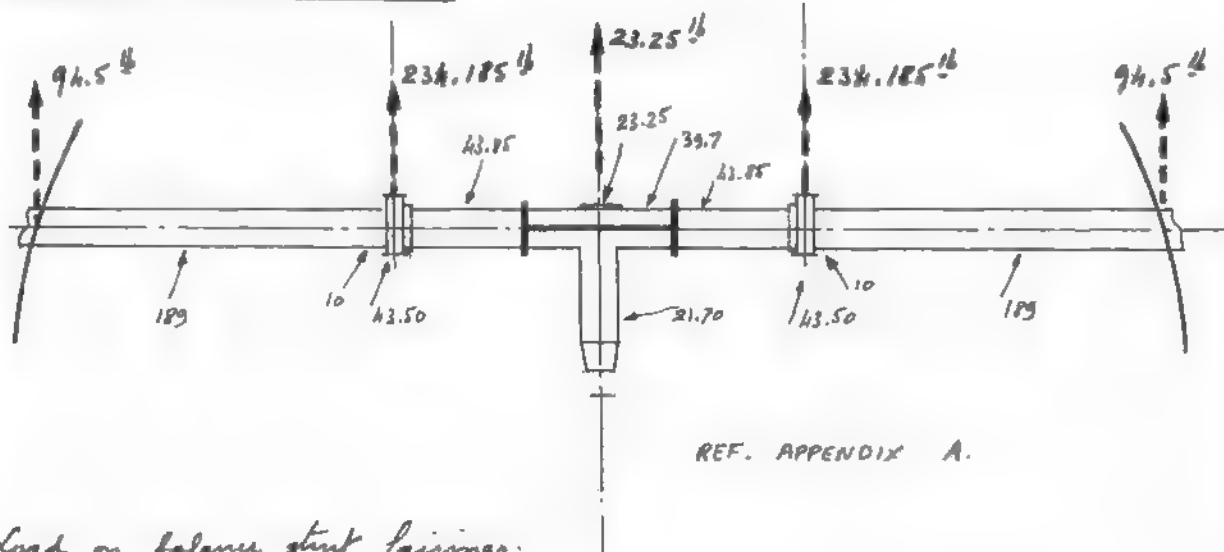
ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

59

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -4-4 FAIRING LOADS4-4-3 LOADS DUE TO STATIC WEIGHTSFAIRINGS - TOTAL WEIGHT.

Load on balance strut fairings:

$$43.50 + 10 + \frac{189}{2} + 43.85 + \frac{23.25}{2} + \frac{39.7}{2} + \frac{21.70}{2} = 234.185 \text{ lb}$$

Load on tunnel wall attachment:

$$\frac{189}{2} = 94.5 \text{ lb}$$

TOTAL WEIGHT OF FAIRINGS.

$$(189 \times 2) + (10 \times 2) + (43.5 \times 2) + (43.85 \times 2) + (23.25 \times 2) + 39.7 + 21.70 =$$

$$378 + 20 + 87 + 87.60 + 46.50 + 39.7 + 21.70 = \underline{\underline{680.50 \text{ lb}}}$$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

/ /

DATE

Sept. 1957

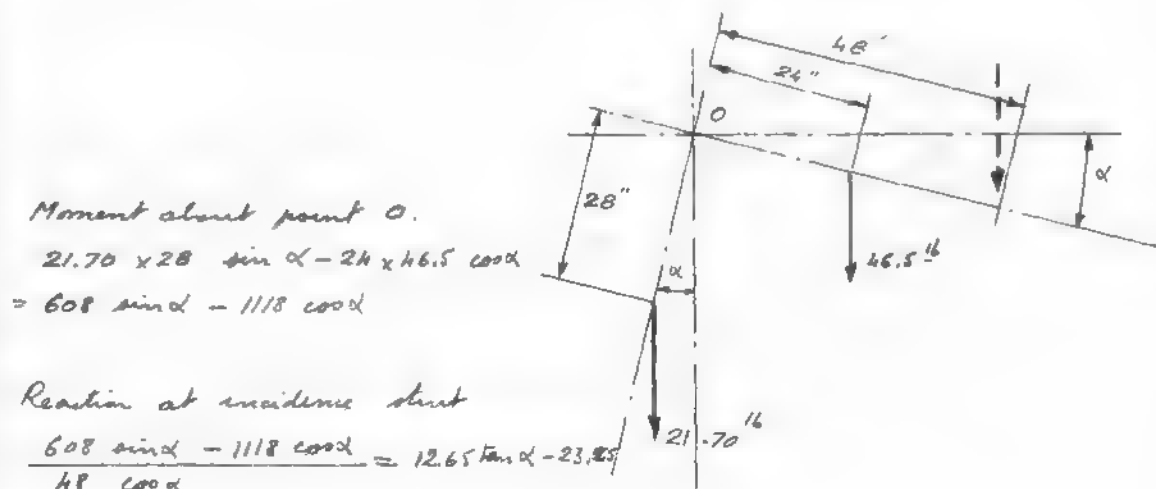
ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.H-4 FAIRING LOADSH-4-3 LOADS DUE TO STATIC WEIGHT & REACTIONSREACTION ON INCIDENCE STRUT FAIRING FOR ANGLES $\alpha \neq 0$ 

$$\alpha = -10^\circ$$

Reaction at incidence strut

$$12.65 \tan(-10^\circ) - 23.25 =$$

$$= -2.23 - 23.25 = -25.48 \text{ lb}$$

Reactions at main struts

$$-234.20 + \frac{2.23}{2} = -233.10 \text{ lb}$$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

112 + 12

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELH-4 FAIRING LOADSH-4-3 LOADS DUE TO STATIC WEIGHT & REACTIONSREACTION ON INCIDENCE STRUT FAIRING FOR ANGLES $\alpha \neq 0$ - CONT'D.

$\alpha = 20^\circ$

Reaction at incidence strut

$12.65 \tan 20^\circ = 23.25 =$

$= -23.25 + 4.6 = -18.65 \text{ lb}$

Reactions at main struts

$-234.20 - \frac{4.6}{2} = -236.50 \text{ lb}$

$\alpha = 45^\circ$

Reaction at incidence strut.

$12.65 \tan 45^\circ = 23.25 =$

$= -23.25 + 12.65 = -10.60 \text{ lb}$

Reactions at main struts

$-234.20 - \frac{12.65}{2} = -240.50 \text{ lb}$

SUMMARY OF STATIC LOADS ON STRUT FAIRINGS & TUNNEL WALLS.

α°	MAIN STRUT FAIRING	INCIDENCE STRUT FAIRING	TUNNEL WALL
-10	233.10	25.5	94.5
0	234.20	23.2	94.5
20	236.50	18.6	94.5
45	240.5	10.2	94.5

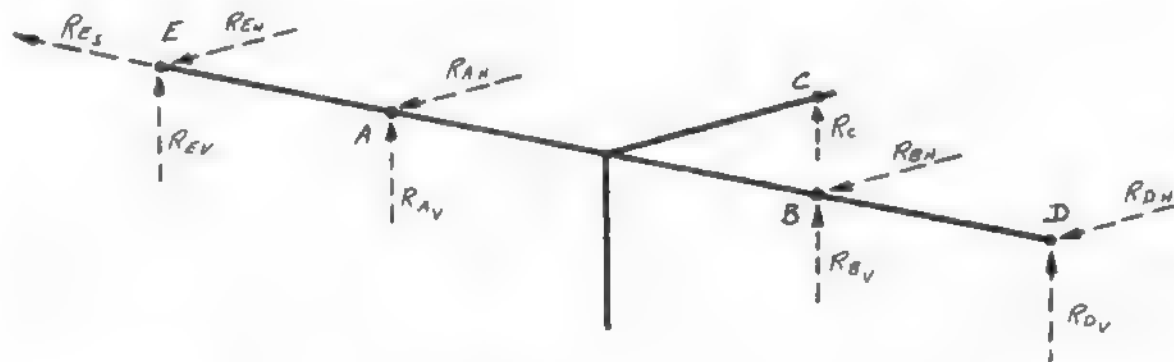
ALL LOADS IN lb

+VE LOADS ARE PULL ON FAIRINGS OR DOWN LOADS ON TUNNEL WALL.

WRITTEN BY G. Jacquemin	CHECKED 15	DECLASSIFIED Sept. 1957	ISSUE	AIRCRAFT
----------------------------	---------------	----------------------------	-------	----------

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-4 FAIRING LOADS4-4-4 NET LOADS & REACTIONS -

REACTIONS α	-10°	0°	20°	45° 189.
R_{AV}	238.3	239.4	241.7	243.6
R_{BV}	238.3	239.4	241.7	243.6
R_{AH}	173.6	173.6	173.6	102.7
R_{BH}	173.6	173.6	173.6	102.7
R_C	15.1	12.8	8.2	4.38
R_{DV}	94.5	94.5	94.5	94.5
R_{EV}	94.5	94.5	94.5	94.5
R_{DH}	78.2	78.2	78.2	46.9
R_{EH}	78.2	78.2	78.2	46.9
R_{ES}^* OPERATING	0	1211.0	0	0
R_{ES}^* PRESSURE	1372.0	1372.0	1372.0	1372.0

* . REF. - 4-3-5

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	W. H. H. H.	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.5-0MODEL STRESS ANALYSIS.5-1-1LOADING CONSIDERATIONS.

The aerodynamic loads developed in section 4 have been used together with pressure in the supply tubes, only to check the strength of the attachment of the model to its supporting structure (see sections 6 & 7)

Due to the robust nature of the model structure, stresses induced in the model by these external loads will be low and can be neglected. The validity of this statement is illustrated by the pessimistic assessment of the loads in the wing attachment bolts (section 5-2-1)

The highest stresses will be those due to the pressure differential between the interior and outside of the model.

DECLASSIFIED

WRITTEN BY

G. Jacquemin

CHECKED BY

G. Jacquemin

DATE

Sept. 1957

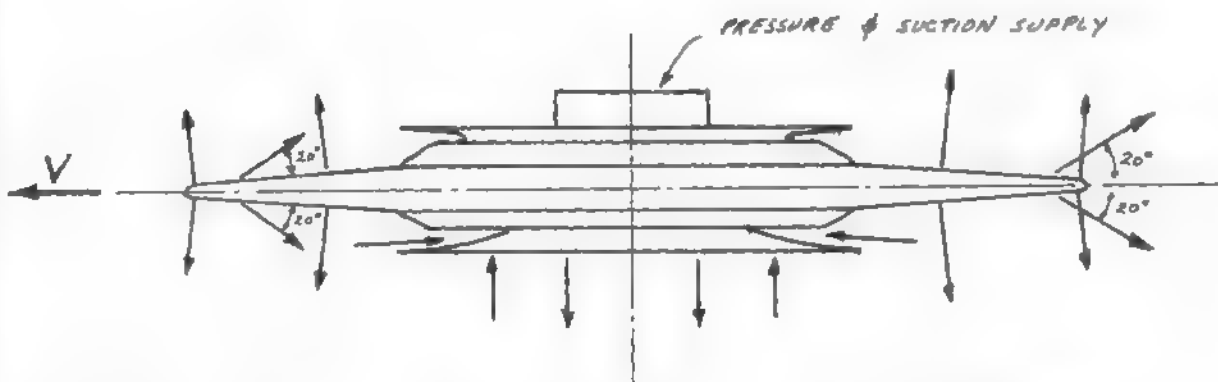
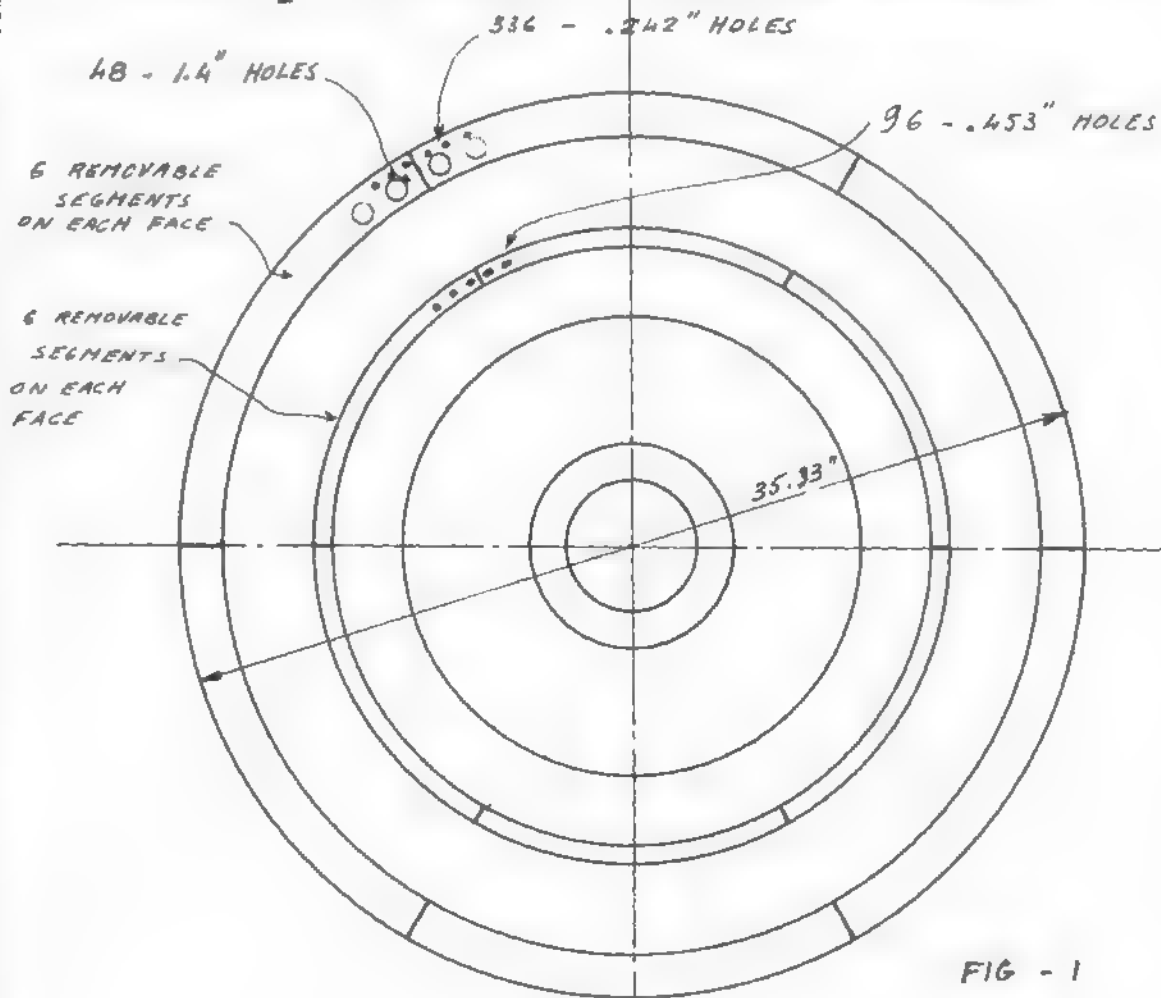
ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED 64

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-O - FIG-8 - $\frac{1}{12}$ SCALE MODEL - SCHEMATIC DIAGRAMTUNNEL SPEED : $V = 158.8 \frac{\text{ft}}{\text{sec}}$ $q = 30 \text{ PSF.}$

WRITTEN BY

G. Jacques

CHECKED

10.7.1957

DECLASSIFIED

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

65

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-1-2 DIFFERENTIAL PRESSURE ON THE WING UPPER SURFACE.

MAX. internal pressure in the wing: 30.74 PSIA

Assume the A/C is at 45° incidence and a pressure distribution giving an average value of $C_p = -5$ on the front part of the wing.

Assume also that the mean value of C_p over the first 3" after L.E. is $C_p = -10$.

Hence: the local pressures: $\Delta P = C_p q$

$$\Delta P_{AVE} = -5 \times 30 = -150 \text{ PSF} = -1.04 \text{ PSI}$$

$$\Delta P_{TIP} = -10 \times 30 = -300 \text{ PSF} = -2.08 \text{ PSI}$$

Hence total external pressure: $P_{AVE} = 14.7 - 1.04 = 13.66 \text{ PSI}$

$$P_{TIP} = 14.7 - 2.08 = 12.62 \text{ PSI}$$

Differential pressure taken by the wing structure:

$$\Delta P_{AVE} = 30.74 - 13.66 = 17.08 \text{ PSI}$$

$$\Delta P_{TIP} = 30.74 - 12.62 = 18.12 \text{ PSI}$$

A General stressing of the wing will be carried out using 17.10 PSI and a local stressing near the leading edge using 18.20 PSI.

With a load factor of 4, these pressures become

$$17.1 \times 4 = \boxed{68.4 \text{ PSI}}$$

$$18.2 \times 4 = \boxed{72.8 \text{ PSI}}$$

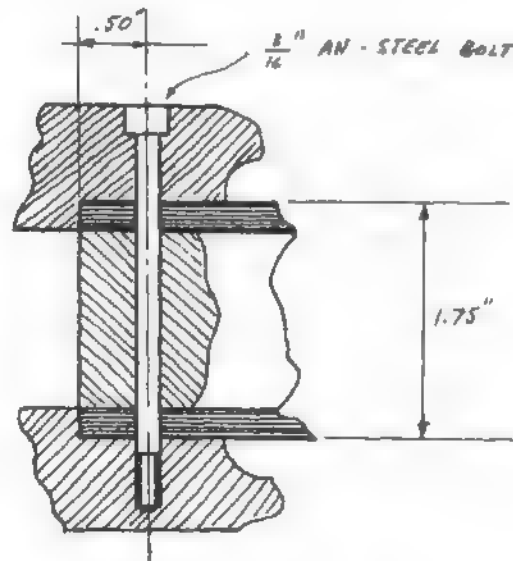
DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	Dr. /	Sept. 1957		

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-2-1 WING ATTACHMENT BOLTS

As a covering stringing,
the bolt is assumed to take
in shear the moment calculated
from the diagram below under
an arbitrary pressure of 5 PSI
At the same time, it will be
considered under the tension due
to internal pressure of 68.4 PSI
on an area of 10 in^2



Hence: tension in the bolt.

$$68.4 \times 10 = 684.0 \text{ lb}$$

Area of the wing segment
 $(2.04 + 4.6) \frac{9.8}{2} = 32.5 \text{ in}^2$

Moment about the bolt
 $4 \times 32.5 \times 5 \times 5.1 = 3308 \text{ in} \cdot \text{lb}$

Shear on the bolt. $\frac{3308}{1.75} = 1890.0 \text{ lb}$

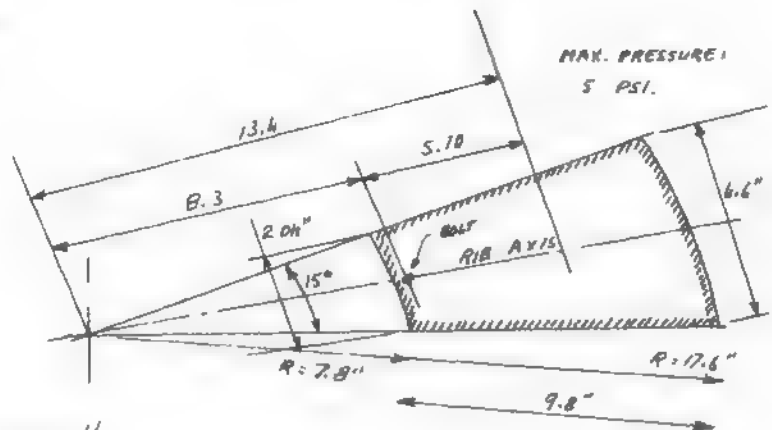
Strength of the $\frac{3}{16}$ " bolt as per AN-C-5: Tension: 2160 lb

shear: 2070 lb

Combined loading: allowable tension: $Y = \sqrt{b^2 \left(1 - \frac{x^2}{a^2}\right)} = b \sqrt{1 - \frac{x^2}{a^2}}$

$$Y = 2160 \sqrt{1 - \left(\frac{1890}{2070}\right)^2} = 2160 \times \sqrt{1 - .835} = 2160 \times .406 = 875 \text{ lb}$$

M.S. $\frac{875}{684.0} - 1 =$



WRITTEN BY

G. Yacopini

CHECKED BY

L. T. J. J. J.

DATE

Sept. 1957

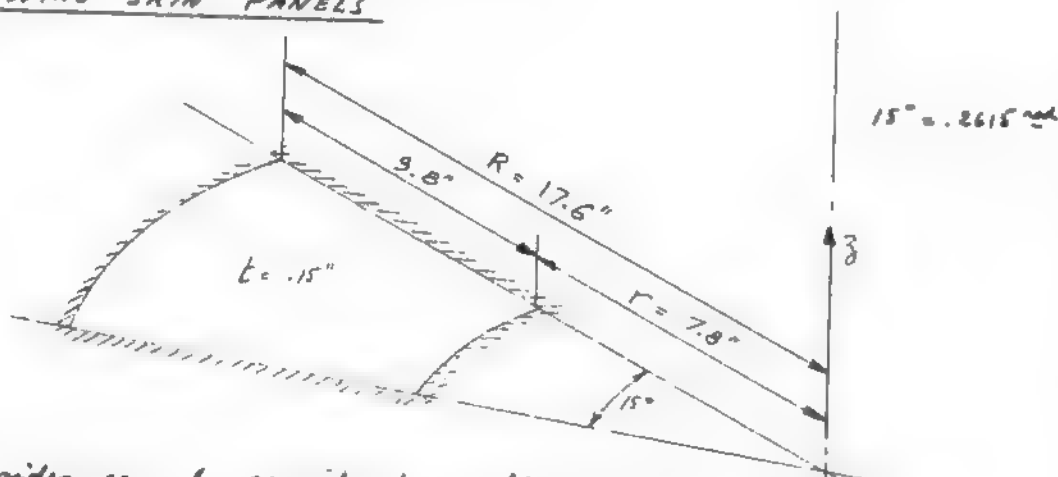
ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

67

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-2-2 WING SKIN PANELS

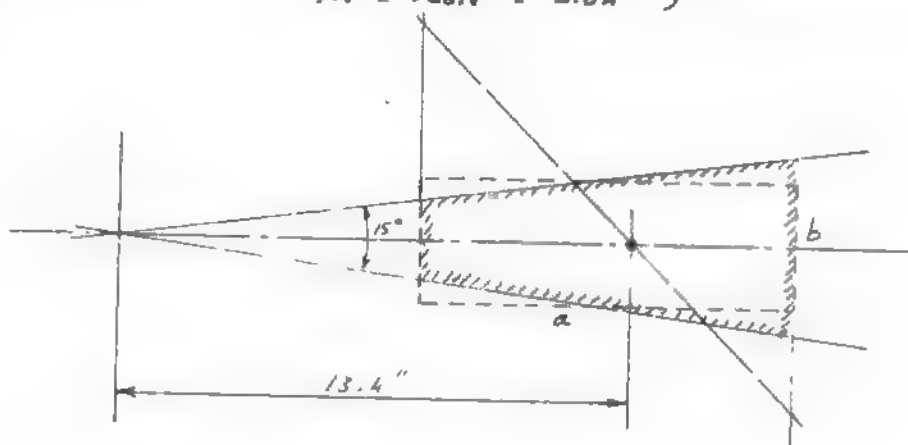
Assume:

- 1 - all sides can be considered as fixed against rotation
- 2 - all sides can be assumed held against deflection in z direction.

Area of panel: $\pi \frac{15}{360} (17.6^2 - 7.8^2) = \frac{\pi}{24} (310 - 61) = 32.5 \text{ in}^2$

Max pressure force on panel: $32.5 \times 17.10 = 556 \text{ lb}$

Length of arc: $\left. \begin{array}{l} 17.6 \times .2615 = 4.6'' \\ 7.8 \times .2615 = 2.04'' \end{array} \right\} \text{mean length: } 3.32''$



DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

68

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.5-0 MODEL STRESS ANALYSIS5-2-2 WING SKIN PANELS

Consider the rectangular plate shown in dotted line.

This plate is relatively thick and will take the load in bending rather than as a membrane.

we have: $b = 3.32"$ $a = 9.80"$ $\frac{b}{a} = .339$

Ref Resistance des matériaux appliquée à l'aviation by Paul Vallat.

Max. bending stress in the plate. $f_{b_n} = A p \left(\frac{b}{t} \right)^2$

Max. deflection at the center $\delta_H = C \frac{p b}{E (1-\nu^2)} \left(\frac{b}{t} \right)^3$

Ref. A from curve (2) Diagram 32-1 - $A = .50$

Ref C " " (4) " " - $C = .212$

Then: $f_{b_n} = .50 \times 17.10 \left(\frac{3.32}{.15} \right)^2 = 4190 \text{ PSI}$ @ 55000 PSI

$$\delta_H = .212 \times \frac{17.10 \times 3.32}{30 \times 10^6 (1.069)} \left(\frac{3.32}{.15} \right)^3 = .000209"$$

Fully factored bending stress: $4 \times 4190 = 16780 \text{ PSI}$

M.S. $\frac{55000}{16780} - 1 = \underline{\hspace{2cm}}$ 2.28

WRITTEN BY

G. Jacquemin

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

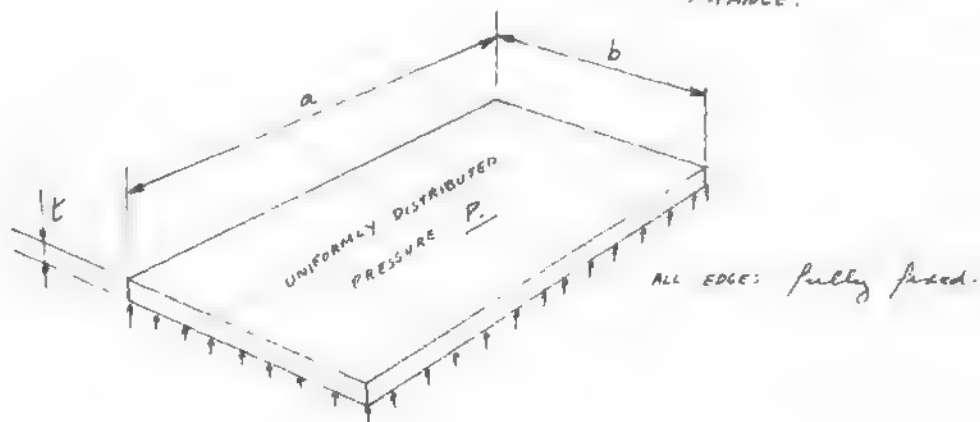
~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.FLAT PLATES UNDER TRANSVERSE LOADING.

The following is translated from "RESISTANCE DES MATERIAUX
APPLIQUEE A L'AVIATION" BY PAUL VALLAT

1ST. EDITION - 1944 - PUBLISHED BY: MENARD - EDITIONS

8 RUE DES REGANS - TOULOUSE
FRANCE.



* MAX. BENDING STRESS AT THE EDGES OF THE PLATE

$$f_{bm} = A P \left(\frac{b}{t} \right)^2$$

MAX. DEFLECTION AT THE CENTER OF THE PLATE

$$f_m = C \frac{P b}{E(1-\sigma^2)} \left(\frac{b}{t} \right)^3$$

WHERE

E = Young's modulus.

σ = Poisson's ratio

A = coef obtained from curve next page

C = coef obtained from curve next page

$a, b \& t$ = dimensions of the plate as shown above

P = applied uniformly distributed pressure

*: or For simply supported edges - max. bending stress at the center of the plate

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemont		Sept 1957		

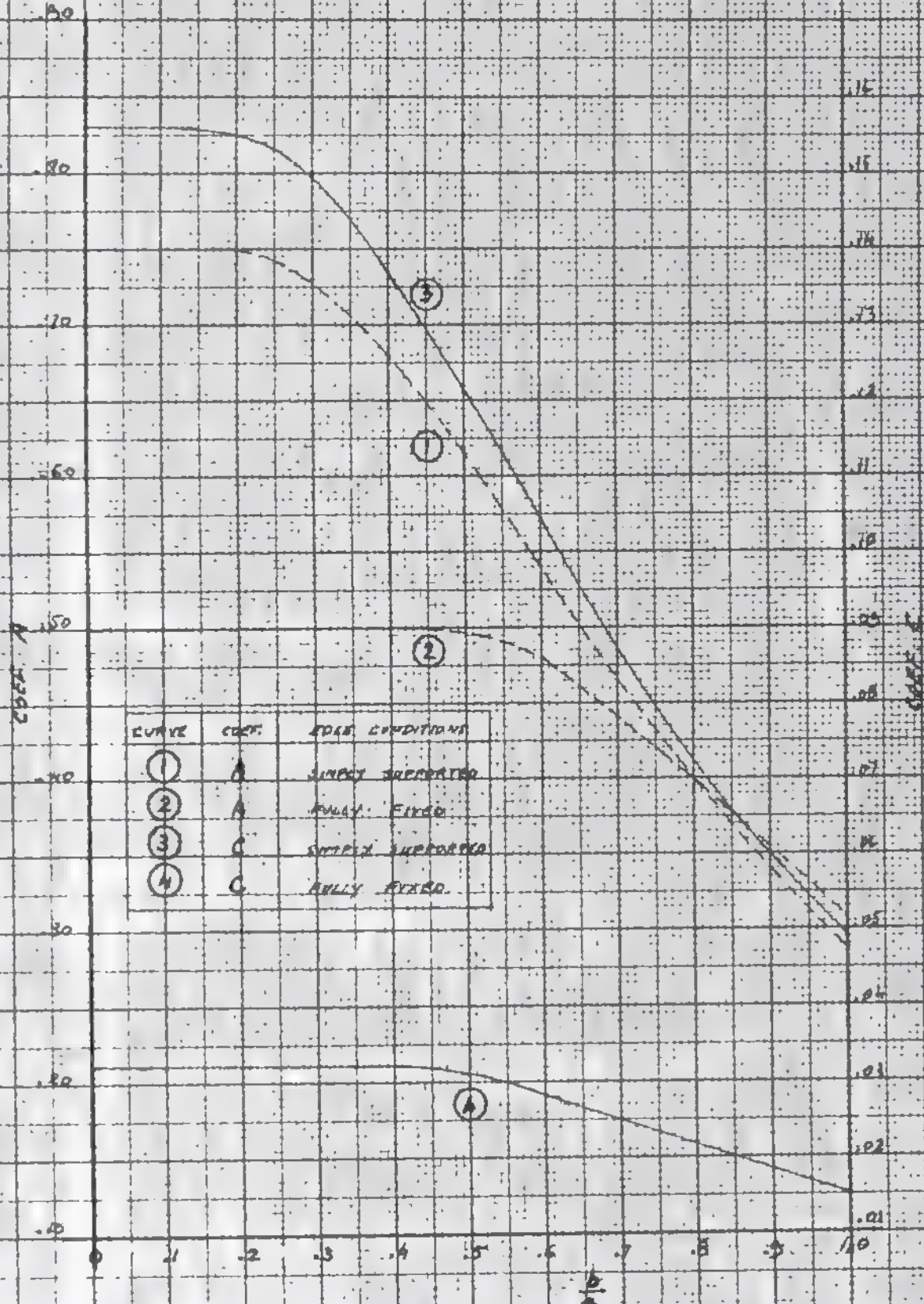
UNCLASSIFIED

AVRO/SPG/TR-112

STRESS ANALYSIS OF IS SCALE HYPERBOLIC TRANSITION THEORY

REF. RESISTANCE DES MATERIAUX APPLIQUEES A LA VIBRATION

BY P. VALLAT



UNCLASSIFIED

Sept. 1957

10 X 10 TO LINE 12 INCH
G-15

~~SECRET~~

DECLASSIFIED

71

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-2-2 WING SKIN PANELSATTACHMENT SCREWS.

The skin is held on the ribs by 8 screws
AN-510 #4 or #5.

Screw strength in tension as per specifications

#5 396 lb

#4 313 lb

Load per screw with a max pressure force of 556 lb per panel at a pressure of 17.10 PSI (unfactored)

$$\frac{556}{8} = 69.5 \text{ lb unfactored}$$

Fully factored load per screw $69.5 \times 4 = 278 \text{ lb}$

Considering now a screw at the outer end of the rib and using the higher pressure 18.2 PSI

Fully factored load per screw

$$278 \frac{18.2}{17.1} = 296 \text{ lb (average load)}$$

Considering the drawing, it can be seen that the outer screw will take approximately the pressure on a strip 4" long and 1.3" wide; hence a load: at 72.8 PSI (fully factored)

$$72.8 \times 4 \times 1.3 = \underline{379 \text{ lb}}$$

∴ #5 screws are required

M.S.

$$\frac{396}{379} - 1 =$$

*
068

* NOTE. This Margin of Safety is pessimistic as no account has been taken of the effect of the edge attachment.

WRITTEN BY

G. Jacques

CHECKED BY

M. T. ...

DECLASSIFIED

Sept. 1957

AIRCRAFT

~~SECRET~~

~~SECRET~~

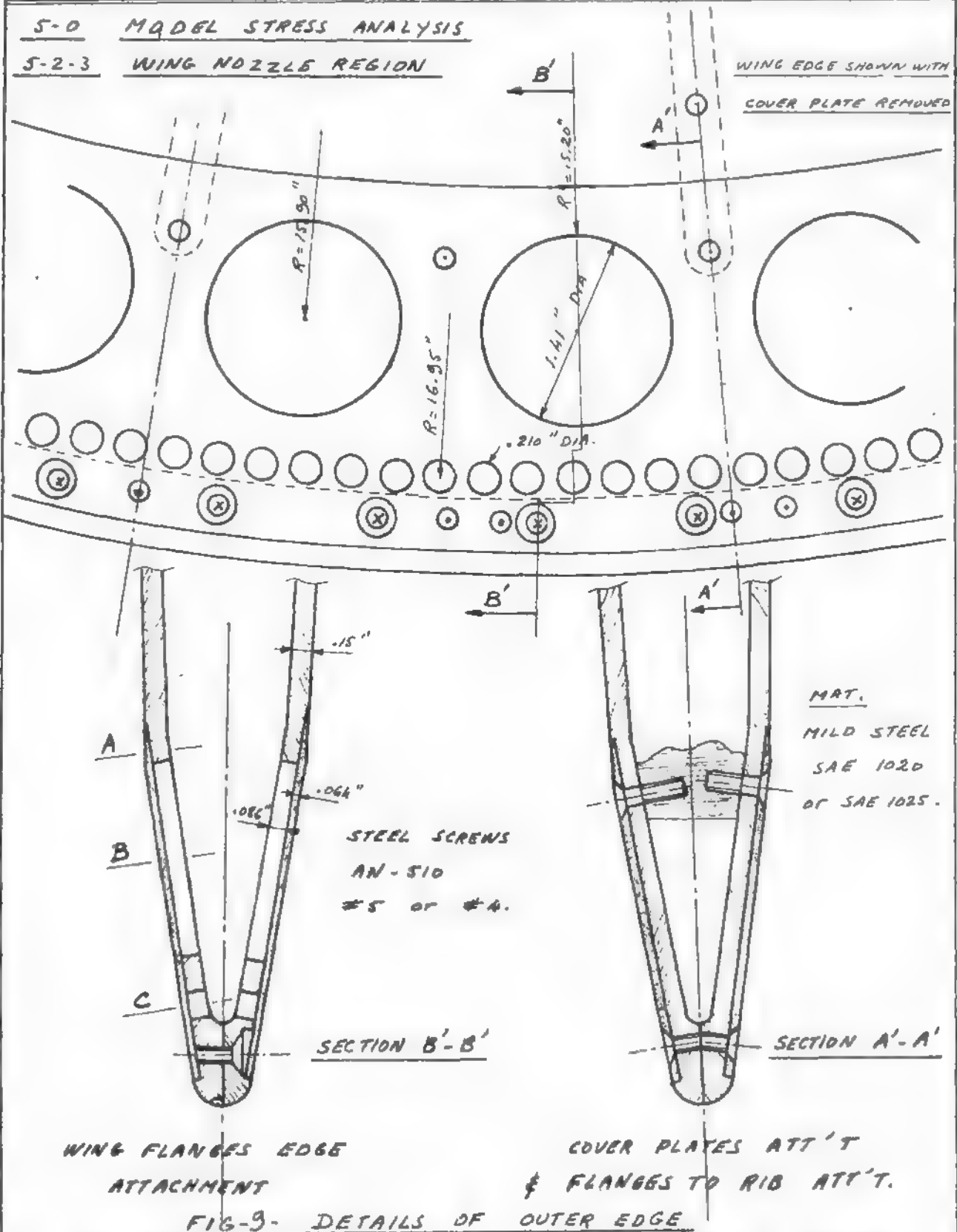
DECLASSIFIED

72

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL-

5-0 MODEL STRESS ANALYSIS

5-2-3 WING NOZZLE REGION



WRITTEN BY

G. Jacquin

CHECKED BY

M. J. ...

DATE

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

73

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL -5-0 - MODEL STRESS ANALYSIS5-2-3 - WING NOZZLE REGIONASSUMPTIONS FOR STRESSING THE EDGE.

- 1 - The differential pressure will be taken at 17.20 PSI as calculated previously
- 2 - The edge will be first treated as a rectangular plate .086" thick with all four sides fixed. Size: $a \times b = 4.6" \times 2.0"$
then $\frac{b}{a} = .435$

This assumption can be made since it was found that the deflection at the center of the .15" thick plate would be of the order of .0002" hence negligible. (page: 68)

- 3 - The max. stress in bending found from plate theory will be assumed to be constant over the plate for the purpose of stressing the 3 sections A, B & C indicated on the sketch, but will be factored up due to the local reduction in section.
- 4 - Section A will be considered .086" thick
Section B will be considered as two plates: .086" + .064" working together independently
Section C will be considered .086" thick

Note: The .064" plate has to be assumed ineffective near its edges due to insufficient attachment. It is assumed however that enough load can be picked up by the plate to make it effective between the 1.41" holes at section B

BENDING STRESS IN THE PLATE AS PER ASSUMPTIONS ① & ②

$$f_b = Ap \left(\frac{b}{t} \right)^2 = .49 \times 17.20 \left(\frac{2.0}{.086} \right)^2 = 4830 \text{ PSI}$$

$$A = .49 \quad (\text{Curve ②})$$

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	17.1.1.1.1.1	Sept. 1957		

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

74

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-2-3 WING NOZZLE REGIONSTRESSING OF THE EDGE.SECTION B.Basic section in bending will be assumed to be a 15° arc of radius $15.90''$ i.e.: $4.16''$ long, having a section modulus

$$\frac{4.16}{6} \cdot .086^2 = .00512 \text{ in}^3$$

The actual section is made of $(1.34'' \times .086'') + (1.34'' \times .064'')$
 having a section modulus $\frac{1.34}{6} (.086^2 + .064^2) = .00257 \text{ in}^3$

Hence, the bending stress:

$$4830 \frac{.00512}{.00257} = 9640 \text{ PSI} \quad @ 55000$$

fully factored: $9640 \times 4 = 38600 \text{ PSI}$ M.S. = $\frac{55000}{38600} - 1 = .425$

SECTION C -Basic section in bending will be assumed to be a 15° arc of radius $16.95''$ i.e.: $4.43''$ long, having a section modulus

$$\frac{4.43}{6} \cdot .086^2 = .00545 \text{ in}^3$$

The actual section has only $1.49'' \times .086''$
 having a section modulus $\frac{1.49}{6} \cdot .086^2 = .001832 \text{ in}^3$

Hence, the bending stress:

$$4830 \frac{.00545}{.001832} = 14400 \text{ PSI} \quad @ 55000$$

fully factored: $14400 \times 4 = 57600 \text{ PSI}$

M.S. = $\frac{55000}{57600} - 1 = .04$

ACTUAL MARGIN OF SAFETY ON
 APPLIED LOAD

3.95.

WRITTEN BY

G. Jacques

CHECKED BY

K. P. P.

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-2-4 WING EDGE ATTACHMENT.STRESSING OF THE EDGE.ATTACHMENT SCREWS.

Strength in tension of #5-44 & #4-48 - AN-510 SCREWS per turn of thread

Screw strength in tension as given by AN-510 - Specs

#5 - 396 ^{lb}

for fully engaged threads.

#4 - 313 ^{lb}

This strength is based on threads engaged in a standard nut. Min height of nut and nb of turns of thread

#5-44 : $h = .102" - .114"$ $n = 4.48$

#4-48 : $h = .087" - .098"$ $n = 4.17$

Strength per turn of thread

#5-44 : $\frac{396}{4.48} = 88.4 ^{lb}$

#4-48 : $\frac{313}{4.17} = 75.0 ^{lb}$

SCREWS ATTACHING WING FLANGES AT THE EDGE

- Length of thread engaged $\approx .15" > .102"$ hence full strength available
- Each screw can be considered as taking a maximum load equal to the pressure over 2 in² : $18.2 \times 2 = 36.4 ^{lb}$

if 11 #4 screws are used : M.S : $\frac{313}{4 \times 36.4} - 1 = \frac{1.15}{1.72}$

" " 5 " " " : M.S : $\frac{396}{4 \times 36.4} - 1 = \frac{1.72}{1.15}$

SCREWS ATTACHING THE COVER PLATES.

- Length of thread engaged : .086" i.e. : nb of thread engaged :

#5 : 3.78 available strength : $88.4 \times 3.78 = 334 ^{lb}$

#4 : 4.13 " " : $75 \times 4.13 = 310 ^{lb}$

- Assuming again 2 in² pressure as a max load : 36.4 ^{lb} per screw.

WRITTEN BY

G. Jacques

CHECKED BY

J. T. J. J. J.

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

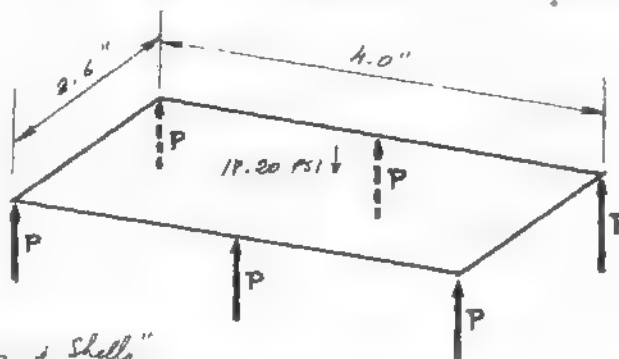
76

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-2-5 - WING .064" COVER PLATESATTACHMENT SCREWS CONT'D.SCREWS ATTACHING THE COVER PLATES - CONT'D

if #34 screws are used:	M.S.	$\frac{310}{4 \times 36.4} - 1 =$	1.1.
" " " " :	M.S.	$\frac{334}{4 \times 36.4} - 1 =$	1.2

.064 COVER PLATE.

This plate will be covered for the case where it is used to blank the 2 sets of holes. Due to splines every other ribs; it must be considered as a plate under uniform loading supported at 6 points. The max pressure of 18.2 PSI will be considered over the plate.



Using Timoshenko "Plates & Shells"

page 243

$$\text{Ratio } \frac{b}{a} = \frac{2.6}{2} = 1.3 \quad \text{hence } \alpha = .0423$$

$$\beta = .0210$$

$$\beta_1 = .0385$$

Deflection at center of plate

$$w = \alpha \frac{q b^4}{E h^3} = .0423 \frac{18.2 \times 2.6^4}{30 \times 10^6 \times .064^3} = .00446''$$

$$M_x = \beta q b^2 = .0210 \times 18.2 \times 2.6^2 = 2.585 \text{ in-lb}$$

$$M_y = \beta_1 q b^2 = .0385 \times 18.2 \times 2.6^2 = 4.730 \text{ in-lb}$$

$$\sqrt{M_x^2 + M_y^2} = \sqrt{2.585^2 + 4.73^2} = 5.32 \text{ in-lb}$$

DECLASSIFIED

WRITTEN BY

G. Jacquemont

CHECKED BY

E. J. 1957

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

77

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-2-5 WING .064" COVER PLATE.064 COVER PLATE - CONT'D.

Section modulus of .064" x 1.00" of plate:

$$\frac{1 \times .064^2}{6} = .000684 \text{ in}^3$$

Max Bending stress in the plate: $\frac{5.32}{.000684} = 7800 \text{ PSI} @ 55000$ fully factored: $7800 \times 1.4 = 31200 \text{ PSI}$

H.S.

$$\frac{55000}{31200} - 1 =$$

.765

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

J. T. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

AVRO/SPG/TR 112

78

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -5-0 MODEL STRESS ANALYSIS5-2-6 WING - MAX. PRESSURE PERMISSIBLE-PRESSURE REQUIRED TO PRODUCE STRUCTURAL FAILURE OF THE WING.

The weakest point of the wing is section C of the edge with a margin of safety : $-.048$ and a load factor $n = 4$.

$$\text{Hence, the failing pressure } 4 \times 18.20 \times (1 - .048) = \underline{\underline{69.4 \text{ PSI}}}$$

$$\text{Pressure at yield of the material : } 69.4 \frac{36}{55} = \underline{\underline{45.3 \text{ PSI}}}$$

PRESSURE REQUIRED TO PRODUCE FAILURE OF THE .064" COVER PLATE.

The minimum margin of safety on the cover plate is : $.762$

$$\text{Hence the failing pressure : } 4 \times 18.20 (1 + .762) = \underline{\underline{128 \text{ PSI}}}$$

$$\text{Pressure at yield of the material : } 128 \frac{36}{55} = \underline{\underline{83.7 \text{ PSI}}}$$

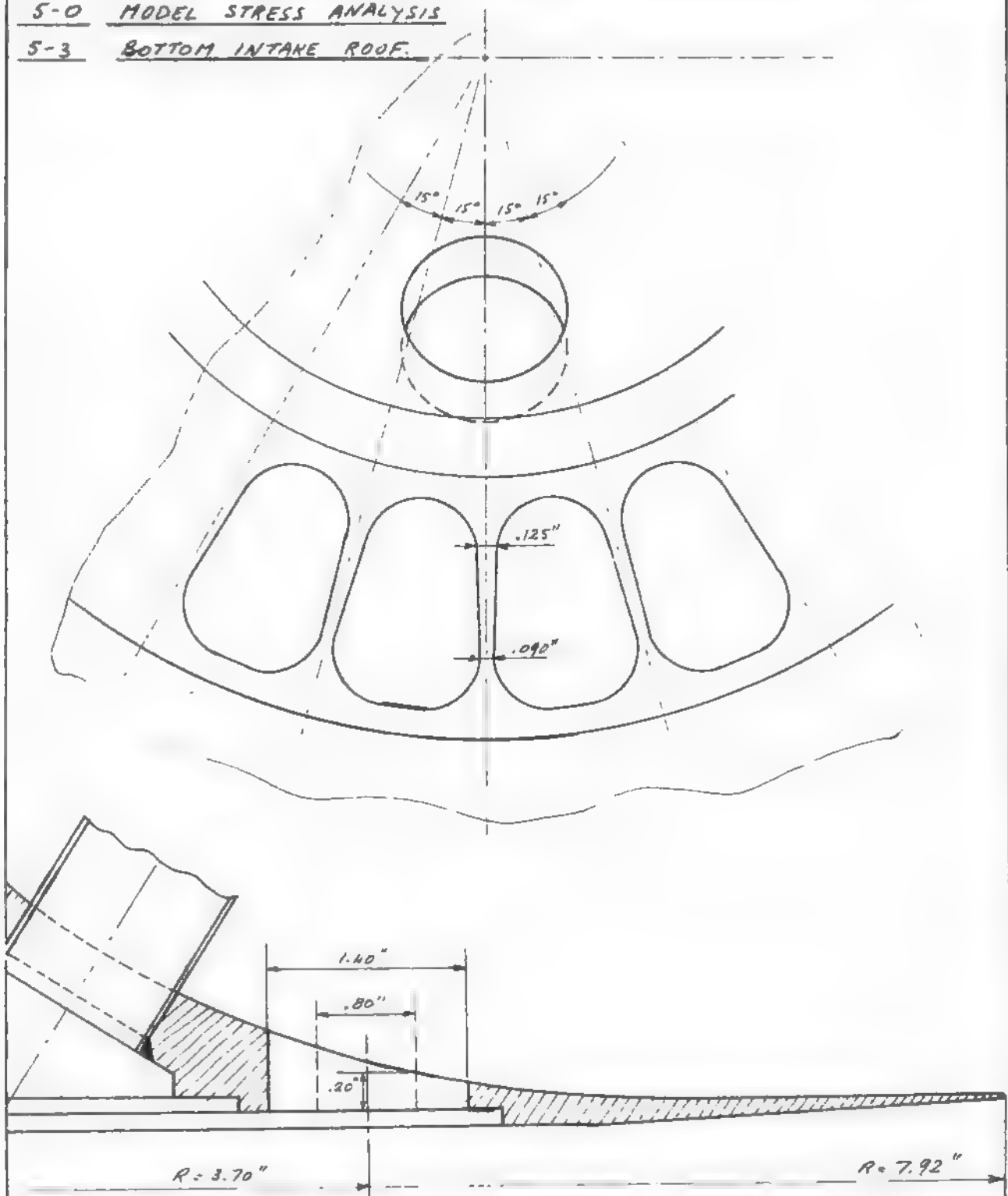
DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	15	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.5-0 MODEL STRESS ANALYSIS5-3 BOTTOM INTAKE ROOF.

MAX. DIFFERENTIAL PRESSURE : ESTIMATED : 1 PSI.

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	1:1:1:1	Sept. 1957		

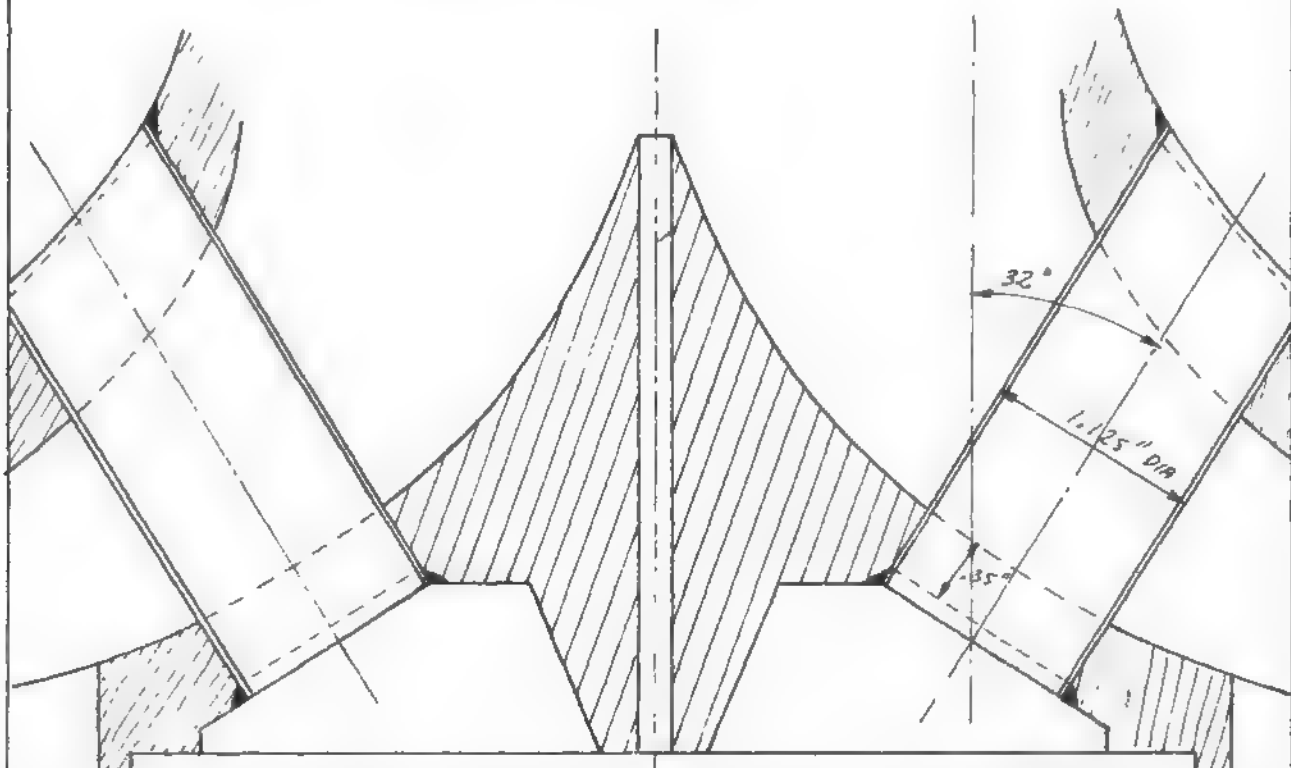
~~SECRET~~

DECLASSIFIED

~~SECRET~~

AVRO/SPG/TR 112

81

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-3 BOTTOM INTAKE ROOF5-3-2 EXHAUST TUBES ATTACHMENT.

CALIBRATION CASE

$$.44 \times 1925 = 848 \frac{1}{2} + 200 = 1048$$

The max. loads on this attachment will occur in the calibration case from section 10 under the max down load of 1925^{lb}.
 44% of this down load is taken by the rod : 1048^{lb}

Hence: load per tube fully factored : $1048 \frac{4}{5} = 698 \frac{1}{5}$

Area of solder in shear: $1.125 \times \pi \times .35 = 1.238 \text{ in}^2$

DECLASSIFIED

WRITTEN BY

J. Jacques

CHECKED BY

F. " "

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL5-0 MODEL STRESS ANALYSIS5-3 BOTTOM INTAKE ROOF5-3-2 EXHAUST TUBES ATTACHMENT.

Chiral load on each tube: $\frac{698}{\cos 32^\circ} = 824 \frac{1}{2}$

Shear stress on the solder: $\frac{824}{1.238} = 665 \text{ PSI}$

The solder used is a 95% tin - 5% lead type

Ref: AP-370 - CHAPT. 405-3 - 1B ultimate shear strength
of solder: 4000 PSI

M.S: $\frac{4000}{665} - 1 = \text{-----}$ 5.00

DECLASSIFIED

WRITTEN BY

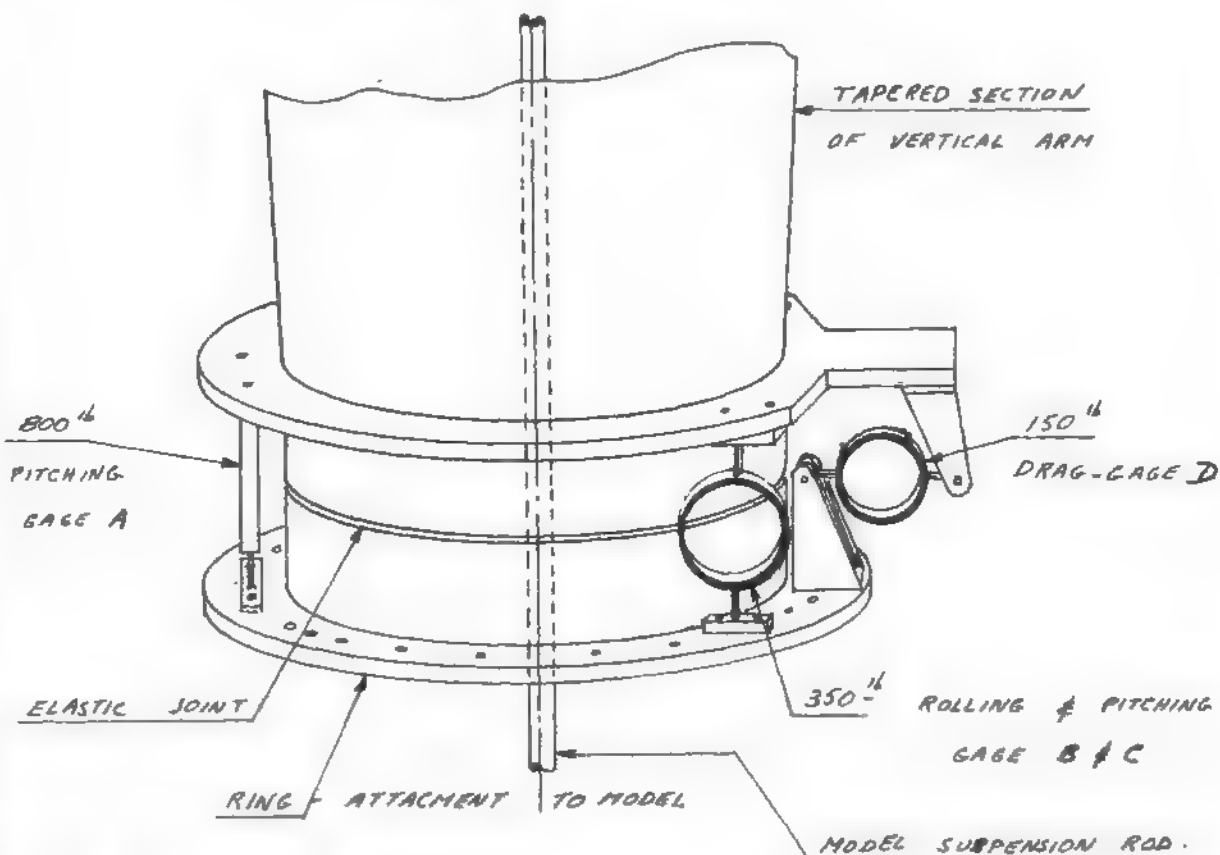
CHECKED BY

DATE

ISSUE

AIRCRAFT

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-0 LOAD GAGE DESIGN.6-1 LOAD ANALYSIS.6-1-1 LOADING CONSIDERATIONSDESCRIPTION OF GAGE SECTIONFIG-10 GAGE SECTION

The model is attached at the bottom of the vertical arm by means of a vertical steel rod and four rings load measuring gages as shown above.

The suspension rod is used to support the model in such a way that no load due to model weight is registered by the gages when the arm is vertical.

Gages A, B & C will measure both pitching moments and loads normal to the plane of the model. In addition, gages B & C

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	1 12 1957	Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -

<u>6-0</u>	<u>LOAD GAGE DESIGN</u>
<u>6-1</u>	<u>LOAD ANALYSIS</u>
<u>6-1-1</u>	<u>LOADING CONSIDERATIONS</u>

DESCRIPTION OF GAGE SECTION - CONT'D

will measure rolling moments. Gage D will measure loads parallel to the plane of the model.

No gage has been provided for measurement of side load.

LOAD PATHS THROUGH GAGE SECTION -

The loads resolved at the model center consist of three forces: Vertical, fore/aft and side and two moments: pitching and rolling. Due to symmetry around the vertical axis, no yawing moment can be produced.

Due to the offset between model center and gage center, the gages will have the following response to the case of fore/aft and side load:

- a/ Fore/aft load. Gage D will indicate a pull or a push. Gages A, B & C a pitching moment
- b/ Side load: Gages B & C will indicate a rolling moment

Side forces will be taken as side loads on gages B & C which are designed to resist them without affecting their normal load measuring accuracy.

The gage center in the case of fore/aft load is obviously contained in a horizontal plane passing through the drag gage D. In the case of side load, it must be in a

WRITTEN BY

G. Jacquem

CHECKED

RE 12-1-1000

~~SECRET~~ DECLASSIFIED

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.

6-0	LOAD GAGE DESIGN
6-1	LOAD ANALYSIS
6-1-1	LOADING CONSIDERATIONS.

LOAD PATHS THROUGH GAGE SECTION - CONT'D

plane passing by the points of zero bending in gages A, B & C operating as cantilever beams with the free end guided against rotation. Since the point of zero bending of gages A, B & C is at the mid distance between the two flanges and since gage D is also placed at mid distance between the same two flanges, the two planes are coincident. The gage center under vertical loads lies on the vertical axis. Hence, the center of all gages is at the intersection of the vertical axis and the plane defined above.

NOTE.

At the time this section of the report was written, the geometry of the gage section was as shown on 6-1-2. Later on, this geometry has been slightly modified to the dimensions shown in 6-3. Since this modification does not materially alter the gage loading, the section has not been rewritten.

However, should exact values of the loads on the gages be needed, they can be computed easily from the equations given in 6-3.

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	L. J. Jaeger	Sept. 1957		

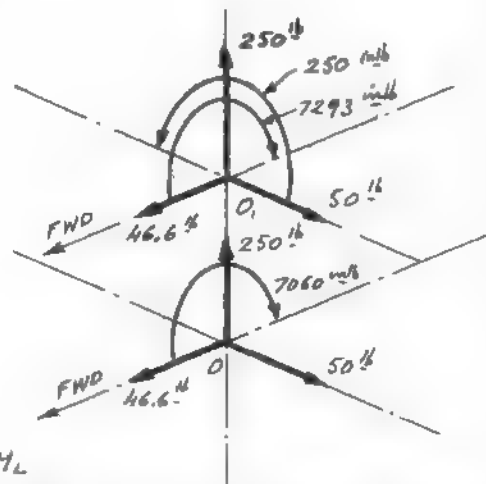
~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-0 LOAD GAGE DESIGN6-1-2 LOADS RESOLVED AT GAGE CENTER.+ 45° CASE - TUNNEL AT $q = 30$ PSF

$$M_L = 7060 + (46.6 \times 5.0) = 7293 \text{ in/lb}$$

$$M_T = 50 \times 5.0 = 250 \text{ in/lb}$$



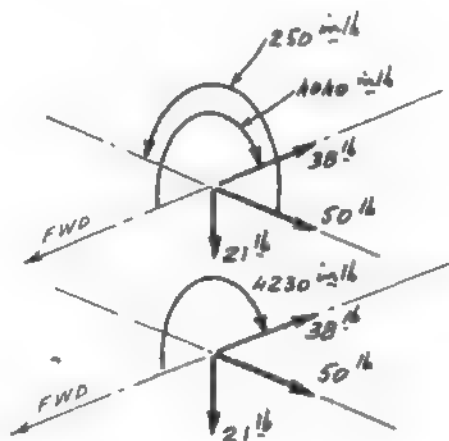
Value of q required to reduce the moment M_L to 4200 in/lb in order not to exceed the strength requirements of the range of $-10^\circ < \alpha < 20^\circ$.

$$q_{45} = 30 \frac{4200}{7300} = 17.25. \quad \text{SAY } 18 \text{ PSF}$$

+ 45° CASE - TUNNEL AT $q = 18$ PSF.

$$M_L = 4230 - (38 \times 5) = 4040 \text{ in/lb}$$

$$M_T = 50 \times 5.0 = 250 \text{ in/lb}$$



DECLASSIFIED

WRITTEN BY

G. Jaeger

CHECKED BY

R. L. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

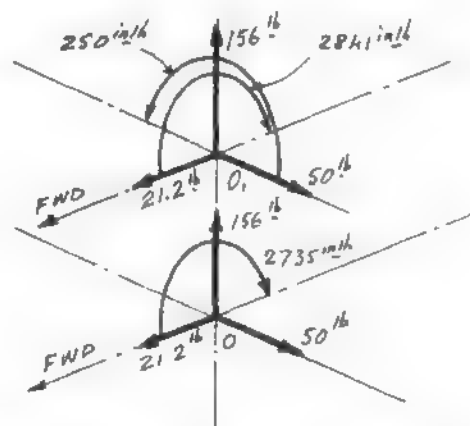
DECLASSIFIED

88

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-0 LOAD GAGE DESIGN6-1-2 LOADS RESOLVED AT GAGE CENTER.+35° CASE. $q = 30 \text{ PSF}$

$$M_L = 2735 + (21.2 \times 5) = 2841 \text{ in/lb}$$

$$M_T = 50 \times 5.0 = 250 \text{ in/lb}$$



In this case, the moment is considerably smaller than 4200 in/lb hence the tunnel can be operated at $q = 30 \text{ PSF}$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	1.	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

6-1-3 - LOAD DISTRIBUTION

DISTRIBUTION OF A NORMAL LOAD ON GAGES A, B & C.

DISTRIBUTION OF A SIDE LOAD ON GAGES A, B & C.

LOAD ON GAGE A.

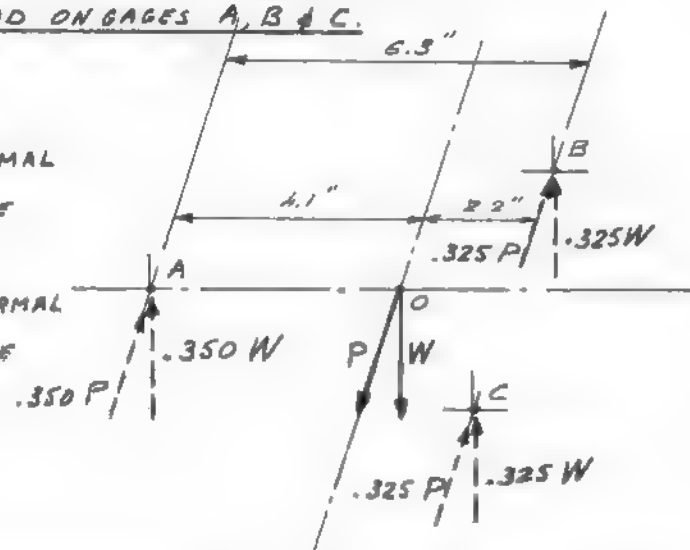
$$W \frac{2.2}{6.3} = .350 W \quad \text{NORMAL}$$

$$P \frac{2.2}{6.3} = .350 P \quad \text{SIDE}$$

LOAD ON GAGES B & C:

$$W \frac{4.1}{6.3 \times 2} = .325 W \quad \text{NORMAL}$$

$$P \frac{4.1}{6.3 \times 2} = .325 P \quad \text{SIDE}$$



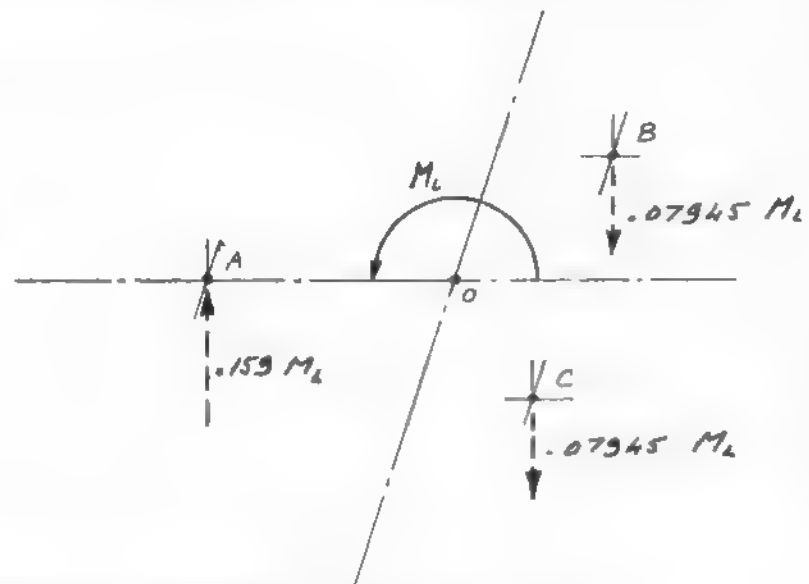
DISTRIBUTION OF A LONGITUDINAL MOMENT ON GAGES A, B & C.

LOAD ON GAGE A

$$\frac{M_L}{6.3} = .159 M_L$$

LOAD ON GAGES B & C

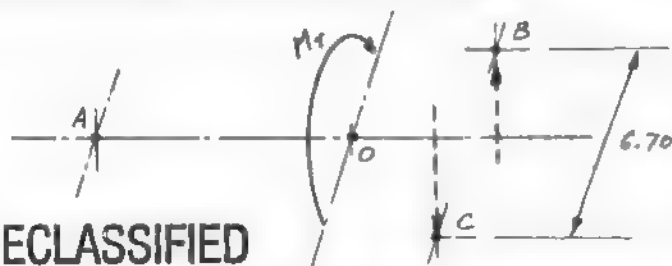
$$\frac{M_L}{2 \times 6.3} = .07945 M_L$$



DISTRIBUTION OF A TRANSVERSAL MOMENT ON GAGES B & C

LOADS ON GAGES B & C

$$\frac{M_T}{6.7} = \pm .1492 M_T$$



DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

H. J. ...

DATE

Sept. 1957

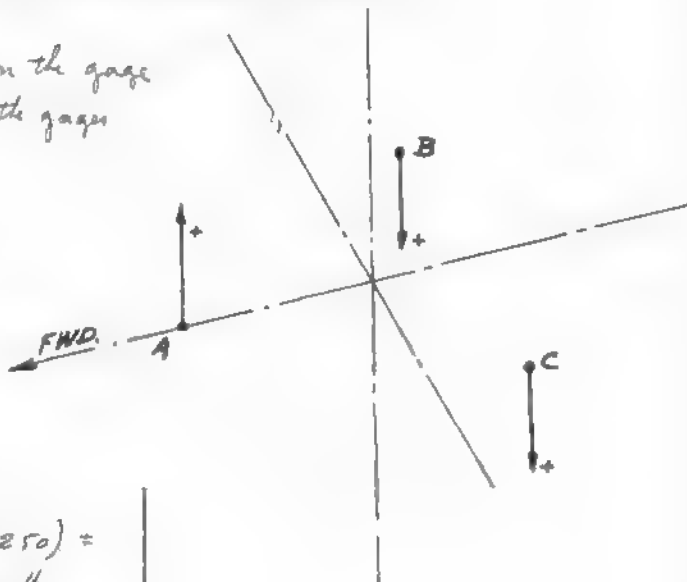
ISSUE

AIRCRAFT

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -6-1-3 LOAD DISTRIBUTION -LOADS ON THE GAGES - EFFECT OF MOMENTS ONLY -

+ve load on gage A: compression on the gage
 +ve " " " B & C: tension on the gages

-10° CASE -

GAGE :

$$A : -.159 \times 4174 = -664.1^{\text{lb}}$$

$$B : (-.07945 \times 4174) + (-.1492 \times 250) = -332 + 37.3 = 294.7^{\text{lb}}$$

$$C : (-.07945 \times 4174) - (-.1492 \times 250) = -332 - 37.3 = 369.3^{\text{lb}}$$

+ 20° CASE -

GAGE :

$$A : -.159 \times 1110 = -176.5^{\text{lb}}$$

$$B : (.07945 \times 1110) + (-.1492 \times 250) = 88.0 + 37.3 = 125.3^{\text{lb}}$$

$$C : (.07945 \times 1110) - (-.1492 \times 250) = 88.0 - 37.3 = 50.7^{\text{lb}}$$

+ 45° - 18° CASE -

GAGE :

$$A : .159 \times 4040 = 643.1^{\text{lb}}$$

$$B : (.07945 \times 4040) + (-.1492 \times 250) = 321.5 + 37.3 = 358.8^{\text{lb}}$$

$$C : (.07945 \times 4040) - (-.1492 \times 250) = 321.5 - 37.3 = 284.2^{\text{lb}}$$

SUMMARY OF GAGE LOADS
EFFECT OF MOMENTS ONLY.

CASE :	-10°	+ 20°	+ 45°
Tunnel 9	30	30	18
GAGE A	664.1 ^{lb} T	-176.5 ^{lb} C	643.1 ^{lb} C
GAGE B	-294.7 ^{lb} C	125.3 ^{lb} T	358.8 ^{lb} T
GAGE C	-369.3 ^{lb} C	50.7 ^{lb} T	284.2 ^{lb} T

REQUIRED GAGE RATING.

$$A : 800^{\text{lb}}$$

$$B : 350^{\text{lb}}$$

$$C : 350^{\text{lb}}$$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

SECRET

DECLASSIFIED

STRESS ANALYSIS OF 1/2 SCALE HOVERING & TRANSITION MODEL6-1.3 LOAD DISTRIBUTIONSUSPENSION ROD.

The rod is designed at an operating stress of 20000 PSI to take a max. load of 550 lb

Required diameter $\sqrt{\frac{4}{\pi} \frac{W}{f}} = D$

$$D = \sqrt{\frac{4}{\pi} \frac{550}{20000}} = \sqrt{.035} = .187''$$

Sectional area: $.187^2 \frac{\pi}{4} = .0275 \text{ in}^2$

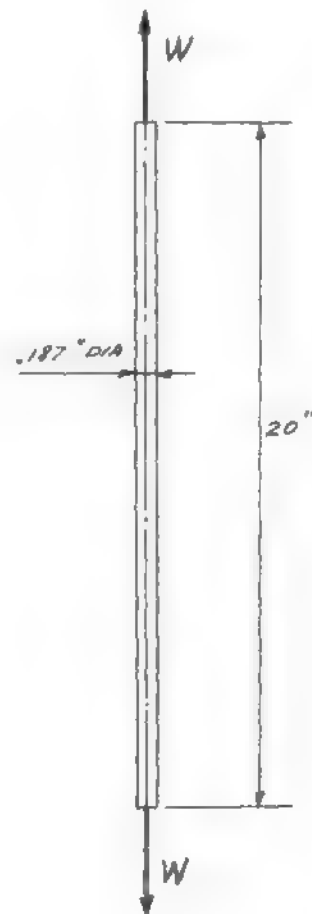
ELONGATION. $\delta = \frac{WL}{AE}$

MAT: SAE - 4130 - CHR. MOLY - STEEL.

@ 125000 PSI UTS.

ELONGATION PER POUND LOAD

$$\delta = W \frac{20}{.0275 \times 125 \times 10^5} = 2.42 \times 10^{-5} W \text{ in/lb}$$



DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	h. d. c.	Sept. 1957		

SECRET

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -

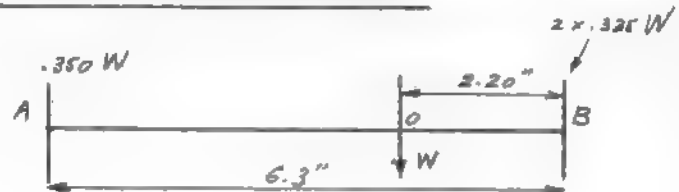
6-1-3 LOAD DISTRIBUTION -

DISTRIBUTION OF LOAD BETWEEN GAGES AND CENTER ROD.

Deflection rate:

$$\text{Gage A : } 2.66 \times 10^{-5} \frac{\text{in}}{\text{lb}}$$

$$\text{Gage B : } 7.42 \times 10^{-5} \frac{\text{in}}{\text{lb}}$$



For a unit gage load

$$\text{Deflection at A : } .35 \times 2.66 \times 10^{-5} = .93 \times 10^{-5} \frac{\text{in}}{\text{lb}}$$

$$\text{Deflection at B : } .325 \times 7.42 \times 10^{-5} = 2.415 \times 10^{-5} \frac{\text{in}}{\text{lb}}$$

Then: deflection at O:

$$\left[2.415 - (2.415 - .93) \frac{2.2}{6.3} \right] \times 10^{-5} = 1.895 \times 10^{-5} \frac{\text{in}}{\text{lb}}$$

$$\text{Deflection rate of the rod : } 2.42 \times 10^{-5} \frac{\text{in}}{\text{lb}}$$

Now, let W_1 & δ_1 be the load and deflection of the rodand W_2 & δ_2 be the load and deflection of the gage system at point Oand ΔW the incremental load on the systemThen, we must have: $\Delta W = W_1 + W_2$ and $\delta_1 = \delta_2$ Let $\Delta W = 1$ and calculate a relation between W_1 & W_2

$$\text{we have: } \delta_1 = 2.42 \times 10^{-5} W_1$$

$$\delta_2 = 1.895 \times 10^{-5} W_2$$

$$\therefore 2.42 \times 10^{-5} W_1 = 1.895 \times 10^{-5} W_2$$

$$W_2 = \frac{2.42}{1.895} W_1 = 1.278 W_1$$

$$\text{Hence: } \Delta W = W_1 + 1.278 W_1 = 2.278 W_1 = 1$$

$$\text{Then } W_1 = \frac{1}{2.278} = .44 \quad \therefore \text{The rod takes } 44\% \text{ of } W$$

the gages 56% of W .

DECLASSIFIED

WRITTEN BY

G. Jacquemin

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~ DECLASSIFIEDSTRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-1-3 LOAD DISTRIBUTION -DISTRIBUTION OF LOAD BETWEEN GAGES & CENTER ROD - cont'd.

From Page : 89 the load on gage A has been found to be 35% of the total load on the gage system and 32.5 % on gage B & C respectively.

Hence: in terms of the incremental load ΔW .

$$\text{Load on gage A: } .56 \times .35 = .196 = 19.6 \%$$

$$\text{Load on gage B or C: } .56 \times .325 = .182 = 18.2 \%$$

Hence: The load distribution is:

ROD	GAGE A	GAGE B	GAGE C
44 %	19.6 %	18.2 %	18.2 %

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	ST. L. G.	Sept. 1957		

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-1-3 LOAD DISTRIBUTIONLOAD ON THE GAGES WITH THE ROD ADJUSTED TO TAKE 200 $\frac{1}{16}$.SUCTION ON-10° CASE - $q = 30$ PSF

LOAD		ROD	A	B	C
		44%	19.6%	18.2%	18.2%
MODEL WEIGHT	200 $\frac{1}{16}$	200 ↓	0	0	0
NORMAL COMP. 197	-3 $\frac{1}{16}$	-1.32 ↑	-.546 ↑	-.546 ↑	-.546 ↑
PRESSURE	286 $\frac{1}{16}$	126 ↓	56 ↓	52 ↓	52 ↓
AIRLOAD	69.13 $\frac{1}{16}$	27.8 ↓	12.4 ↓	11.5 ↓	11.5 ↓
MOMENTS		0	664 ↓	-295 ↑	-363 ↑
		352.48 ↓	731.8 ↓	232.1 ↑	306.1 ↑

+20° CASE - $q = 30$ PSF.

LOAD		ROD	A	B	C
		44%	19.6%	18.2%	18.2%
MODEL WEIGHT	200 $\frac{1}{16}$	200 ↓	0	0	0
NORMAL COMP. 188	-12	-5.28 ↑	-2.35 ↑	-2.185 ↑	-2.185 ↑
PRESSURE	286	126 ↓	56 ↓	52 ↓	52 ↓
AIRLOAD	-443.8	-195.2 ↑	-97.0 ↑	-80.8 ↑	-80.8 ↑
MOMENTS		0	222.5 ↑	148.55 ↓	74 ↓
		145.52 ↓	-255.85 ↑	117.565 ↓	43.015 ↓

NOTE. Airload + pressure load + normal component of model weight =
net normal load given page 40.

Load given above under normal component is the change in normal
load due to model weight with angle of attack

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemont	1.1.1	Sept. 1957		

~~SECRET~~

DECLASSIFIED 95

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MONEY6-1-3 LOAD DISTRIBUTION -LOAD ON THE GAGES WITH THE ROD ADJUSTED TO TAKE 200 lb.SUCTION ON+45° CASE - 9 = 18 PSF

LOAD		ROD	A	B	C
		44%	19.6%	18.2%	18.2%
MODEL WEIGHT	200 lb	200 ↓	0	0	0
NORMAL COMP. 141	-59%	-26 ↑	-11.56 ↑	-10.72 ↑	-10.72 ↑
PRESSURE	286 lb	126 ↓	56 ↓	52 ↓	52 ↓
AIR LOAD	-406 lb	-178.9 ↑	-79.5 ↑	-73.8 ↑	-73.8 ↑
MOMENTS		0	-643 ↑	359 ↓	284 ↓
		121.1 ↓	678.06 ↑	326.48 ↓	251.48 ↓

SUCTION OFF.-10° CASE - 9 = 30 PSF

LOAD		ROD	A	B	C
		44%	19.6%	18.2%	18.2%
MODEL WEIGHT	200 lb	200 ↓	0	0	0
NORMAL COMP. 197	-3%	-1.32 ↑	-588 ↑	-546 ↑	-546 ↑
PRESSURE *	320	141 ↓	62.6 ↓	58.2 ↓	58.2 ↓
AIR LOAD	63.13	27.8 ↓	12.4 ↓	11.5 ↓	11.5 ↓
MOMENTS			664 ↓	295 ↑	369 ↑
		367.48 ↓	718.412 ↓	-225.85 ↑	-299.85 ↑

* SEE PAGE 20

SEE NOTE PAGE 34

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	11	Sept. 1957		

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

96

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -6-1-3 LOAD DISTRIBUTIONLOAD ON THE GAGES WITH THE ROD ADJUSTED TO TAKE 200 $\frac{1}{16}$ SUCTION OFF -+20° CASE - $q = 30$ PSF

LOAD		ROD	A	B	C
		44%	19.6%	18.2%	18.2%
MODEL WEIGHT	200 $\frac{1}{16}$	200 ↓	0	0	0
NORMAL COMP. 188	-12 $\frac{1}{16}$	-5.28 ↑	-2.35 ↑	-2.185 ↑	-2.185 ↑
PRESSURE *	320 $\frac{1}{16}$	141 ↓	62.6 ↓	58.2 ↓	58.2 ↓
AIRLOAD	-443.8 $\frac{1}{16}$	-195.2 ↑	-57.0 ↑	-80.8 ↑	-80.8 ↑
MOMENTS		0	222.5 ↑	148.55 ↓	74 ↓
		140.52 ↓	-249.25 ↑	223.765 ↓	49.215 ↓

+ 45° CASE - $q = 18$ PSF

LOAD		ROD	A	B	C
		44%	19.6%	18.2%	18.2%
MODEL WEIGHT	200 $\frac{1}{16}$	200 ↓	0	0	0
NORMAL COMP 141	-59 $\frac{1}{16}$	-26 ↑	-11.55 ↑	-10.72 ↑	-10.72 ↑
PRESSURE *	320 $\frac{1}{16}$	141 ↓	62.6 ↓	58.2 ↓	58.2 ↓
AIRLOAD	-406 $\frac{1}{16}$	-178.5 ↑	-79.5 ↑	-73.8 ↑	-73.8 ↑
MOMENTS		0	-643 ↑	359 ↓	284 ↓
		136.5 ↓	-671.45 ↑	332.68 ↓	257.68 ↑

* SEE PAGE 20

SEE NOTE PAGE 94

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemin		Sept. 1957		

~~SECRET~~ DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-1-3 - LOAD DISTRIBUTION -LOAD ON THE GAGES WITH THE ROD DISCONNECTED.SUCTION ON.-10° CASE - $q = 30 \text{ PSF}$

LOAD		ROD	A	B	C
		0%	35%	32.5%	32.5%
WEIGHT COMP.	197	0	69 ↓	64 ↓	64 ↓
PRESSURE *	286	0	100 ↓	93 ↓	93 ↓
AIRLOAD	63.13	0	22.1 ↓	20.5 ↓	20.5 ↓
MOMENTS		0	664 ↓	- 295 ↑	- 369 ↑
		0	855.1 ↓	- 117.5 ↑	- 191.5 ↑

+ 20° CASE - $q = 30 \text{ PSF}$

LOAD		ROD	A	B	C
		0%	35%	32.5%	32.5%
WEIGHT COMP.	188 ¹⁴	0	658 ↓	61.1 ↓	61.1 ↓
PRESSURE *	286	0	100 ↓	93 ↓	93 ↓
AIRLOAD	-4.38	0	- 155.4 ↑	- 144.2 ↑	- 144.2 ↑
MOMENTS		0	- 222.5 ↑	148.55 ↓	74 ↓
		0	- 212.1 ↑	158.4 ↓	83.9 ↓

* . SEE PAGE 20

SEE NOTE PAGE 94

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques		Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-1-3 LOAD DISTRIBUTIONLOAD ON THE GAGES WITH THE ROD DISCONNECTED.SUCTION ON+45° CASE - $\beta = 18$ PSF

LOAD		ROD	A	B	C
		0%	35%	32.5%	32.5%
WEIGHT COMP.	141	0	49.4 ↓	45.8 ↓	45.8 ↓
PRESSURE *	286	0	100 ↓	93 ↓	93 ↓
AIRLOAD	-406	0	-142 ↑	-132 ↑	-132 ↑
MOMENTS		0	-643 ↑	359 ↓	284 ↓
			-635.6 ↑	365.8 ↓	290.8 ↓

SUCTION OFF.-10° CASE - $\beta = 30$ PSF

LOAD		ROD	A	B	C
		0%	35%	32.5%	32.5%
WEIGHT COMP.	197	0	69 ↓	64 ↓	64 ↓
PRESSURE *	320	0	112 ↓	104 ↓	104 ↓
AIRLOAD	63.13	0	22.1 ↓	20.5 ↓	20.5 ↓
MOMENTS		0	664 ↓	-295 ↑	-369 ↑
		0	867.1 ↓	-106.5 ↑	-180.5 ↑

* SEE PAGE 20

SEE NOTE PAGE 94

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquin	A. J. J. J.	Sept. 1957		

~~SECRET~~STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -6-1.3 LOAD DISTRIBUTIONLOAD ON THE GAGES WITH THE ROD DISCONNECTED.SUCTION OFF.+ 20° CASE - $\pm = 20$ PSF

LOAD		ROD	A	B	C
		0%	35%	32.5%	32.5%
WEIGHT COMP.	188	0	65.8 ↓	61.1 ↓	61.1 ↓
PRESSURE *	320	0	112 ↓	104 ↓	104 ↓
AIRLOAD	-443.8	0	-155.4 ↑	-144.2 ↑	-144.2 ↑
MOMENTS		0	-222.5 ↑	148.5 ↓	74 ↓
		0	-200.1 ↑	169.4 ↓	94.9 ↓

+ 45° CASE - $\pm = 18$ PSF

LOAD		ROD	A	B	C
		0%	35%	32.5%	32.5%
WEIGHT COMP.	141	0	49.4 ↓	45.8 ↓	45.8 ↓
PRESSURE *	320	0	112 ↓	104 ↓	104 ↓
AIRLOAD	-406	0	142 ↑	132 ↑	132 ↑
MOMENTS		0	643 ↑	359 ↓	284 ↓
		0	-623.6 ↑	374.8 ↓	301.8 ↓

* SEE PAGE 20

SEE NOTE PAGE 94

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	/	Sept. 1957		

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -6-1-3 LOAD DISTRIBUTIONSUMMARY OF LOADS ON GAGES & ROD.

CASE	q PSF	SUCTION ON - OFF	ROD PRELOAD	ROD lb	A lb	B lb	C lb
(1) -10	30	ON	200	352.48 ↓	731.8 ↓	-232.1 ↑	-306.1 ↑
+20	30	ON	200	145.52 ↓	-255.85 ↑	117.56 ↓	43.02 ↓
+45	18	ON	200	121.10 ↓	-678.06 ↑	326.48 ↓	251.48 ↓
(2) -10	30	OFF	200	367.48 ↓	718.41 ↓	-228.85 ↑	-249.85 ↑
+20	30	OFF	200	140.52 ↓	-249.25 ↑	223.77 ↓	49.22 ↓
+45	18	OFF	200	136.5 ↓	-671.45 ↑	332.68 ↓	257.68 ↓
(3) -10	30	ON	DISCONNECT 0	0	855.1 ↓	-117.5 ↑	-191.5 ↑
+20	30	ON	0	0	-212.1 ↑	158.4 ↓	83.9 ↓
+45	18	ON	0	0	-635.6 ↑	265.8 ↓	290.8 ↓
(4) -10	30	OFF	0	0	867.1 ↓	-106.5 ↑	-180.5 ↑
+20	30	OFF	0	0	-200.1 ↑	169.4 ↓	94.9 ↑
+45	18	OFF	0	0	-623.6 ↑	376.8 ↓	301.8 ↓
GAGE RATING :					800	350	350

↓ GAGE IN TENSION

↑ GAGE IN COMPRESSION.

- NOTES :
- 1 - The gages are designed for cases (1) & (2)
 - 2 - Cases (1) & (3) are measurement cases.
Cases (2) & (4) are tunnel starting cases.
 - 3 - Loads on gages B & C are interchangeable depending on the direction of the side load.

WRITTEN BY

G. Jacques

CHECKED BY

J. C. ...

DATE

Sept 1957

ISSUE

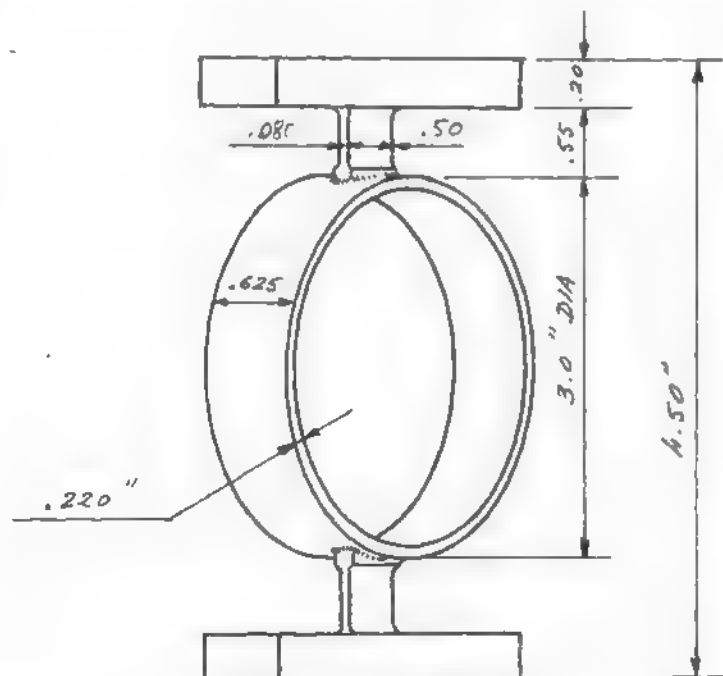
DECLASSIFIED

AIRCRAFT

~~SECRET~~

DECLASSIFIED

101

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -6-2 GAGE DESIGN6-2-1GAGE A - 800^{lb}

This gage is designed according to report AVRO/SPG/TR-B7 for an operating max stress of 40000 PSI at the strain gage section

Required thickness.

$$t = \sqrt{.07425 K^2 + .545 \times 3 K} = .2725 K$$

$$\text{where } K = \frac{W}{40000b} = \frac{800}{40000 \times .625} = .032$$

$$\therefore t = \sqrt{.07425 \times .032^2 + 1.635 \times .032} = .2725 \times .032$$

$$t = \sqrt{.000076 + .0523} = .008725 = \sqrt{.052376} = .008725$$

$$= .2287 - .0087 = .220"$$

MATERIAL :

AN-QQ-S-689 COND "F"

$F_{T1} : 125000 \text{ PSI} - F_{T2} : 100000 \text{ PSI} - F_{S1} : 75000 \text{ PSI}$

WRITTEN BY

G. Jacquin

CHECKED BY

1-2, 1-11

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL-6-2 GAGE DESIGN6-2-1 -GAGE A - cont'd.

With reference to "Formulas for Stress and Strain" by Roark-

- a) Max. bending in the ring at the flexure: $.3183 W R_m$ in-lb
 b) Max bending in the ring at the strain gages: $.1817 W R_m$ in-lb

at a), we also have a max shear load = $\frac{W}{2}$ per sectionat b), we also have a tensile or compressive load = $\frac{W}{2}$ per section.Section modulus of the ring: $\frac{.625 \times .22^3}{6} = .00504 \text{ in}^3$ Sectional area of the ring: $.625 \times .22 = .1375 \text{ in}^2$

Bending moments:

at a/ : $.3183 \times 800 \times \frac{3-.22}{2} = 354 \text{ in-lb}$

at b/ : $.1817 \times 800 \times \frac{3-.22}{2} = 202 \text{ in-lb}$

Stresses at point a/

Bending: $\frac{354}{.00504} = 70200 \text{ PSI}$

Shear : $\frac{800}{2 \times .1375} = 2910 \text{ PSI}$

Principal stress $\frac{70200}{2} + \sqrt{\left(\frac{70200}{2}\right)^2 + 2910^2} = 70320 \text{ PSI}$ unfactored

Stresses at point b/

Bending : $\frac{202}{.00504} = 40000 \text{ PSI}$

Tension : $\frac{800}{2 \times .1375} = 2910 \text{ PSI}$

Total stress : $40000 + 2910 = 42910 \text{ PSI}$ unfactored.

WRITTEN BY

G. Jacques

CHECKED BY

R. L. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

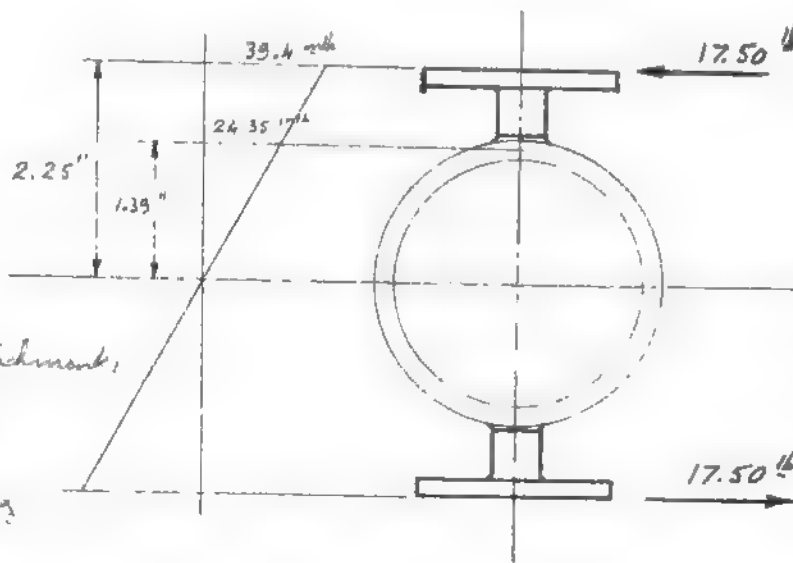
DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -

6-2 GAGE DESIGN

6-2-1-

GAGE A - cont'd.



Bending moment at attachment,
 $17.5 \times 2.25 = 39.4 \text{ in-lb}$

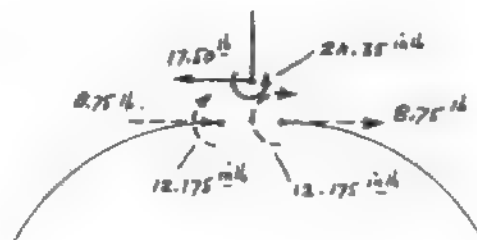
Bending moment in ring
 attachment.
 $17.5 \times 1.39 = 24.35 \text{ in-lb}$

Ring section modulus: $.00504 \text{ in}^3$

Ring sectional area: $.1375 \text{ in}^2$

Bending stress in ring

$$\frac{12.175}{.00504} = 2420 \text{ PSI}$$



Normal stress: $\frac{8.75}{.1375} = 63.7 \text{ lb}$

Max. total normal stress: $2420 + 63.7 = 2483.7 \text{ PSI}$ say 2500 PSI

Total stress on the ring at this point

$$10320 + 2500 = 12820 \text{ PSI, unyielded}$$

$$\text{L/M. M.S. } \frac{100000}{12820} - 1 = \underline{\hspace{2cm}}$$

*. This margin of safety is quoted against the actual stress.
 The factor $n=4$ does not apply in this case

WRITTEN BY

G. Jacquin

CHECKED BY

Wm. J. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -6-2 GAGE DESIGN6-2-1GAGE A - cont'd.FLEXURES -

From report AVRO/SPG/TR-87 for a flexure operating at 20000 PSI under 800 lb with width $b = .50"$
 thickness $K = .080"$ - Sectional area: $.5 \times .08 = .040 \text{ in}^2$
 Flexure length: $.55"$

The side load on the ring induces a bending moment:
 $17.5 \times 2.05 = 35.9 \text{ in lb}$

Section modulus:

$$\frac{.08}{6} .50^2 = .00333 \text{ in}^3$$

Bending stress:

$$\frac{35.9}{.00333} = 10800 \text{ PSI}$$

Total max normal stress: $20000 + 10800 = 30800 \text{ PSI}$ unfactored

Stability in compression as per JOHNSON'S FORMULA

Least moment of inertia: $\frac{.5 \times .08^3}{12} = .00002135 \text{ in}^4$

Radius of gyration $S = \sqrt{\frac{.00002135}{.040}} = \sqrt{.000533} = .0231"$

Slenderness ratio: $\lambda = \frac{.55}{.0231} = 23.8$

Buckling stress: Johnson's formula: $f_c = f_u - \frac{1}{4E} \left(\frac{f_u \lambda}{\pi} \right)^2$

$$f_c = 125000 - \frac{1}{4 \times 3 \times 10^7} \left(\frac{125000 \times 23.8}{\pi} \right)^2 = 125000 - \frac{89.5 \times 10^{10}}{12 \times 10^7}$$

$$= 125000 - 7450 = 117550 \text{ PSI}$$

unfactored: MARGIN OF SAFETY: $\frac{117550}{30800} - 1 =$

2.82

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	1. J. S. 1.	Sept. 1957		

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

105

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -6-2 GAGE DESIGN6-2-1
GAGE A - CONT'D.ATTACHMENT BOLTS -

Attachment is by means of: 2 - $\frac{1}{4}$ " AN STEEL BOLTS - at each end
 steel @ 125000 PSI - Tensile strength of one bolt Ref AN-C-5: 4080^{lb}

Available strength: $4080 \times 2 = 8160$ ^{lb}

Applied load: max. load with factor of 4:
 $800 \times 4 = 3200$ ^{lb}

$$M.S. \quad \frac{8160}{3200} - 1 = \text{-----} \quad 1.5$$

WRITTEN BY

G. Jacques

CHECKED BY

12/1

DATE

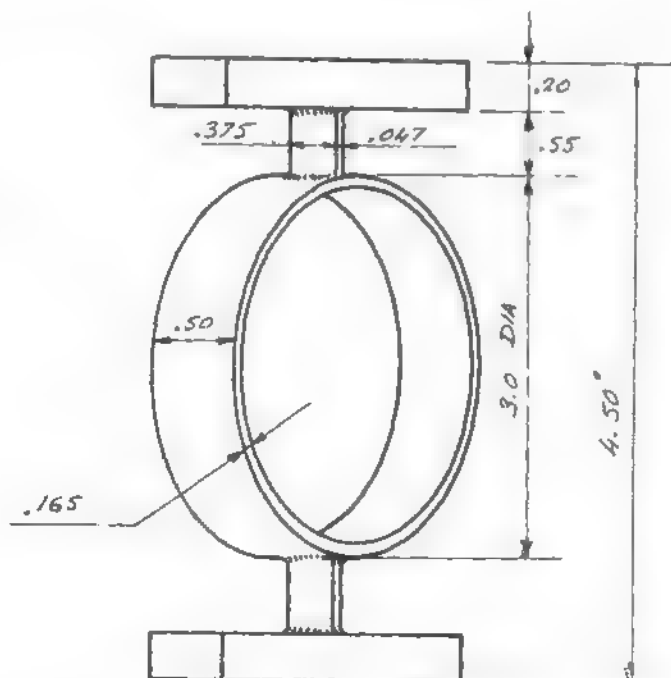
Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-2 - GAGE DESIGN6-2-2 -
GAGES B & CRATED LOAD : 350^{lb}

This gage is designed according to report AVRO/SPG/TR-81 for an operating max stress of 40000 PSI at the strain gage section:

Required thickness

$$t = \sqrt{.07425 K^2 + .545 \times 3 K} - .2725 K$$

$$\text{where } K = \frac{W}{40000 b} = \frac{350}{40000 \times .50} = .0175$$

$$\therefore t = \sqrt{.07425 \times .0175^2 + 1.635 \times .0175} - .2725 \times .0175$$

$$t = \sqrt{.00002275 + .0286} - .004768 = \sqrt{.02862275} - .004768$$

$$= .1693 - .004768 = .16453$$

take .1650"

MATERIAL :

AN - QQ - S - 689 - COND. "F"

$F_{TU} : 125000 \text{ PSI} - F_{TS} : 75000 \text{ PSI}$

DECLASSIFIED

WRITTEN BY

G. Jaeger

CHECKED BY

DATE

Sept 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-2 GAGE DESIGN6-2-2GAGE B & C - cont'd.

With reference to "Formulas for stress and strain" by Roach

a) Max bending in the ring at the flexure: $.3183 W R_m \frac{\text{in} \cdot \text{lb}}{\text{in}^3}$

b) Max. bending in the ring at the strain gages: $.1817 W R_m \frac{\text{in} \cdot \text{lb}}{\text{in}^3}$

at a), we also have a max shear load = $\frac{W}{2}$ per section

at b), we also have a tensile or compressive load = $\frac{W}{2}$ per section

Section modulus of the ring: $\frac{.50 \times .165^2}{6} = .00227 \text{ in}^3$

Sectional area of the ring: $.50 \times .165 = .0825 \text{ in}^2$

Bending moments:

at a): $.3183 \times 350 \times \frac{3 - .165}{2} = 158 \frac{\text{in} \cdot \text{lb}}{\text{in}^3}$

$.1817 \times 350 \times \frac{3 - .165}{2} = 90.2 \frac{\text{in} \cdot \text{lb}}{\text{in}^3}$

Stress at point a)

Bending: $\frac{158}{.00227} = 69600 \text{ PSI}$

Shear: $\frac{350}{2 \times .0825} = 2125 \text{ PSI}$

Principal Stress $\frac{69600}{2} + \sqrt{\left(\frac{69600}{2}\right)^2 + 2125^2} = 70000 \text{ PSI unfactored}$

Stress at point b)

Bending: $\frac{90.2}{.00227} = 39750 \text{ PSI}$

Tension: $\frac{350}{2 \times .0825} = 2125$

Total Stress: $39750 + 2125 = 41875 \text{ PSI unfactored.}$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED 108

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-2 GAGE DESIGN6-2-2
GAGES B & C.

Side load on the gages.
 $50 \times .325 = 16.25 \text{ lb}$

Torsional section modulus
 of the ring section

$$K = \beta \times .165^2 \times .50$$

$$\beta = .270 \quad \text{for } \frac{.165}{.50} = .330$$

$$K = .27 \times .165^2 \times .50 = .00367 \text{ in}^3$$

Max Torsional shear stress: $\frac{T}{K}$

$$\frac{11.525}{.00367} = 4230 \text{ PSI}$$

Direct shear stress in the section

$$\frac{8.125}{.0265} = 98.5 \text{ PSI}$$

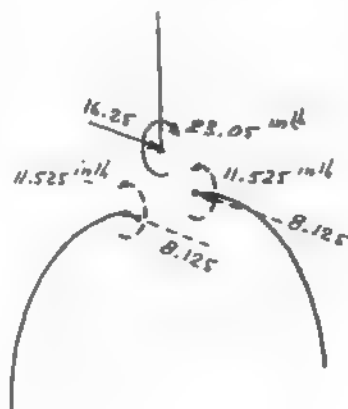
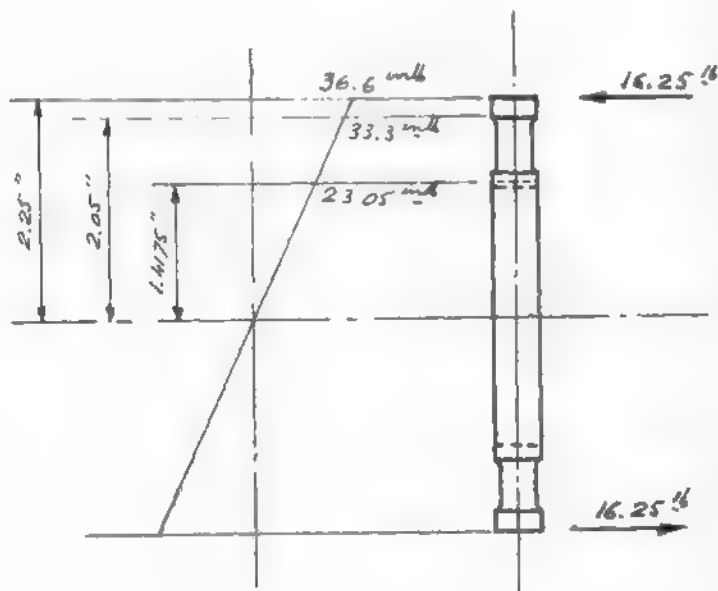
Total Shear Stress in the section:

$$4230 + 98.5 + 2125 = 6458.5 \text{ PSI}$$

$$\text{Principal stress} = \frac{69600}{2} + \sqrt{\left(\frac{69600}{2}\right)^2 + 6458.5^2} = 70200 \text{ PSI unfactored.}$$

$$\text{LIM M.S.} = \frac{100000}{70200} - 1 = \underline{\hspace{2cm}} \quad .42$$

* This margin of safety is quoted against the actual stress
 The factor $n=4$ does not apply in this case.



WRITTEN BY

G. Jaeger

CHECKED BY

H. J. Jaeger

DATE

Sept. 1957

DECLASSIFIED

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-2 GAGE DESIGN6-2-2GAGES B & CFLEXURES:

From report AVRO/SPG/TR 87, for a flexure operating at 20000 PSI under 350° with width $b = .375"$, thickness $K = .047"$

Sectional area: $.375 \times .047 = .0176 \text{ in}^2$

Flexure length: $.55"$

The side load on the ring induces a bending moment.

$$16.25 \times 2.05 = 33.3 \text{ inlb}$$

Section modulus:

$$\frac{.047}{6} \times .375^2 = .0011 \text{ in}^3$$

Bending stress:

$$\frac{33.3}{.0011} = 30200 \text{ PSI}$$

Total max stress: $20000 + 30200 = 50200 \text{ PSI}$

Stability in compression as per JOHNSON'S FORMULA

Least moment of inertia: $\frac{.375 \times .047^3}{12} = 3.25 \times 10^{-6} \text{ in}^4$

Radius of gyration $r = \sqrt{\frac{3.25 \times 10^{-6}}{1.76 \times 10^{-2}}} = \sqrt{1.85 \times 10^{-4}} = .0136"$

Slenderness ratio $\lambda = \frac{.55}{.0136} = 40.4$

Buckling stress Johnson Formula $f_c = f_u - \frac{1}{4E} \left(\frac{f_u \lambda^2}{\pi^2} \right)$

$$f_c = 125000 - \frac{1}{4 \times 3 \times 10^7} \left(\frac{125000 \times 40.4^2}{\pi^2} \right) = 125000 - \frac{25.8 \times 10^6}{12 \times 10^7} = 125000 - 21500 = 103500 \text{ PSI}$$

unfactored MARGIN OF SAFETY: $\frac{103500}{50200} - 1 = 1.06$

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	14	Sept. 1957		

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

110

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.6-2 - GAGE DESIGN6-2-2GAGES B & C - CONT'D.ATTACHMENT BOLTS -

Attachment by means of : 2 - $\frac{1}{4}$ " AN STEEL BOLTS. at each end
 Steel @ 125000 PSI - Tensile strength of one bolt : Ref. AN-C-5. 4080^{lb}

Available strength $4080 \times 2 = 8160$ ^{lb}

Applied load : max. load with factor of 4
 $350 \times 4 = 1400$ ^{lb}

$$M.S. \frac{8160}{1400} - 1 = \text{-----} 4.8$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemont	1-07-2-1-11	Sept. 1957		

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL6-2 - GAGE DESIGN6-2-3GAGE D - cont'd.

With reference to "Formulas for Stress and Strain" by Roark

- a) Max bending in the ring at the flange: $.3183 W R_m$ ^{in-lb}
 b) Max bending on the ring at the strain gage: $.1817 W R_m$ ^{in-lb}

at a), we also have a max shear load = $\frac{W}{2}$ per section

at b), we also have a tensile or compressive load = $\frac{W}{2}$ per section

Section modulus of the ring $\frac{.40 \times .10^2}{6} = .000667 \text{ in}^3$

Sectional area of the ring = $.40 \times .10 = .040 \text{ in}^2$

Bending moments:

$$\text{at a) : } .3183 \times 150 \times \frac{2 - .10}{2} = 46.6 \text{ in-lb}$$

$$\text{at b) : } .1817 \times 150 \times \frac{2 - .10}{2} = 26.6 \text{ in-lb}$$

Stresses at point a)

$$\text{Bending: } \frac{46.6}{.000667} = 70000 \text{ PSI}$$

$$\text{Shear: } \frac{150}{2 \times .040} = 1875 \text{ PSI}$$

$$\text{Principal Stress: } \frac{70000}{2} + \sqrt{\left(\frac{70000}{2}\right)^2 + 1875^2} = 70100 \text{ PSI unfactored.}$$

$$\text{unfactored: LIM. M.S. } \frac{100000}{70100} - 1 = \text{_____} \quad -43$$

Stresses at point b)

$$\text{Bending: } \frac{26.6}{.000667} = 40000 \text{ PSI}$$

$$\text{Tension: } \frac{150}{2 \times .040} = 1875 \text{ PSI}$$

$$\text{Total Stress: } 40000 + 1875 = 41875 \text{ PSI unfactored}$$

WRITTEN BY

G. Jacques

CHECKED BY

J. F. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.6-2 GAGE DESIGN6-2.3GAGE D - cont'd.FLEXURES:

From report A.R.T. SPG/TR 87, for a flexure operating at 20000 PSI under 150 lb with width $b = .25"$: thickness $K = .030"$

Flexure length: $.35"$

Sectional area $.25 \times .03 = .0075 \text{ in}^2$

Stability in compression as per JOHNSON'S FORMULA

Least moment of inertia $= \frac{.25 \times .03^3}{12} = .5625 \times 10^{-6} \text{ in}^4$

Radius of gyration $S = \sqrt{\frac{.5625 \times 10^{-6}}{.75 \times 10^{-2}}} = .866 \times 10^{-2} = .00866"$

Slenderness ratio $\lambda = \frac{.35}{.00866} = 40.5$

Buckling stress, Johnson's formula, $f_c = f_a - \frac{1}{4E} \left(\frac{f_a \lambda}{\pi} \right)^2$

$$\begin{aligned} f_c &= 125000 - \frac{1}{4 \times 3 \times 10^7} \left(\frac{125000 \times 40.5}{\pi} \right)^2 \\ &= 125000 - \frac{1}{12 \times 10^7} \left(25,95 \times 10^3 \right)^2 = 125000 - 21650 \\ &= 103350 \text{ PSI} \end{aligned}$$

$$\text{MARGIN OF SAFETY} = \frac{103350}{20000} - 1 = 4.17$$

NOTE. A large Margin of Safety is necessary on this flexure as bending stresses due to deflection of the other gages could not be avoided with sufficient accuracy.

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	10.1.1957	Sept. 1957		

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.6-2 GAGE DESIGN6-2-3GAGE D - CONT'D.

Attachment by means of 1 - $\frac{1}{8}$ " AN STEEL BOLT at each end
 Steel @ 125000 PSI - Bolts in double shear
 Shear strength - Ref AN-C-5 - single shear: 3680 ^{lb}

Strength of bolt: $3680 \times 2 = 7360$ ^{lb}

Applied load: max. load with factor of 4:
 $150 \times 4 = 600$ ^{lb}

$$MS \quad \frac{7360}{600} - 1 = \text{-----} > 1$$

WRITTEN BY

G. Jacques

CHECKED BY

H. J. ...

DATE

Sept. 1957

ISSUE

DECLASSIFIED

AIRCRAFT

~~SECRET~~

~~SECRET~~STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7.0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1 HORIZONTAL TUBE7-1-1 TUBE IN BENDING.SECTION PROPERTIES OF THE TUBE.Size: $7" \times \frac{3}{16}"$ - ID = 6.625"

Sectional area:

$$A = \frac{\pi}{4} (7^2 - 6.625^2) = 3.94 \text{ in}^2$$

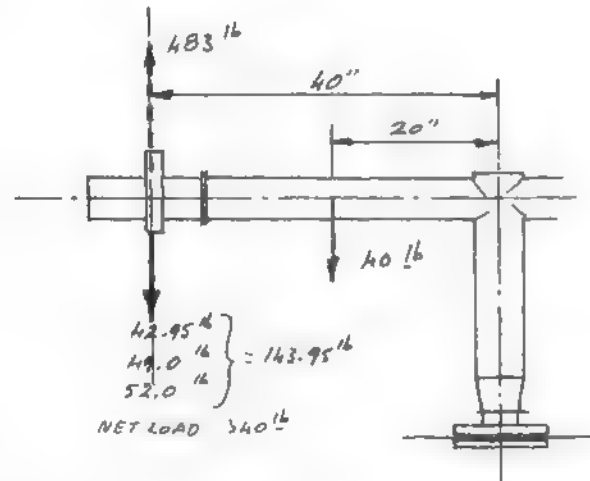
Moment of inertia:

$$I = \frac{\pi}{64} (7^4 - 6.625^4) = 23.3 \text{ in}^4$$

Section modulus

$$Z = \frac{I}{\frac{7}{32}} = 6.65 \text{ in}^3$$

The max support reactions under both static and aerodynamic loading occurs with the incidence of the model at 45° . Then

45° CASE.

REF. SECTION 4-3-3 - & APPENDIX A

Bending moment under static load

Bending moment at the center line:

$$M = -(340 \times 40) + (40 \times 20) = -13600 + 800 = -12800 \text{ in} \cdot \text{lb.}$$

Bending moment under model airload

$$\text{Vertically. } 333.1 \times 40 = 13320 \text{ in} \cdot \text{lb}$$

REF. 4-3-5

$$\text{Horizontally: } 126.1 \times 40 = 5050 \text{ in} \cdot \text{lb}$$

WRITTEN BY

G. Jacques

CHECKED BY

15/1/57

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

117

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE.7-1 HORIZONTAL TUBE7-1-1 TUBE IN BENDING45° CASE - CONT'D.

Since airloads relieve the static loads, the critical loads occur with the tunnel off.

Then: max. bend. stress in the tube

$$f_b = \frac{M}{Z} \quad \text{h} \quad \frac{12800}{6.65} = 7660 \text{ PSI}$$

$$\text{M.S.} \quad \frac{55000}{7660} - 1 = \text{---} \quad 6.16$$

-10° CASE.

This case is to be considered as bending moments from static load add to bending moment from airload. $(330 - 144) = 186 = R_a$.

Static load:

$$M = (186 \times 4) - (.40 \times 20) = 7440 - 800 = 6640 \text{ in-lb.}$$

Airload:

$$\text{Vertical: } 109.31 \times 40 = 4370 \text{ in-lb}$$

$$\text{Horizontal: } 13.59 \times 40 = 544 \text{ in-lb}$$

Total Bending moment:

$$M_T = \sqrt{(6640 + 4370)^2 + 544^2} = 11024 \text{ in-lb}$$

Max bending stress:

$$f_b = \text{h} \quad \frac{11024}{6.65} = 6640 \text{ PSI}$$

$$\text{M.S.} = \frac{55000}{6640} - 1 = \text{---} \quad 7.30$$

WRITTEN BY

G. Jacquemin

CHECKED BY

12/1/57

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

118

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1 HORIZONTAL TUBE7-1-2 -FLANGES ON 7.00" TUBE.

Bending Moment:

$$340 \times 5 = 1700 \text{ lb} \text{ unfactored}$$

Shear force:

$$184 - 144 = 340 \text{ lb} \text{ unfactored.}$$

Bolt strength in tension

Ref. AN-C-5

$$\text{AN-6} : \frac{3}{8} \text{ DIA.} : 10100 \text{ lb}$$

$$\text{AN-5} : \frac{5}{16} \text{ DIA.} : 6500 \text{ lb}$$

Bolt strength in shear:

$$\text{AN-6} : \frac{3}{8} \text{ DIA.} : 8280 \text{ lb}$$

$$\text{AN-5} : \frac{5}{16} \text{ DIA.} : 5750 \text{ lb}$$

Centroid of bolt cluster in tension

$$(10100 - 6500) \frac{4.15}{10100 + (7 \times 6500)} = .269 \text{ inches}$$

Distribution of tensions due to bending in the bolt cluster

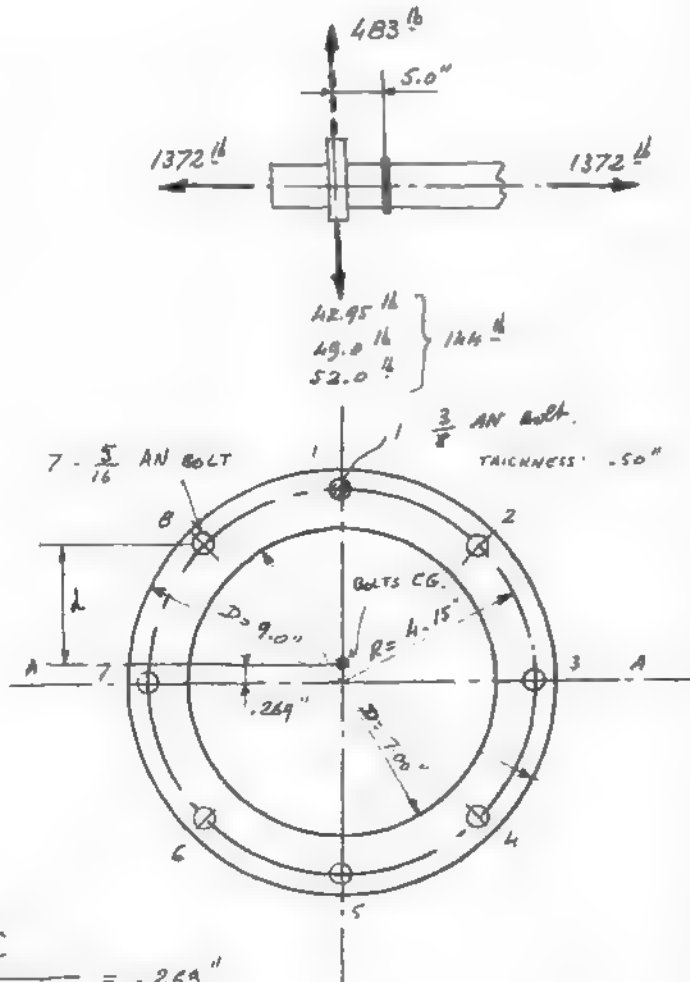
The flange pressure in the compression side is assumed concentrated at the bolts.

With S = the strength of any bolt. F = force on the bolts:

d = distance of bolts to centroid.

$$F_{iM} = M \frac{d_i S_i}{\sum d^2 S}$$

Direct tension: $F_{iT} = T \frac{S_i}{\sum S}$



WRITTEN BY

G. Jaeger

CHECKED BY

12/1/57

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

119

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1 HORIZONTAL TUBE7-1-2.FLANGES ON 7.00" TUBE- CONT'D.

BOLT.	1	2	3	4	5	6	7	8
S	10100	6500	6500	6500	6500	6500	6500	6500
d	3.881	2.661	- .269	- 3.199	- 4.419	- 3.199	- .269	2.661
d ²	15.1	7.1	- .0725	10.12	19.55	10.12	.0725	7.1
Sd	39.2	17.3	- 1.75	- 20.8	- 28.7	- 20.8	- 1.75	17.3
Sd ²	1525	46.2	- .471	65.8	127.0	65.8	- .471	46.2
Sd/ΣSd ²	.0778	.0344	- .00347	- .0413	- .0570	- .0413	- .00347	.0344
$\frac{S}{\Sigma S}$.182	.117	.117	.117	.117	.117	.117	.117
F _{JM} lb	161.0	71.0	- 7.2	- 85.5	- 118.0	- 85.5	- 7.2	71.0
F _{JT} lb	250.0	160.5	160.5	160.5	160.5	160.5	160.5	160.5
F _{JTOTAL} lb	411.0	231.5	153.3	85.0	42.5	85.0	153.3	231.5

unfactored loads.

$$\Sigma Sd^2 = 504.442.$$

$$\Sigma S = 55.6$$

$$\text{Total Bending moment: } 1700 + (1372 \times .269) = 1700 + 369 = 2069 \text{ in}^2$$

Bolts in Shear:

$$\text{Total shear strength available } 8280 + (7 \times 5750) = 8280 + 40250 = 48530 \text{ lb}$$

$$\text{Shear on AN-6 Bolt: } 329 \frac{8280}{48530} = 57 \text{ lb unfactored}$$

$$\text{Shear on AN-5 Bolt: } 329 \frac{5750}{48530} = 40.1 \text{ lb unfactored.}$$

Allowable tension on bolts:

Ref. AN-C-5

$$Y = b \sqrt{1 - \left(\frac{x}{a}\right)^3} = 10100 \sqrt{1 - \left(\frac{57}{8280}\right)^3} = 10100 \times \sqrt{1 - (.00688)^3}$$

effect of shear is negligible

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	1. 1. 1.	Sept. 1957		

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1 HORIZONTAL TUBE7-1-2FLANGES ON 7.00" TUBE - CONT'D.

Margin of Safety on bolts:

$$AN-6 - : M.S. : \frac{10100}{4 \times 411} - 1 = \underline{\hspace{2cm}} \quad 5.14$$

$$AN-5 : M.S. : \frac{6800}{4 \times 231.5} - 1 = \underline{\hspace{2cm}} \quad 6.03$$

~~SECRET~~ DECLASSIFIEDSTRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1 HORIZONTAL TUBE7-1-2FLANGES ON 7.00" TUBE - CONT'D.

Margin of Safety on bolts:

$$AN-6 - MS \quad \frac{10100}{4 \times 411} - 1 = \text{-----} \quad 5.14$$

$$AN-5 : MS \quad \frac{6500}{4 \times 231.5} - 1 = \text{-----} \quad 6.03$$

WELD.Assume the load of AN-6 bolt taken by 2" of $\frac{1}{4}$ " weld

$$\text{Weld area: } 2 \times .25 = .50 \text{ in}^2$$

Allowable UTS of weld metal: 51000 PSI (Ref. AN-C-5)

" USS " " " : 32000 PSI (" ")

$$\text{Weld Stress: } \frac{411}{.5} = 822 \text{ PSI unfactored.}$$

$$MS \quad \frac{32000}{4 \times 822} - 1 = \text{-----} \quad 8.71$$

DECLASSIFIED

WRITTEN BY G. Jaeger	CHECKED BY 11 / 11	DATE Sept. 1957	ISSUE	AIRCRAFT
-------------------------	-----------------------	--------------------	-------	----------

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1-3 - MAIN SUPPORT BEARINGS.MAIN STRUTS BEARINGS.

SKF. BALL BEARING - N° 6238 - M.

Ref. SKF CATALOG N° 551 - STATIC STRENGTH : RADIAL: 53000 ^{lb}
 DYNAMIC " : " : 44000 ^{lb}

Max applied load. $\sqrt{333.1^2 + 124.1^2} = 356$ ^{lb} - Ref. A.3.

$$M.S. \quad \frac{53000}{4 \times 356} - 1 = \text{---} > 10$$

Static load on bearings : tunnel stopped. 352 ^{lb} - Ref. B.3.

BEARING HOUSING.MOUNTING BOLTS3 BOLTS: $\frac{1}{2}$ " DIA INTERNAL WRENCHINGNAS BOLTS in tension: 23500 ^{lb} per boltTotal strength available $23500 \times 3 = 70500$ ^{lb}

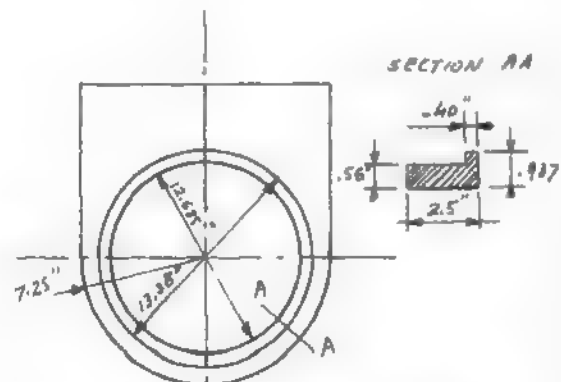
$$M.S.: \quad \frac{70500}{4 \times 356} - 1 = \text{---} > 10$$

LUG :

MATERIAL: SAE 1020 STEEL.

Stressing as per Melcon & Hoblit
 method.

Tension & bearing.



WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaques	1. 1. 1.	Sept 1957		

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1-3 MAIN SUPPORT BEARINGS.LUG - CONT'D.Tension.

$$\text{Ratio: } \frac{\text{Width}}{\text{I.D.}} = \frac{7.25 \times 2}{13.38} = 1.083$$

Cof: $K_t = .99$ from graph #12

$$\text{Tensile stress in the ring: } f_t = \frac{P}{K_t A} = \frac{356 \times 4}{.99 \times 2.5 \times .56} = 1260 \text{ PSI}$$

Bearing:

Ratio: $\frac{\text{edge distance}}{\text{I.D.}}$. In this case: concentric lug:

$$\therefore \text{Ratio } \frac{\text{edge distance}}{\text{I.D.}} = \frac{\text{Width}}{2 \text{ I.D.}} = \frac{1.083}{2} = .5415$$

Cof $K_{br} = .10$ from graph #13

$$\text{Bearing stress on the ring: } f_{br} = \frac{P}{K_{br} A} = \frac{356 \times 4}{.10 \times 2.5 \times .56} = 10200 \text{ PSI}$$

Characteristics of material

AN-5-11. Ref. AVRO DESIGN MANUAL - Sect H - 3.2.4.4

UTS: 55000 PSI

UBS: 90000 PSI

YTS: 36000 PSI

MARGINS OF SAFETY

$$\text{TENSION: } \frac{55000}{1260} - 1 = \text{_____} > 10$$

$$\text{BEARING: } \frac{90000}{10200} - 1 = \text{_____} > 8$$

WRITTEN BY

G. J. Janssen

CHECKED BY

12. J. J. Janssen

DATE

Sept. 1957

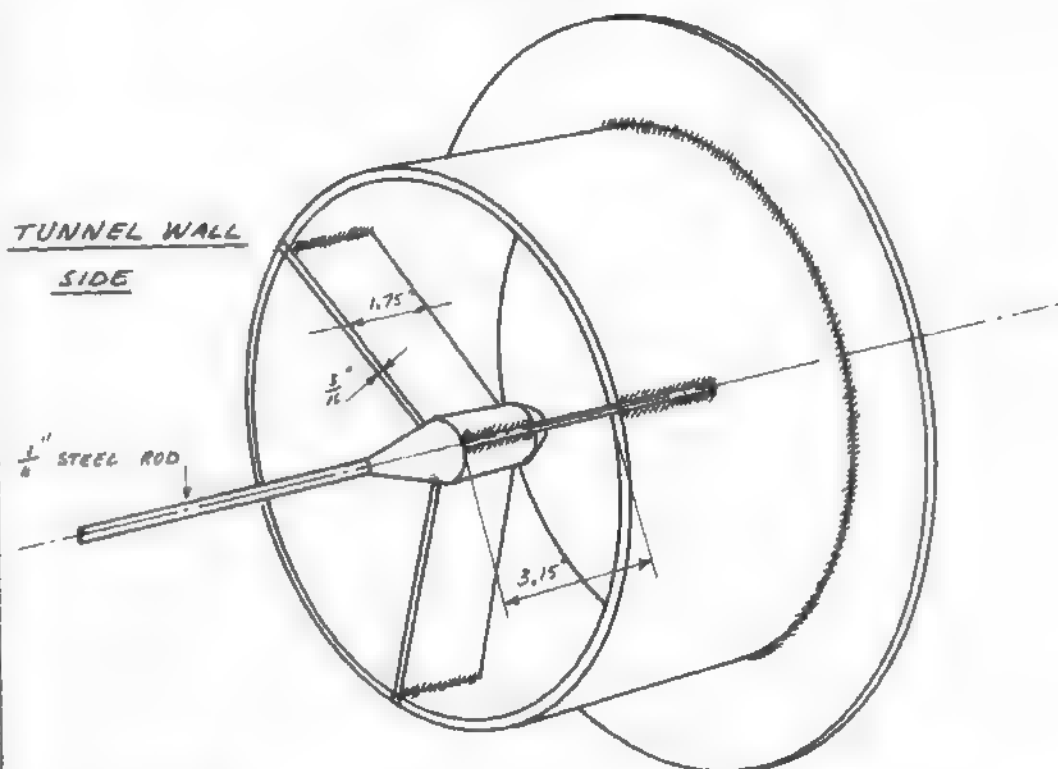
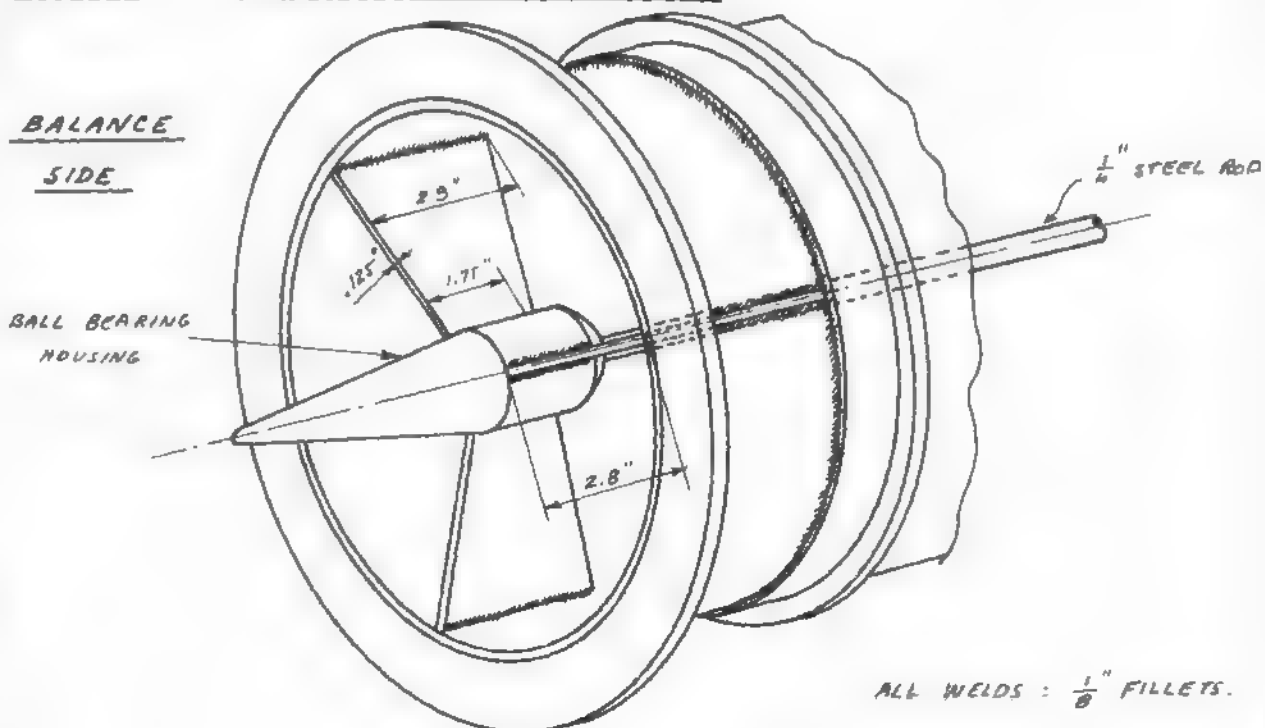
ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1-4 - PRESSURE HOLDING LINN.

WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

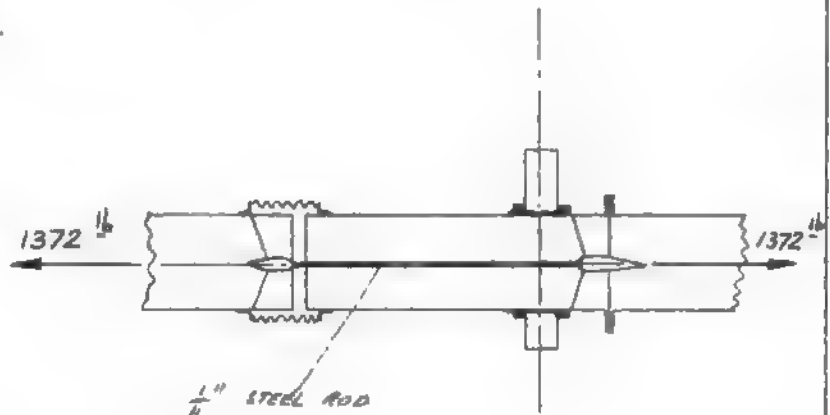
AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL.7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1-4PRESSURE HOLDING LINK -

LENGTH IN TENSION: 24.40"

MIN. DIA. AT END OF THREAD: .233"

UNFACTORED LOAD: 1372 ^{lb} TENSION.

REF. H-3 5

FULLY FACTORED LOAD: $1372 \times 4 = 5490$ ^{lb}Sectional area - $.233^2 \frac{\pi}{4} = .0427$ ⁱⁿ²Tensile stress: $\frac{5490}{.0427} = 128800$ PSI

1- The rod is made of SAE 4130 steel @ 125000 PSI

M.S.

$$\frac{125000}{128000} - 1 =$$

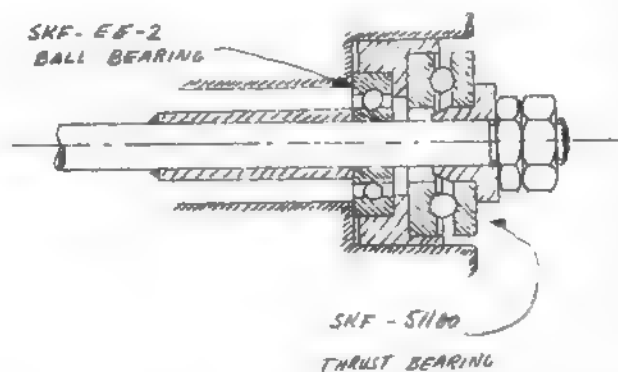
ACTUAL M.S.

Rod elongation under load: $\frac{1372 \times 24.4}{.0427 \times 30 \times 10^6} = .0262$ "BALL BEARINGS CAPACITY

Ref SKF CATALOG N° 551

EE-2 - Static 216 ^{lb} radial
 Dynamic 430 ^{lb} radial

51100 - Static 2500 ^{lb} axial
 Dynamic 1730 ^{lb} axial.

SKF-EE-2
BALL BEARING

SKF-51100

THRUST BEARING

WRITTEN BY

G. Jaeger

CHECKED BY

1 / 1

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

125

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1-4PRESSURE HOLDING LINK. CONT'D.SKF - BALL BEARINGS:

According to SKF catalogue #551 - page 21: "Static Carrying Capacity". The failing load of ball bearings is usually higher than 8 x static load indicated in the tables.

Hence: for the thrust bearing #5110-0: the failing load is approx: $2500 \times 8 = 20000 \text{ lb}$

$$H.S. \quad \frac{20000}{1372} - 1 = \underline{\hspace{2cm}}$$

13.5

WRITTEN BY

G. Jaeger

CHECKED BY

J.C. /

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 - STRESS ANALYSIS - MODEL SUPPORT STRUCTURE.7-1-4 PRESSURE HOLDING LINK.END BRACKETS.BALANCE SIDE.

Each vane takes $\frac{1}{3}$ of the load.

Each vane is fully fixed on the bearing housing and can also be considered as fully fixed on the tube side since it is welded to two rings.

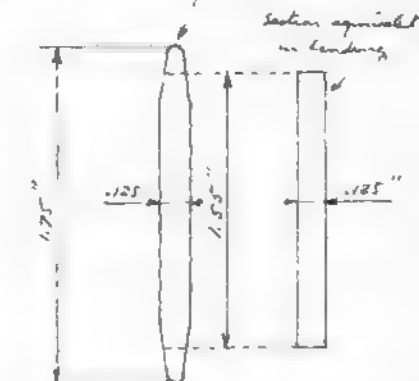
Hence load in the vane $1372 \times \frac{4}{3} = 1830 \text{ lb}$ fully factored.

Max bending moment $1830 \frac{2.8}{2} = 2560 \text{ in lb}$ / Vane section

Section modulus of vane at small end

$$\frac{1.5^2 \times .125}{6} = .050 \text{ in}^3$$

Bending Stress $\frac{2560}{.050} = 51200 \text{ PSI}$



$$M.S \quad \frac{55000}{51200} - 1 = \text{---} \quad .07$$

WELD FILLETS:

2 fillets, $.125" \times 1.75"$ taking 2560 in lb bending
+ 1830 lb direct shear

Ref. AN-C-5. Shear strength of welded joint 32000 PSI

Weld area: $2 \times .125 \times 1.75 = .437 \text{ in}^2$

direct Shear stress: $\frac{1830}{.437} = 4180 \text{ PSI}$

Section modulus of weld in shear: $2 \frac{1.75^2 \times .125}{6} = .1272 \text{ in}^3$

WRITTEN BY

G. Jaeger

CHECKED BY

1.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

127

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 - STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1 - 4 PRESSURE HOLDING LINK.END BRACKETS - CONT'DBALANCE SIDE - CONT'D

Shear stress due to bending in the weld

$$\text{max. } \frac{2560}{.1272} = 20150 \text{ PSI}$$

Max shear stress in the weld: $\sqrt{20150^2 + 4190^2} = 20600 \text{ PSI}$

$$\text{M.S. } \frac{32000}{20600} - 1 = \text{---} \quad .55$$

TUNNEL WALL SIDE -Each vane takes $\frac{1}{3}$ of the load

Each vane is fully fixed on the center piece and has some degree of flexing on the tube. It will be assumed that the tube provides a fixing about equal to half that of the center piece

Hence: Load on each vane; $1372 \times \frac{4}{3} = 1830 \text{ lbs. full. load}$

Max Bending Moment

$$1830 \times \frac{2}{3} \times 3.15 = 3840 \text{ in. lbs.}$$

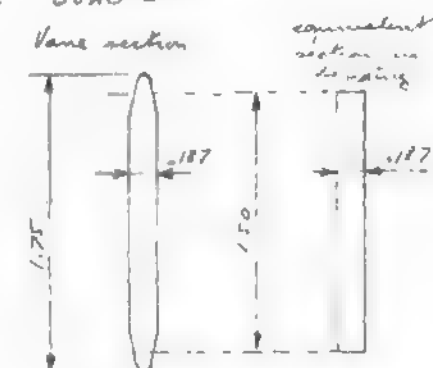
Section modulus of the vane:

$$\frac{1.5^2 \times .187}{6} = .0701 \text{ in}^3$$

Max. bending stress

$$\frac{3840}{.0701} = 54800 \text{ PSI}$$

$$\text{M.S. } \frac{55000}{54800} - 1 = \text{---} \quad .005$$



WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-1-4 PRESSURE HOLDING LINK.END BRACKETS - CONT'DTUNNEL WALL SIDE - CONT'D.WELD FILLETS.

2 fillets. $.125 \times 1.75"$ taking 3840 $\frac{1}{2}$ bending
+ 1820 $\frac{1}{2}$ direct shear

Ref. AN-C-5: Shear strength of welded joint: 32000 PSI

Weld area: $2 \times .125 \times 1.75 = .437 \text{ in}^2$

Direct shear stress $\frac{1820}{.437} = 4180 \text{ PSI}$

Section modulus of weld in shear. $2 \frac{1.75^2 \times .125}{6} = .1272 \text{ in}^3$

Shear stress due to bending in the weld:

max: $\frac{3840}{.1272} = 30200 \text{ PSI}$

Max shear stress on the weld: $\sqrt{30200^2 + 4180^2} = 30500 \text{ PSI}$

M.S. $\frac{32000}{30500} - 1 = \text{-----} .05$

WRITTEN BY

G. Jaeger

CHECKED BY

DATE

Sept 1957

ISSUE

AIRCRAFT

DECLASSIFIED

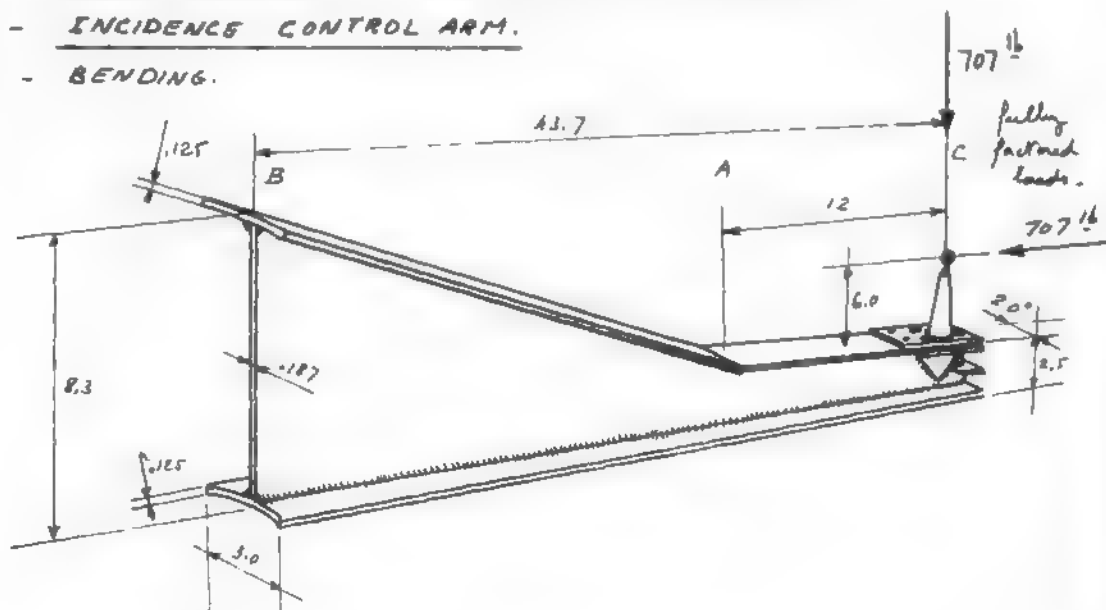
~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.

7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE

7-2 - INCIDENCE CONTROL ARM.

7-2-1 - BENDING.



Max load on this member is $250 \frac{1}{2}$ when $\alpha = 45^\circ$ and tunnel stopped

Hence: load normal to the arm and fully factored:

$$\frac{250 \times 4}{\sqrt{2}} = 707 \frac{1}{2}$$

Compression in the arm: $\frac{250 \times 4}{\sqrt{2}} = 707 \frac{1}{2}$

Bending Moments

$$M_C: 707 \times (6 + 2.5 - 1.25) = 707 \times 7.25 = 5120 \text{ in-lb}$$

$$M_A: 707 \times (6 + 2.5 - 1.25) - (707 \times 12) = 5120 - 8480 = -3360 \text{ in-lb}$$

$$M_B: 707 (6 + 2.5 - 4.15) - (707 \times 43.7) = 3075 - 30900 = -27825 \text{ in-lb}$$

WRITTEN BY

G. Jacques

CHECKED BY

1. 1. 1. 1.

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-2-1 INCIDENCE CONTROL ARM. - BENDINGSECTION A & C

$$\text{Sectional area: } 2.5 \times 2 - 2.25 \times 1.813 =$$

$$5 - 4.08 = .92 \text{ in}^2$$

$$\text{Section modulus } \frac{2.5^3 \times 2 - 2.25^3 \times 1.813}{6} =$$

$$= \frac{13.922}{6} = .63 \text{ in}^3$$

SECTION B

$$\text{Sectional area: } 8.3 \times 3 - 8.05 \times 2.813 =$$

$$24.9 - 23.4 = 1.5 \text{ in}^2$$

$$\text{Section modulus: } \frac{8.3^3 \times 3 - 8.05^3 \times 2.813}{6} =$$

$$= \frac{207.183}{6} = 4 \text{ in}^3$$

Bending stresses.

$$\text{Section C } \frac{5120}{.63} = 8140 \text{ PSI}$$

$$\text{Section B: } \frac{27125}{4} = 6960 \text{ PSI}$$

Compression stress

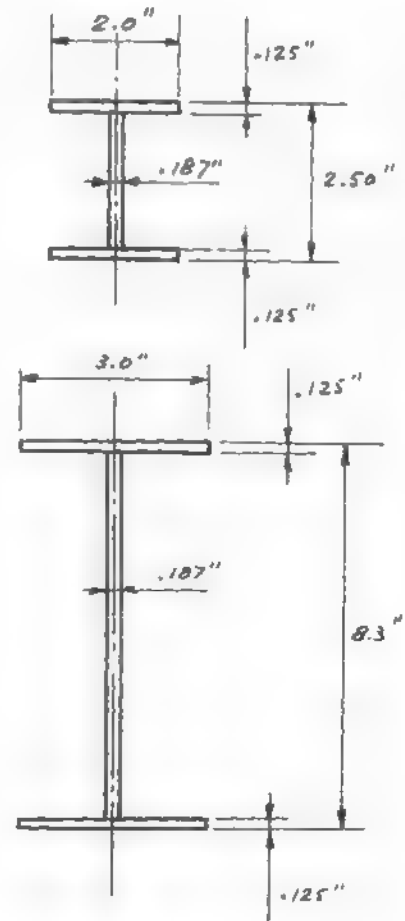
$$\text{Section C: } \frac{707}{.92} = 768 \text{ PSI}$$

$$\text{Section B: } \frac{707}{1.5} = 472 \text{ PSI}$$

Total max stresses

$$\text{Section C: } 8140 + 768 = 8908 \text{ PSI}$$

$$\text{Section B: } 6960 + 472 = 7432 \text{ PSI}$$



WRITTEN BY

G. Jaeger

CHECKED BY

J. C. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-2 INCIDENCE CONTROL ARM.7-2-2ATTACHMENT LINK - CONT'D

Circular section in bending + compression at bottom of link
 1.125" dia SAE 1020 steel.

$$\text{Bending moment} : 707 \times 6 = 4242 \text{ in-lb}$$

$$\text{Section modulus} : \frac{\pi}{64} D^3 = .0984 \times 1.125^3 = .0984 \times 1.424 = .14 \text{ in}^3$$

$$\text{Sectional area} : \frac{\pi}{4} D^2 = \frac{\pi}{4} \times 1.125^2 = 1.0 \text{ in}^2$$

$$\text{Bending stress} : \frac{4242}{.14} = 30300 \text{ PSI}$$

$$\text{Compression stress} : \frac{707}{1.0} = 707 \text{ PSI}$$

$$\text{Total max. comp. stress} : 30300 + 707 = 31007 \text{ PSI}$$

$$\text{M.S.} \quad \frac{55000}{31007} - 1 = \text{---} \quad -77$$

WELD FILLETS.

2 FILLETS. $\frac{1}{8}$ " wide

Consider the fillets as rings having $\frac{1}{8}$ " width and a mean dia. of 1.125"

$$\therefore D = 1.25" \quad d = 1.00"$$

$$\text{Sectional area} : \frac{\pi}{4} (D^2 - d^2) = \frac{\pi}{4} (1.25^2 - 1^2) = \frac{\pi}{4} \times .56 = .440 \text{ in}^2$$

$$\text{Section modulus} \quad \frac{\pi}{32} \left(\frac{D^4 - d^4}{D} \right) = .0984 \left(\frac{1.25^4 - 1^4}{1.25} \right) = .0984 \times \frac{2.44}{1.25} = .092 \text{ in}^3$$

Hence, for both sections

$$A = .44 \times 2 = .88 \text{ in}^2$$

$$Z = .092 \times 2 = .184 \text{ in}^3$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	1.5	Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-2 INCIDENCE CONTROL ARM.7-2-2ATTACHMENT LINK - CONT'D.WELD FILLETS - CONT'D.

$$\text{Bending stress in the fillet} \cdot \frac{4242}{.184} = 23100 \text{ PSI}$$

$$\text{Compression stress in the fillet} \cdot \frac{707}{.88} = 804 \text{ PSI}$$

$$\text{Total max comp. stress} \cdot 23100 + 804 = 23904 \text{ PSI}$$

$$\text{M.S.} \quad \frac{51000}{23904} - 1 = \text{---}$$

1.10

7-2-3BASE PLATE.Shear per $\frac{3}{16}$ bolt:

$$\frac{707}{2} = 353.5 \text{ lb}$$

Tension on aft bolts

$$\frac{4242}{2 \times 1.5} - \frac{707}{4} = 1410 - 176 = 1234 \text{ lb}$$

Strength of AN-3 steel bolts in shear 2070 lb (AN-C-5)

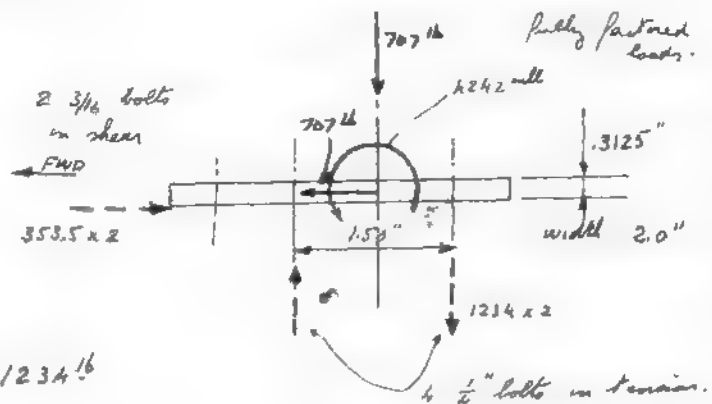
$$\text{M.S.} \quad \frac{2070}{353.5} - 1 = \text{---}$$

4.85

Strength of AN-4 steel bolts in tension 4080 lb (AN-C-5)

$$\text{M.S.} \quad \frac{4080}{1234} - 1 = \text{---}$$

2.3



DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	15.1.1	Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL

7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE

7-2- INCIDENCE CONTROL ARM.

7-2-3

ATTACHMENT LINK - CONT'D

BASE PLATE - CONT'D.

Section in bending is assumed
as shown, length 1.20"
thickness .3125"

Section modulus:

$$\frac{.3125^2 \times 1.2}{6} = .0195 \text{ in}^3$$

Bending Moment: $1234 \times .6 = 740 \text{ inlb.}$

fully factored

Max bending stress: $\frac{740}{.0195} = 38000 \text{ PSI}$

$$M.S. \frac{55000}{38000} - 1 =$$

.44

7-2-4

LOCAL REINFORCEMENT OF THE CONTROL ARM.

Bending moment at section AA.
 $1234 \times .406 = 501 \text{ inlb}$

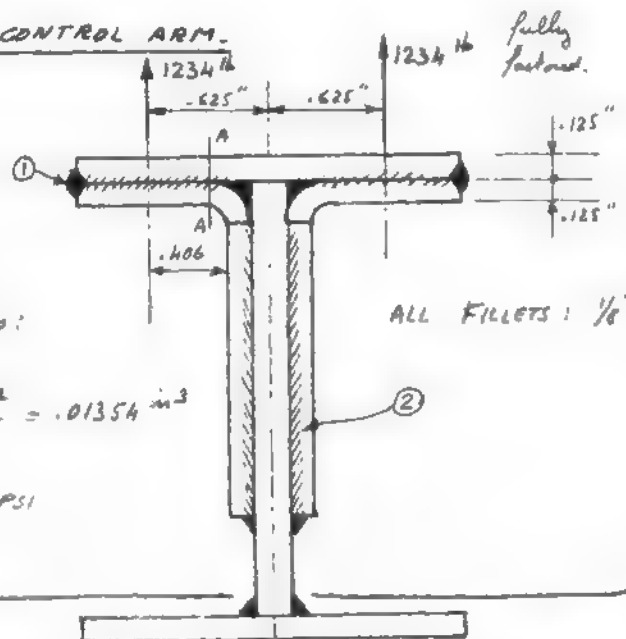
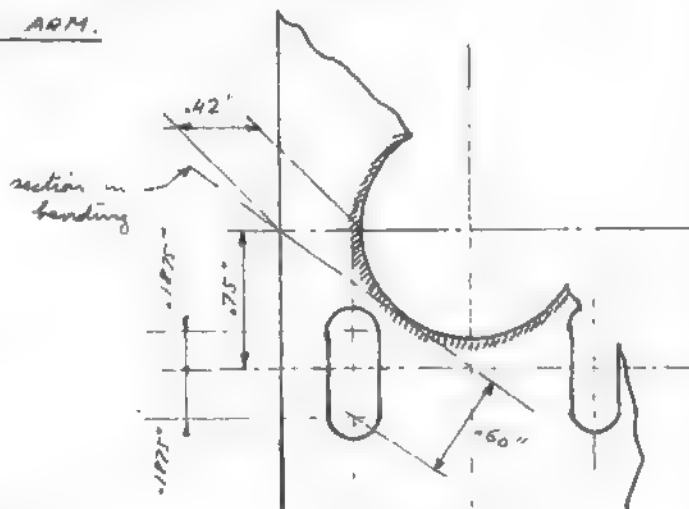
Consider a section in bending
1.30" long, made of 2 .125" plates:

Section modulus: $1.30 \times \frac{.125^2}{6} = .01354 \text{ in}^3$

Bending stress: $\frac{501}{.01354} = 37000 \text{ PSI}$

$$M.S. \frac{55000}{37000} - 1 =$$

.48



WRITTEN BY

G. Jacques

CHECKED BY

1.1.1

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

135

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-2- INCIDENCE CONTROL ARM.7-2-4LOCAL REINFORCEMENTS - CONT'D.SHEAR STRESS IN FILLET N° ①Area of fillet in shear: $.125 \times 2.00 = .25 \text{ in}^2$ Shear on this section: $1.5 \frac{W}{h} = 1.5 \frac{1234}{.25} = 7410 \text{ lb fully fact.}$

Shear stress in the weld.

$$\frac{7410}{.25} = 29600 \text{ PSI}$$

$$\text{M.S. } \frac{32000}{29600} - 1 = \text{---}$$

.083

NOTE The length of weld has been taken as 1.30" along the length + .70" across the backSHEAR STRESS IN FILLET N° ②It is assumed that $\frac{1}{2}$ of the load is introduced in the $\frac{3}{16}$ " web by the upper $\frac{1}{8}$ " cap. The other half through the reinforcing bracket. The effect of moments will be accounted for by assuming that the whole load is introduced through only one oblique side 3" long.

$$\text{Weld area: } 3.0 \times .25 = .75 \text{ in}^2$$

$$\text{fully factored load } \frac{1234}{2} = 617 \text{ lb}$$

$$\text{Shear stress in the weld: } \frac{617}{.75} = 16500 \text{ PSI}$$

$$\text{M.S. } \frac{31000}{16500} - 1 = \text{---}$$

.88

WRITTEN BY

G. Jacques

CHECKED BY

1.1

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

136

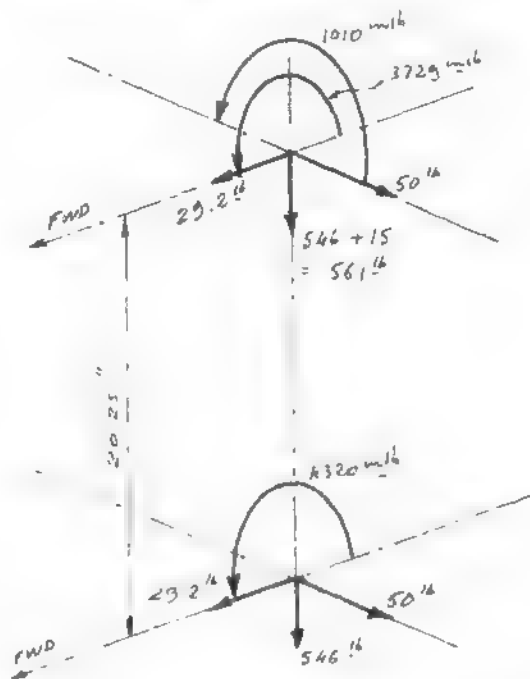
STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE

7-3-

TAPERED SECTION OF VERTICAL ARM.7-3-1 UPPER FLANGE.

Considering the same case as for the gauges (Section 6) and revolving at the upper flange.

-10° Case is the straining case

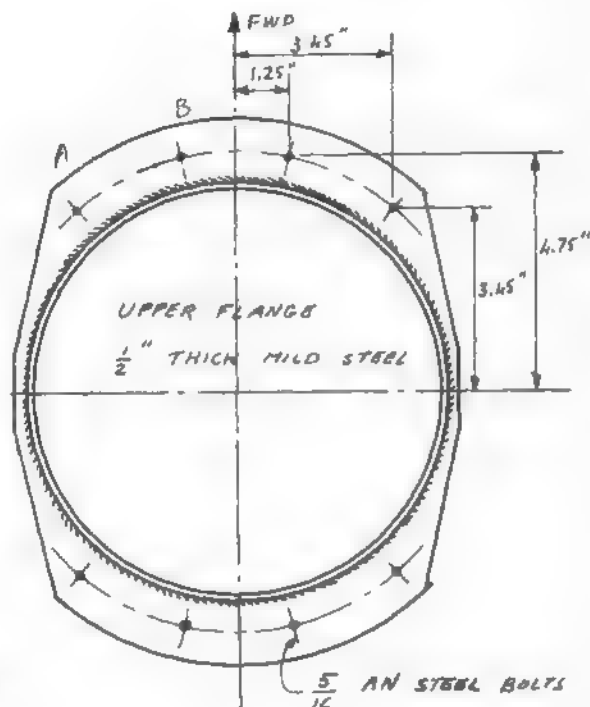
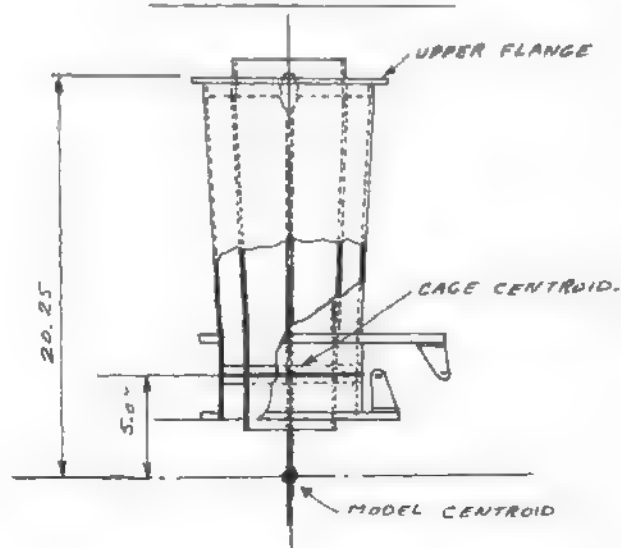


Load per bolt due to Vertical load
 $\frac{561}{8} = 70.2 \text{ lb}$ tension

Total shear on the bolts.

$$\sqrt{29.2^2 + 50^2} = 57 \text{ lb}$$

Shear per bolt $\frac{57}{8} = 7.25 \text{ lb}$ negligible

REMOVABLE SECTION

WRITTEN BY

G. Jaeger

CHECKED BY

1-1

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

137

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE.7-3-TAPERED SECTION OF VERTICAL ARM- CONT'D.7-3-1 UPPER FLANGE

Loads on the bolts due to moments.

The bolts are stressed as clusters under tension & compression

Longitudinal moment

$$\text{Load on bolt B: } \frac{M \times 4.75}{4 \times (4.75^2 + 3.45^2)} = \frac{1.188 M}{34.5} = .0344 M$$

$$= .0344 \times 4320 = 148.5^{16}$$

$$\text{Load on bolt A: } \frac{M \times 3.45}{4 \times (4.75^2 + 3.45^2)} = .0250 M$$

$$= .025 \times 4320 = 108^{16}$$

Transversal moment

$$\text{Load on bolt A: } \frac{M \times 3.45}{4 \times (3.45^2 + 1.25^2)} = \frac{.862 M}{13.46} = .064 M$$

$$= .064 \times 1010 = 63.4^{16}$$

$$\text{Load on bolt B: } \frac{M \times 1.25}{4 \times (3.45^2 + 1.25^2)} = .0232 M$$

$$= .0232 \times 1010 = 23.4^{16}$$

$$\text{Total max. load is on bolt: } A = 108 + 63.4 = 171.4^{16} \text{ tension}$$

$$B = 148.5 + 23.4 = 171.9^{16} \text{ tension}$$

say $172^{16} + 70.2^{16}$ from direct load on previous page

$$\text{Total unfactored load on one } \frac{5}{16} \text{ AN Bolt: } 172 + 70.2 = 242.2^{16}$$

$$\text{With factor of 4: } 242.2 \times 4 = 968.8^{16}$$

Strength of bolt in tension - Ref AN-C-5: 6500^{16}

$$MS \cdot \frac{6500}{968.8} = \dots \dots \dots 5.7$$

WRITTEN BY

G. Jacques

CHECKED BY

1 7

DATE

Sept. 1957

ISSUE

AIRCRAFT

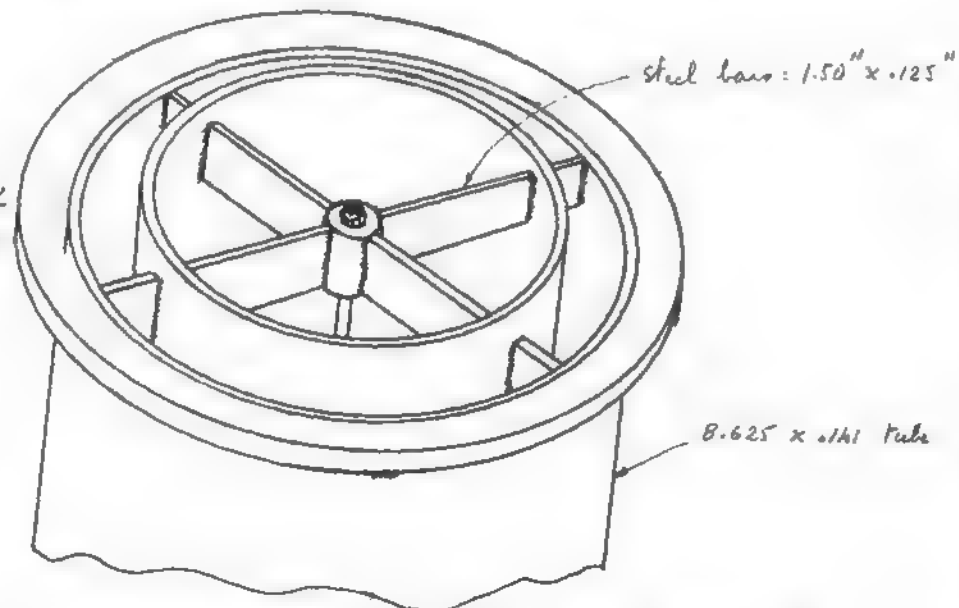
DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

138

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-3- TAPERED SECTION OF VERTICAL ARM.7-3-2CRUCIFORM
BRACKET.MODEL SUSPENSION
ROD ATTACHMENT.

This bracket is stressed to have the same strength than the rod in tension

Strength of the rod: taking strength of equivalent
 $\frac{3}{16}$ AN 808 @ 125000 PSI - Ref. AN-C-5: 2160 $\frac{1}{16}$ say 2200 $\frac{1}{16}$

Each bar of the cruciform bracket takes $\frac{1}{4}$ the load: i.e. 1100 $\frac{1}{16}$

Max bending moment on the bar.

$$\frac{1100 \times 8.484}{4} = 2210 \text{ in-lb}$$

Section modulus of bar:

$$\frac{1.5^2 \times .125}{6} = .0468 \text{ in}^3$$

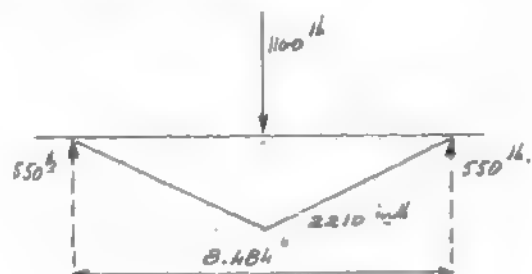
Bending stress:

$$\frac{2210}{.0468} = 47250 \text{ PSI}$$

M.S.

$$\frac{55000}{47250} - 1 = \dots$$

+ .160



WRITTEN BY

G. Jaquemin

CHECKED BY

1.1.1.

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED • 139

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE7-3- TAPERED SECTION OF VERTICAL ARM7-3-2 CRUCIFORM BRACKET.WELD FILLETS ON HUB.

2 $\frac{1}{8}$ " fillets : $.125 \times 1.5$ " taking 2210 in^{lb} bending
+ 550 lb direct shear

Weld section area: $2 \times .125 \times 1.5 = .375 \text{ in}^2$

Direct shear stress: $\frac{550}{.375} = 1470 \text{ PSI}$

Section modulus of weld in shear.

$$2 \times \frac{1.5^2 \times .125}{6} = .0937 \text{ in}^3$$

Shear stress due to bending = $\frac{2210}{.0937} = 26600 \text{ PSI}$

Total max shear stress: $\sqrt{26600^2 + 1470^2} = 26650 \text{ PSI}$

$$M.S. \quad \frac{32000}{26650} - 1 = \text{---} \quad .20$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemont	10/1/57	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE

7-3-

TAPERED SECTION OF VERTICAL ARM-

7-3-3

BRACKETS ATTACHING DRAG GAGE-

Strapping of the lower bracket
will cover the upper bracket

Bending Moment at root
 $152 \times 2.25 = 342 \text{ in-lb (UL)}$

Section on landing: 2 - $\frac{1}{8}$ " steel plates
2 sections: $1.20" \times .25"$

$$I = \frac{2}{6} (1.20^2 \times .25) = .12 \text{ cm}^3$$

Bending stress, fully factored:

$$4 \frac{342}{.12} = 11400 \text{ PSI (ULT.)}$$

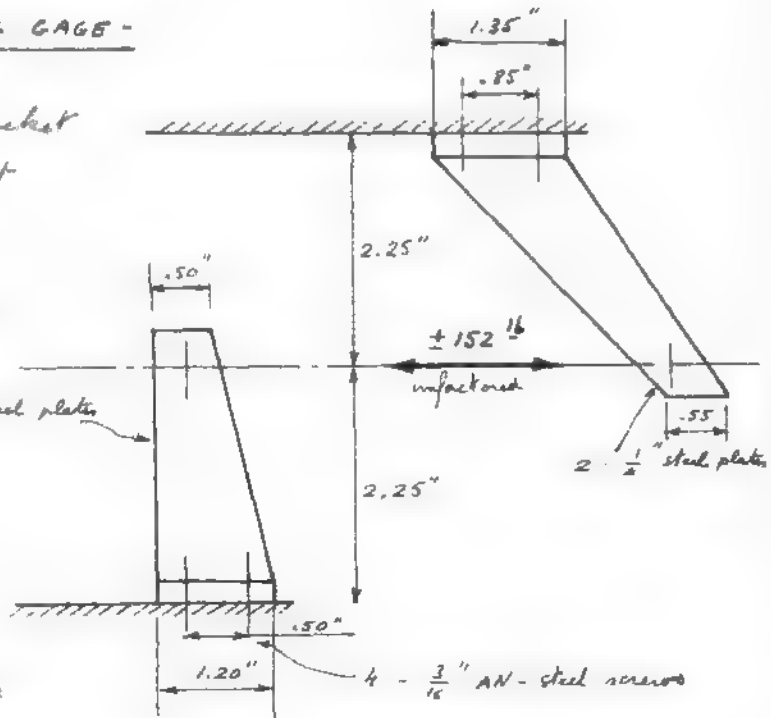
$$M.S.: \frac{55000}{11400} - 1 = 3.82$$

Load on attachment screws

$$\frac{1}{2} 342 \frac{4}{.5} = 1370 \text{ lb ULT.}$$

Strength of $\frac{3}{16}$ " AN screws in tension, Ref. AN-C-5: 2160 lb

$$M.S.: \frac{2160}{1370} - 1 = .57$$



WRITTEN BY

G. Jacques

CHECKED BY

11 1 1 1

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~ DECLASSIFIED

~~SECRET~~

DECLASSIFIED

141

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

7-0 STRESS ANALYSIS - MODEL SUPPORT STRUCTURE

7-3- TAPERED SECTION OF VERTICAL ARM.

7-3-4

MODEL ATTACHMENT.

The load can be assumed to pass entirely into the bolts closest to the gage attachment

Thus, the attachment can be covered by considering the two bolts taking the load of the 800^{lb} gage.

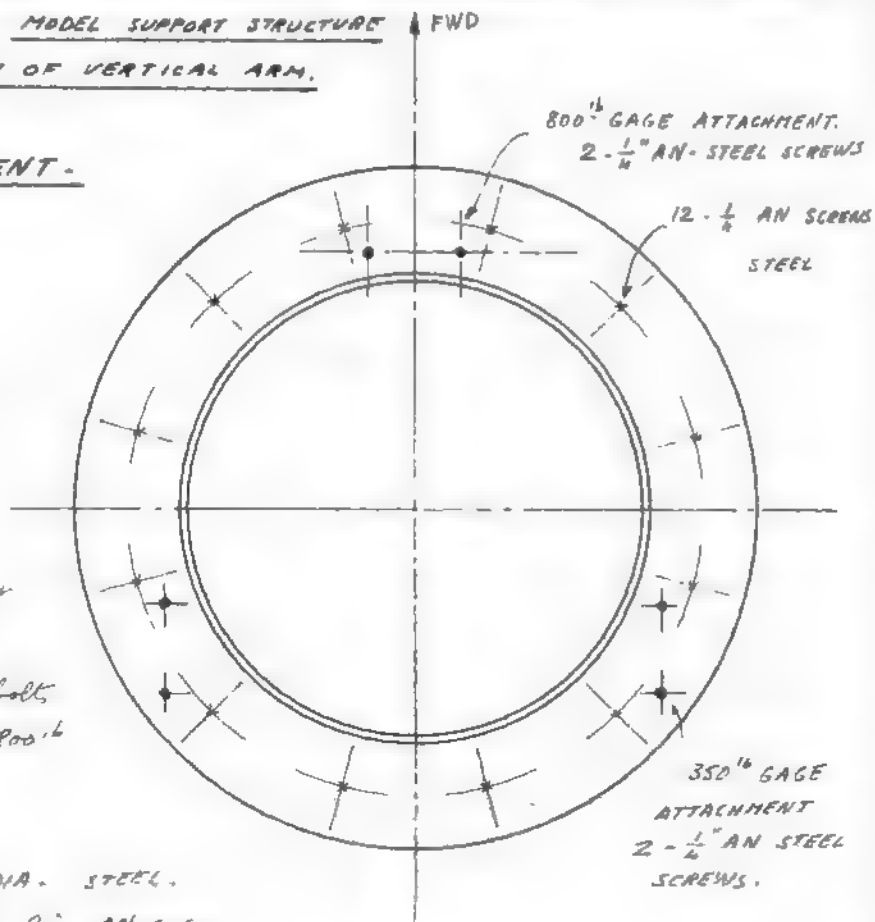
2 AN-SCREWS - $\frac{1}{4}$ " DIA. STEEL.

MAX Tensile Strength R_t AN-C-5

$$4080 \times 2 = 8160^{lb}$$

$$\text{Factored Load: } 800 \times 4 = 3200^{lb}$$

$$M.S. \quad \frac{8160}{3200} - 1 = \text{-----} \quad 1.55$$



DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques		Sept. 1957		

~~SECRET~~

DECLASSIFIED

AVRO/SPG/TR 112

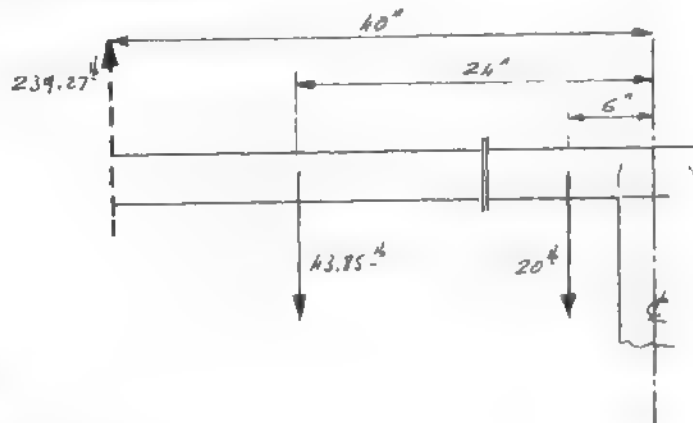
~~SECRET~~

142

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-1HORIZONTAL TUBE.B-1-1 BENDING.Section properties of the tube:

Size: 10" x .141"

ID = 9.718"

Sectional area: $A = \frac{\pi}{4} (10^2 - 9.718^2) = 3.53 \text{ in}^2$ Moment of inertia: $I = \frac{\pi}{64} (10^4 - 9.718^4) = 54 \text{ in}^4$ Section modulus: $Z = \frac{\pi}{32} \frac{10^4 - 9.718^4}{10} = 10.8 \text{ in}^3$ Stresses under static load + airloads:Bending moment under static loads:Bending moment at \bar{x}

$$M = (239.27 \times 40) - (43.85 \times 24) - (20 \times 6) = 9560 - 1052 - 120 = 8388 \text{ in-lb.}$$

DECLASSIFIED

WRITTEN BY

G. Jaques

CHECKED BY

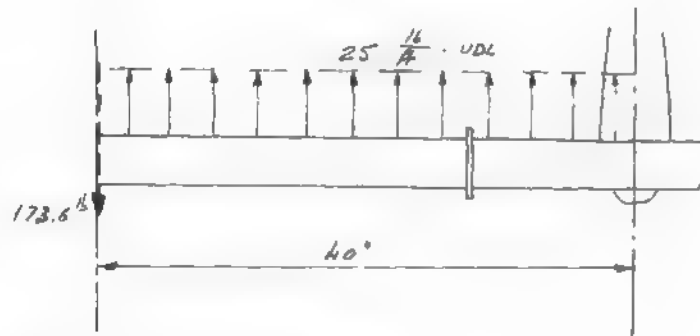
L. J. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRING.B-1 HORIZONTAL TUBEB-1-1 BENDING.Bending moment
under airload

Bending moment

$$M = 173.6 \times 40 - 25 \frac{40^2}{2 \times 12} = 6940 - 1666 = 5274 \text{ in}^2.$$

Total Bending moment on the section.

$$M_T = \sqrt{8388^2 + 5274^2} = 9870 \text{ in}^2 \text{ (LIN)}$$

Bending stress: max.

$$\frac{4}{10.8} \frac{9870}{10.8} = 3660 \text{ PSI (UCT)}$$

$$M.S. \quad \frac{55000}{3660} - 1 = \text{---} > 10$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques	L. J. ...	Sept. 1957		

DECLASSIFIED

~~SECRET~~

AVRO/SPG/TR 112

144

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-1 HORIZONTAL TUBEB-1-2FLANGES ON 10" TUBE.FLANGE LOADING.

STATIC LOADS: VERTICAL

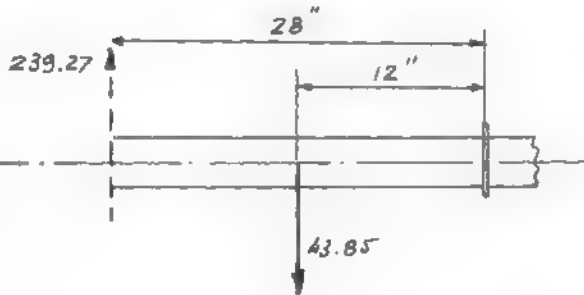
Bending moment at flange section: —

$$(239.27 \times 28) - (43.85 \times 12) =$$

$$6700 - 527 = 6173 \text{ in-lb unfactored}$$

Shear force:

$$239.27 - 43.85 = 195.42 \text{ lb unfactored}$$



AIRLOADS HORIZONTAL

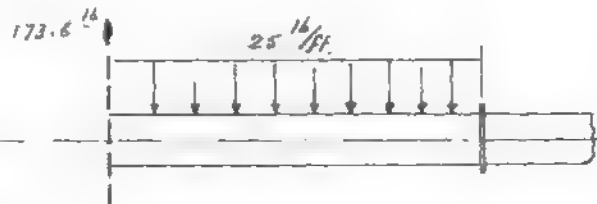
Bending moment at flange section —

$$(173.6 \times 28) - 25 \frac{28^2}{12 \times 2} =$$

$$4860 - 815 = 4045 \text{ in-lb unfactored}$$

Shear force.

$$173.6 - 25 \frac{28}{12} = 173.6 - 58.3 = 115.3 \text{ lb unfactored.}$$



TOTAL BENDING MOMENT:

$$\sqrt{6173^2 + 4045^2} = 7380 \text{ in-lb unfactored.}$$

Total shear force

$$\sqrt{195.42^2 + 115.3^2} = 226 \text{ lb unfactored}$$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

J. T. " "

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

AVRO/SPG/TR 112

145

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-1 HORIZONTAL TUBEB-1-2.FLANGES ON 10" TUBE -

Bolt strength in tension

Ref AN-C-5.

$$AN-5 - \frac{5}{16} \text{ DIA. : } 8500^{16}$$

Bolt strength in shear

$$AN-5 - \frac{5}{16} \text{ DIA : } 5750^{16}$$

Distribution of tensions due to bending in the bolt cluster

$$F_b = \frac{M \frac{d_f}{2}}{\sum d^2}$$

Considering only the bolt having greatest tension

$$\sum d^2 = 5.6^2 [2 + 4 \sin^2 60^\circ + 4 \sin^2 30^\circ]$$

$$\therefore F = \frac{M}{5.6 [2 + 4 \sin^2 60^\circ + 4 \sin^2 30^\circ]} \quad \text{for } d_f = 5.6. \quad F = .0298 M$$

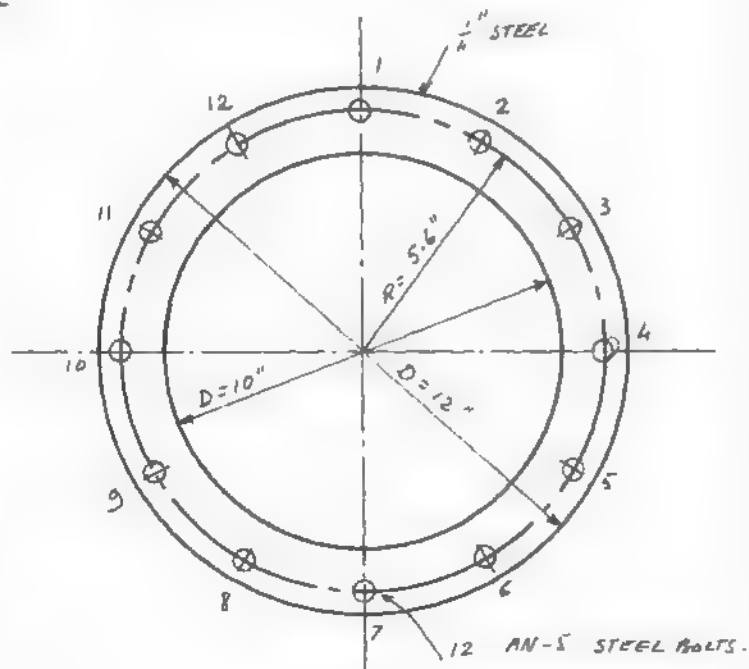
$$\therefore F = 7380 \times .0298 = 220^{16} \quad \text{unfactored}$$

$$\text{Shear per bolt: } \frac{226}{12} = 18.85^{16} \quad \text{unfactored.}$$

Such low shear does not practically reduce the tensile strength

$$\therefore \quad H.S \quad \frac{6500}{4 \times 220} - 1 = \text{---}$$

6.4



DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

1

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~ DECLASSIFIEDSTRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-1 HORIZONTAL TUBEB-1-2FLANGES ON 10" TUBE.WELDS.Assume max load on bolt to be taken by 2" of $\frac{1}{4}$ " weld.Weld area: $2 \times .25 = .50 \text{ in}^2$

Allowable U.S.S. of weld metal 32000 PSI (Ref. AN-C-5)

Weld stress: $\frac{220}{.50} = 440 \text{ PSI}$ unfactored

$$M.S. \quad \frac{32000}{4 \times 440} - 1 = \text{-----} > 10$$

WRITTEN BY

G. Jacquemine

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

147

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRING.B-2 VERTICAL FAIRINGB-2-1 - LOADING.

MAT. AL. ALLOY. .064".

AREA:

$$(3.11 \times 3.18) - \left(\frac{1.80 \times 1.042}{2} \right) =$$

$$9.88 - .94 = 8.94 \text{ ft}^2$$

Side load on fairing.

$$C_d @ 5^\circ \approx .50$$

Total load at 30 g.

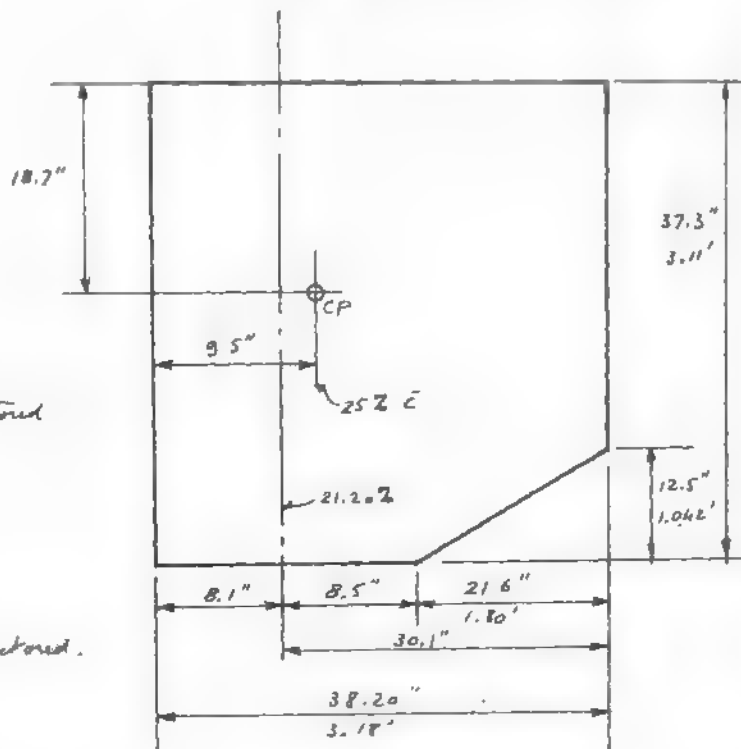
$$.50 \times 8.94 \times 30 = 134 \frac{1}{2} \text{ unfactored}$$

Aft load on fairing:

$$C_d @ 5^\circ \approx .30$$

Total load at 30 g:

$$.30 \times 8.94 \times 30 = 80.5 \frac{1}{2} \text{ unfactored.}$$

Fully factored loads: ($n=4$)

$$\text{Side load: } 134 \times 4 = 536 \frac{1}{2}$$

$$\text{Drag load: } 80.5 \times 4 = 322 \frac{1}{2}$$

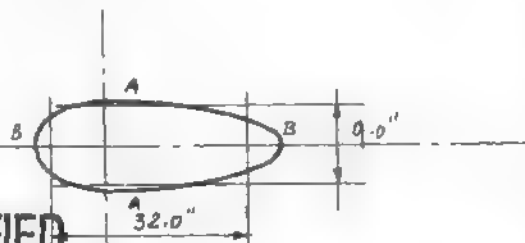
Assuming CP at 25% chord and $\frac{1}{2}$ span

Moments at root

$$\text{SIDE MOMENT: } 18.7 \times 536 = 10000 \text{ in/lb}$$

$$\text{AFT MOMENT: } 18.7 \times 322 = 6020 \text{ in/lb}$$

These moments are considered
as taken by groups of screws
as shown on sketch.



DECLASSIFIED

WRITTEN BY

G. Jaquar

CHECKED BY

J. J. J.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

148

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.B-0 STRESS ANALYSIS - FAIRING.B-2 VERTICAL FAIRING.B-2-2 - VERTICAL FAIRING ATTACHMENT.

Loads on groups of rivets.

$$\text{RIVETS AA: } \frac{10000}{9} = 1120 \text{ lb}$$

$$\text{RIVETS BB: } \frac{6020}{32} = 201 \text{ lb}$$

Bearing strength of -AD $\frac{5}{32}$ " rivets on .064" 35- $\frac{1}{2}$ H al alloy

In the absence of exact data regarding the max. allowable bearing stress on 35- $\frac{1}{2}$ H, this stress is taken as being twice the UTS by comparison with other similar soft al. all.

$$\text{UTS} = 20000 \text{ PSI (Ref. Engineering Manual)}$$

$$\therefore \text{UBS} = 2 \times 20000 = 40000 \text{ PSI.}$$

Bearing strength on .064 (AN-C-5) for $\frac{e}{D} = 2.0$

$$1020 \frac{40000}{100000} = 408 \text{ lb}$$

The 1120 lb load is to be taken by rivets at 2.00" pitch. and a length of: 12" will be interested to take this load. Hence 6 rivets having a total strength of: $6 \times 408 = 2448 \text{ lb}$

$$\text{M.S. } \frac{2448}{1120} - 1 = \text{---}$$

1.19

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquart	i	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

149

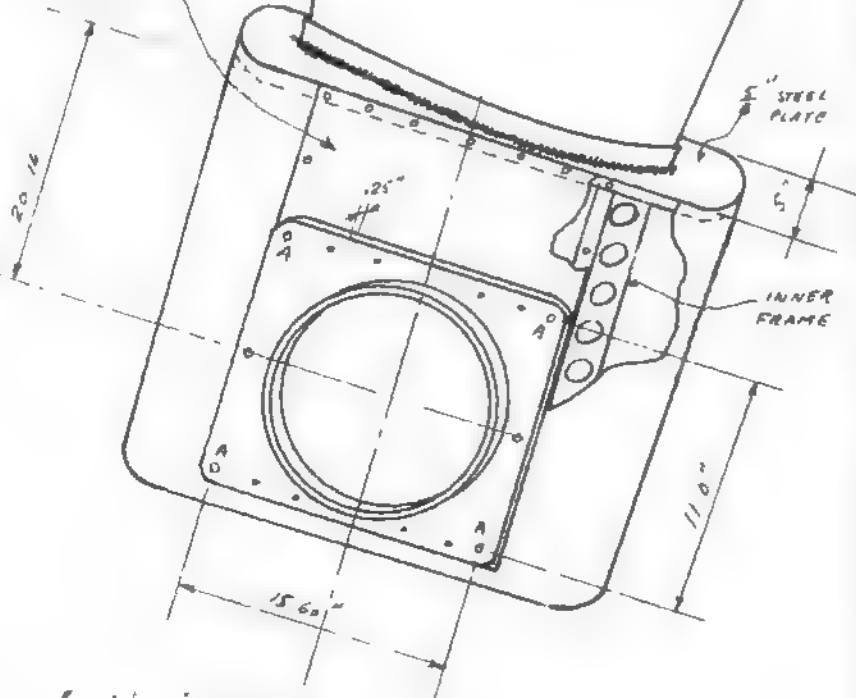
STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-3 ATTACHMENT TO STRUT FAIRINGSB-3-1 LOADING.

NOTE Both "A" join
flanges on both sides
and are blocked tight
on a tube spacer

Flanges offset to load
carrying plate:

inner flange .95"
outer flange 1.50"

.071" STEEL
LOAD CARRYING
PLATE

APPLIED LOADS.

On the inner side where loading is max

240^{lb} Vertically down.

174^{lb} Horizontally aft.

80.5^{lb} Side load due to Vertical fairing

} unfactored

NOTE. The side load is taken on the Port side only.

FULLY FACTORED APPLIED LOADS

$\lambda = 4.0$

960^{lb} Vertically down

696^{lb} Horizontally aft.

322^{lb} Side load

NOTE. - Loads on the outer side are smaller than on the inner side
- As a cover up stringing, only loads on the inner side will be
considered

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. J. Jorgensen	1	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

149

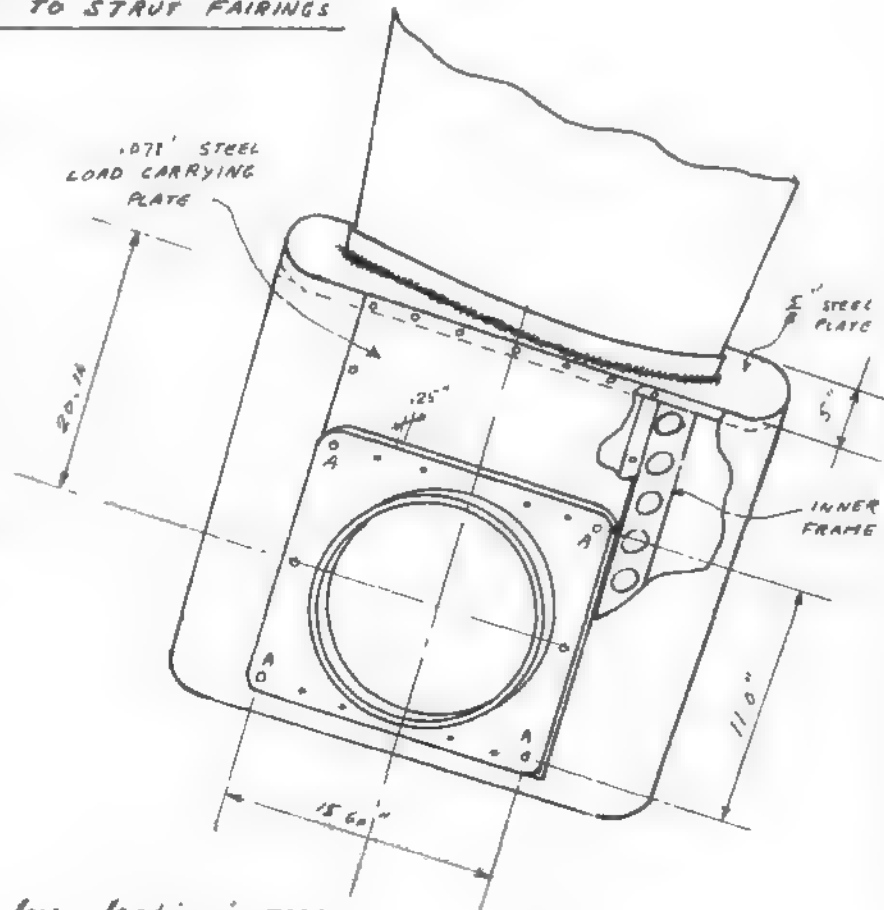
STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-3 ATTACHMENT TO STAVE FAIRINGSB-3-1 LOADING.

NOTE: Bolt "A" join
flange on both sides
and are blocked tight
on a tube spacer

Flange offset to load
carrying plate:

inner flange .95"

outer flange 1.50"

APPLIED LOADS:

On the inner side where loading is max

240^{lb} Vertically down.

174^{lb} Horizontally aft.

80.5^{lb} Side load due to Vertical fairing

} unfactored.

NOTE. The side load is taken on the Port side only

FULLY FACTORED APPLIED LOADS

$n = 4.0$

960^{lb} Vertically down

696^{lb} Horizontally aft.

322^{lb} Side load

NOTE: - Loads on the outer side are smaller than on the inner side
- As a cover up stressing, only load on the inner side will be considered.

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

J. J.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-3 ATTACHMENT TO STRUT FAIRINGB-3-2LOAD CARRYING STEEL PLATE-

Max. Vertical load

$$960 + 322 \frac{20.14}{5} = 960 + 1300 = 2260 \text{ lb}$$

Load per bolt due to 2260 lb

$$\frac{2260}{7} = 323 \text{ lb}$$

Load per bolt due to side load.

$$\frac{696}{7} = 99.4 \text{ lb}$$

Load on bolts due to moment of side load:

$$\text{Moment: } 696 \times 20.14 = 14000 \text{ in-lb}$$

Load on bolt 1

$$14000 \frac{7.8}{(7.8^2 + 5.2^2 + 2.6^2)2} = 14000 \frac{7.8}{189.6} = 73.9 \times 7.8 = 577 \text{ lb Vertical}$$

$$\text{Load on bolt 2 : } 73.9 \times 5.2 = 384 \text{ lb Vertical}$$

$$\text{Load on bolt 3 : } 73.9 \times 2.6 = 192 \text{ lb Vertical}$$

$$\text{Total load on bolt 1 : } \sqrt{(323 + 577)^2 + 99.4^2} = 905 \text{ lb}$$

Strength of bolt in shear Ref AN-C-5 2126 lb

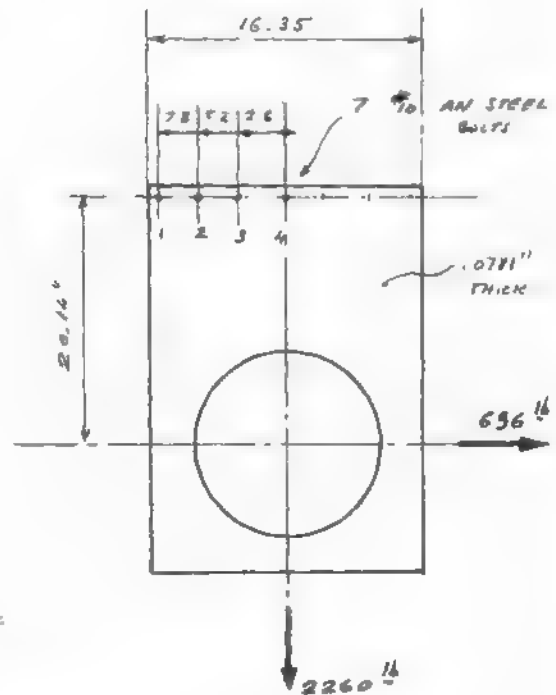
$$M.S. \frac{2126}{905} - 1 = 1.34$$

Steel plate: Strength of a 1" strip under tension at UTS 55000 PSI

$$1" \times .0781 \times 55000 = 4300 \text{ lb}$$

Assuming a 1" strip carries the load to bolt 1.

$$M.S. \frac{4300}{905} - 1 = 3.75$$



WRITTEN BY

G. Jaeger

CHECKED BY

1 f

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

151

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-3 ATTACHMENT TO STRUT FAIRINGSB-3-3.BEARING FLANGES

Load per bolt due to

322^{lb} tension:

$$\frac{322}{6} = 53.7^{lb}$$

Tension on upper bolts
due to moment of
vertical load.

$$960 \frac{1}{11.0} \times \frac{1}{2} = 43.6^{lb}$$

Tension on side bolts
due to moment of
horizontal load

$$696 \frac{1}{15.6} \times \frac{1}{3} = 14.9^{lb}$$

$$\text{Max tension on one bolt: } 53.7 + 43.6 + 14.9 = 112.2^{lb}$$

Total shear strength of the assembly. (Bearing not critical! Ref AN-C-5)
 $(6 \times 3680) + (14 \times 862) = 22160 + 12068 = 34228^{lb}$

$$\text{Shear per bolt: } V \frac{3680}{34228} = .108 V$$

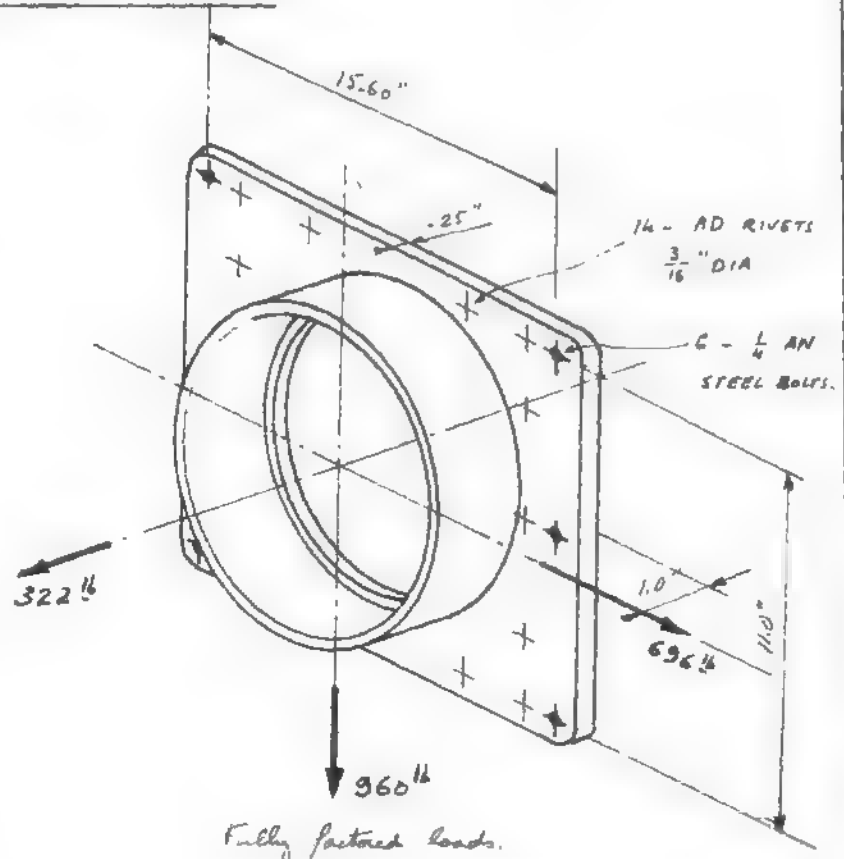
$$\text{Total shear force: } \sqrt{960^2 + 696^2} = 1182^{lb}$$

$$\text{Shear per bolt: } 1.182 \times .108 = 128^{lb}$$

Strength of $\frac{1}{4}$ AN steel bolt. (AN-C-5) Tension: 4080^{lb}
 Shear: 3680

M.S.

>10



WRITTEN BY

G. Jacques

CHECKED BY

L. J. ...

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODELB-0 STRESS ANALYSIS - FAIRINGB-3 ATTACHMENT TO STRUT FAIRINGS.B-3-3.BEARING FLANGES - CONT'D.FLANGE IN BENDING UNDER LOAD OF CORNER BOLTBolt tension: 112.3^{16} Moment arm 4.00"Section in bending: $.25" \times 8"$ Section modulus. $.25^2 \frac{8}{6} = .0832 \text{ in}^3$ Bending stress: $\frac{112.2 \times 4.0}{.0832} = 5400 \text{ PSI}$ M.S. $\frac{55000}{5400} - 1 =$

7.2

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacqueniz	112.3 15 112	Sept. 1957		

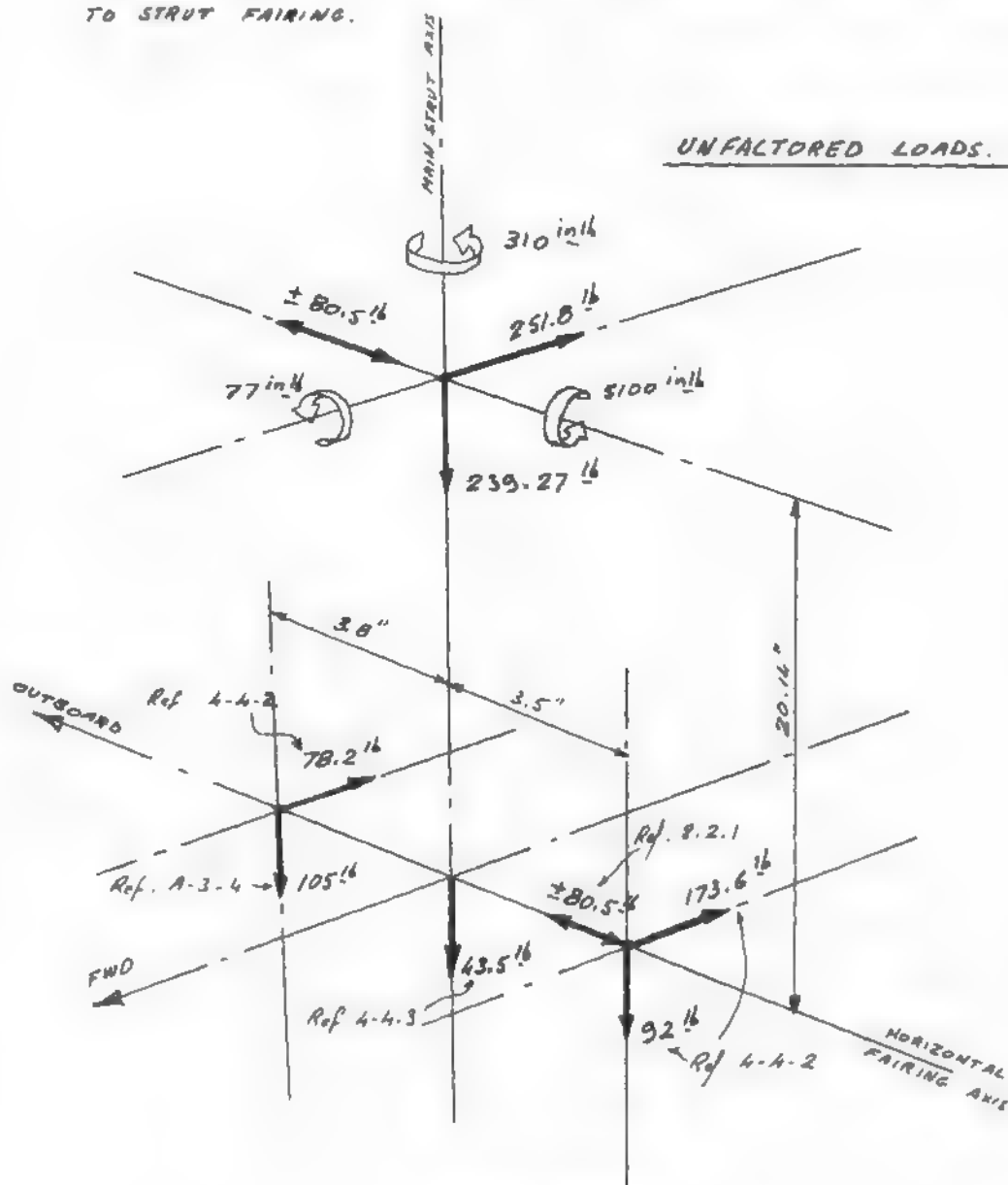
~~SECRET~~

~~SECRET~~

DECLASSIFIED 153

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.B-0 STRESS ANALYSIS - FAIRING.B-3 ATTACHMENT TO STRUT FAIRING.B-3-4 LOADS RESOLVED AT ATTACHMENT TO STRUT FAIRING.

LOADING REQUIRED FOR DESIGN BY WPAFB OF ATTACHMENT
 PLANCE ITEM 420 SN 30290 - FAIRING ASS'y ATTACHMENT
 TO STRUT FAIRING.



DECLASSIFIED

WRITTEN BY

G. Jacquemin

CHECKED BY

A. L. G. J. J.

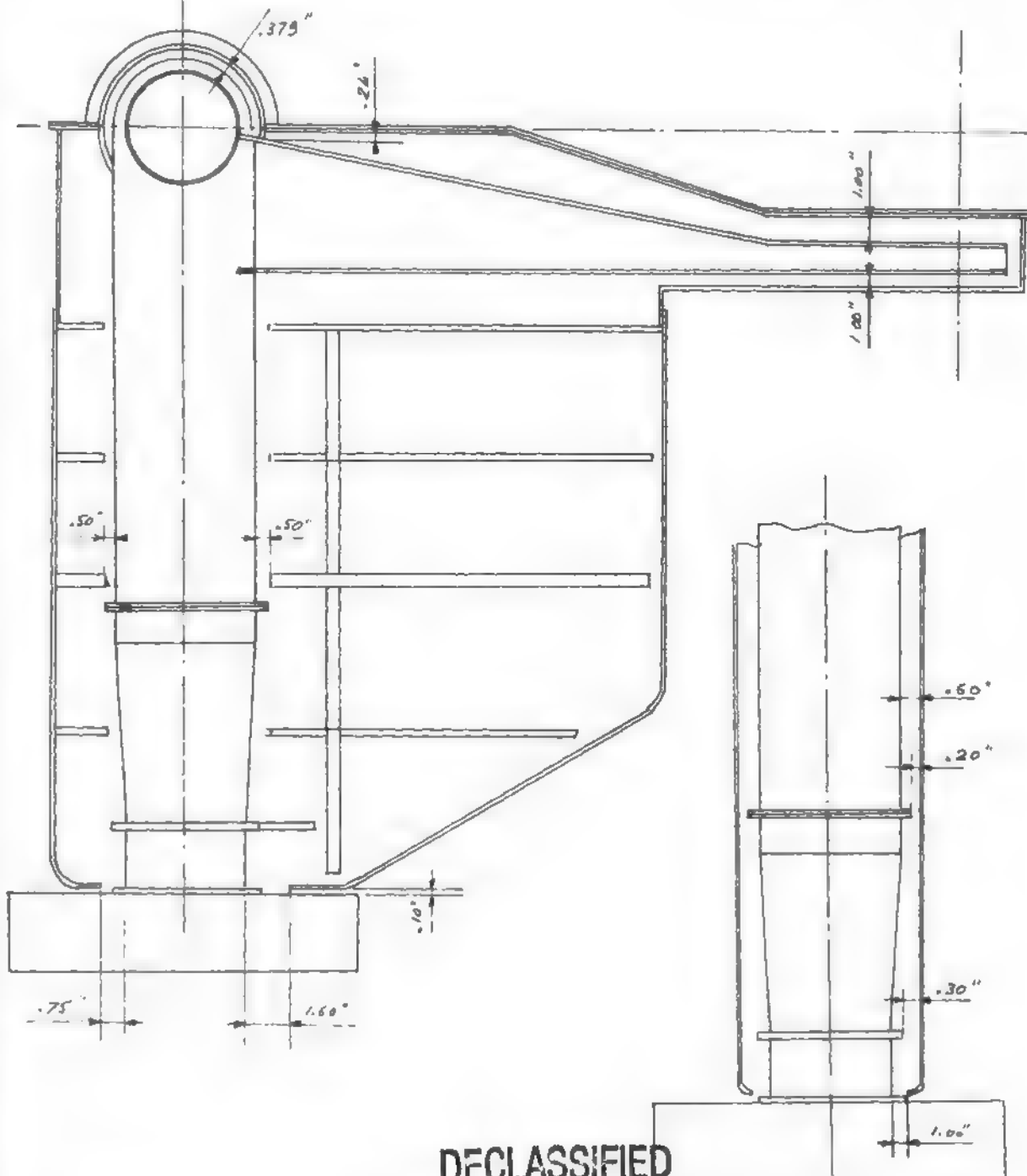
DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.9-0DEFLECTIONS.9-1NOMINAL MINIMUM CLEARANCES -FIG - 11

DECLASSIFIED

WRITTEN BY

G. Jacquemin

CHECKED BY

11/1/10

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

155

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL3-0DEFLECTIONS3-2GAGE SECTION DEFLECTION.

The gages are designed as per report. AVRO/SPG/TR-87.

GAGE A - 800^{lb}

OUTER DIA. 3.00"

WIDTH $b = .625"$

Operating Stress: 40000 PSI

Thickness: $t = .220$

$$\frac{D}{t} = 13.63$$

GAGE B & C - 350^{lb}

OUTER DIA. 3.00"

WIDTH $b = .500"$

Operating Stress: 40000 PSI

Thickness: $t = .165$

$$\frac{D}{t} = 18.20$$

GAGE DEFLECTION AND ROTATION OF MODEL.

$$\text{GAGE A: } \int_{800} = .0213"$$

$$\therefore \int_1 = \frac{.0213}{800} = 2.66 \times 10^{-5} \frac{in}{lb}$$

$$\text{GAGE B \& C: } \int_{350} = .0260"$$

$$\therefore \int_1 = \frac{.0260}{350} = 7.42 \times 10^{-5} \frac{in}{lb}$$

ROTATION OF MODEL UNDER 100^{lb} APPLIED AT CENTER.

$$\text{Load on gage A: } 100 \times .350 = 35^{lb}$$

$$\text{Load on gage B \& C: } 100 \times .325 = 32.5^{lb}$$

$$\text{Gage A deflection: } 2.66 \times 35 \times 10^{-5} = .000932"$$

$$\text{Gage B deflection: } 7.42 \times 32.5 \times 10^{-5} = .00241"$$

$$\text{deflection angle of the model: } \frac{.00241 - .000932}{6.3} = .000235 \text{ rad.}$$

$$\text{Rotation of the model in degrees: } 57.3 \times .000235 = .0134^\circ \text{ per } 100^{lb}$$

DECLASSIFIED

WRITTEN BY

G. Jaeger

CHECKED BY

J. A. ...

DATE

Sept. 1957

ISSUE

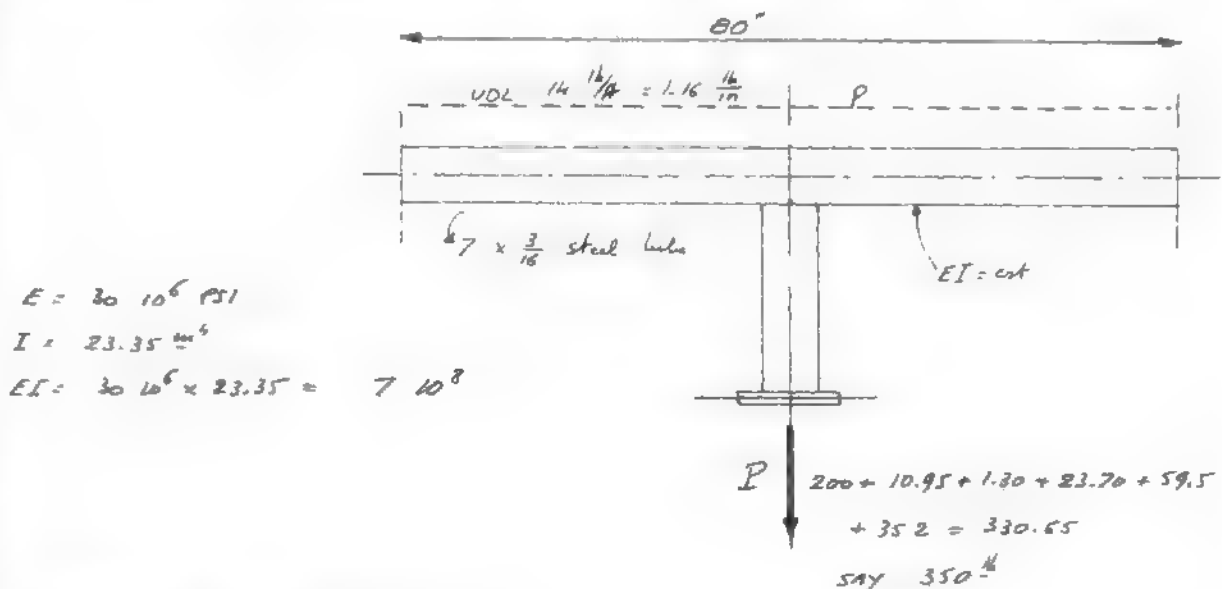
AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

156

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL9-0 DEFLECTIONS9-3 DEFLECTION OF MODEL SUPPORT STRUCTURE9-3-1DEFLECTION OF MODEL MOUNT UNDER STATIC LOAD. 1 - VERTICAL.DEFLECTION UNDER UDL: P .

$$\delta_1 = \frac{5}{384} P \frac{l^4}{EI} = \frac{.01302 \times 80^4}{7 \times 10^8} P = .00768 P = 7.68 \times 10^{-3} P$$

DEFLECTION UNDER CONCENTRATED LOAD P

$$\delta_2 = \frac{Pl^3}{48EI} = P \frac{80^3}{48 \times 7 \times 10^8} = 1.525 \times 10^{-5} P$$

$$\text{TOTAL DEFLECTION: } \delta = \delta_1 + \delta_2 = 7.68 \times 10^{-2} P + 1.525 \times 10^{-5} P$$

$$\delta = 7.68 \times 10^{-2} \times 1.16 + 1.525 \times 10^{-5} \times 350 = .0089 + .00534 =$$

$$= .01424 \text{ in}$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. J. J. J.		Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

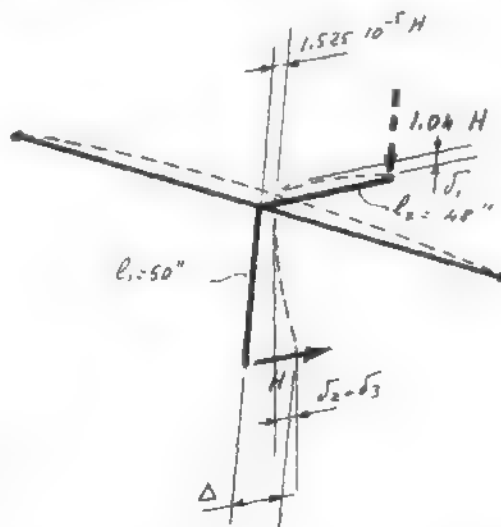
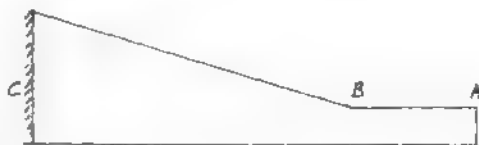
9-0 DEFLECTIONS

9-3 DEFLECTION OF MODEL SUPPORT STRUCTURE

9-3-2

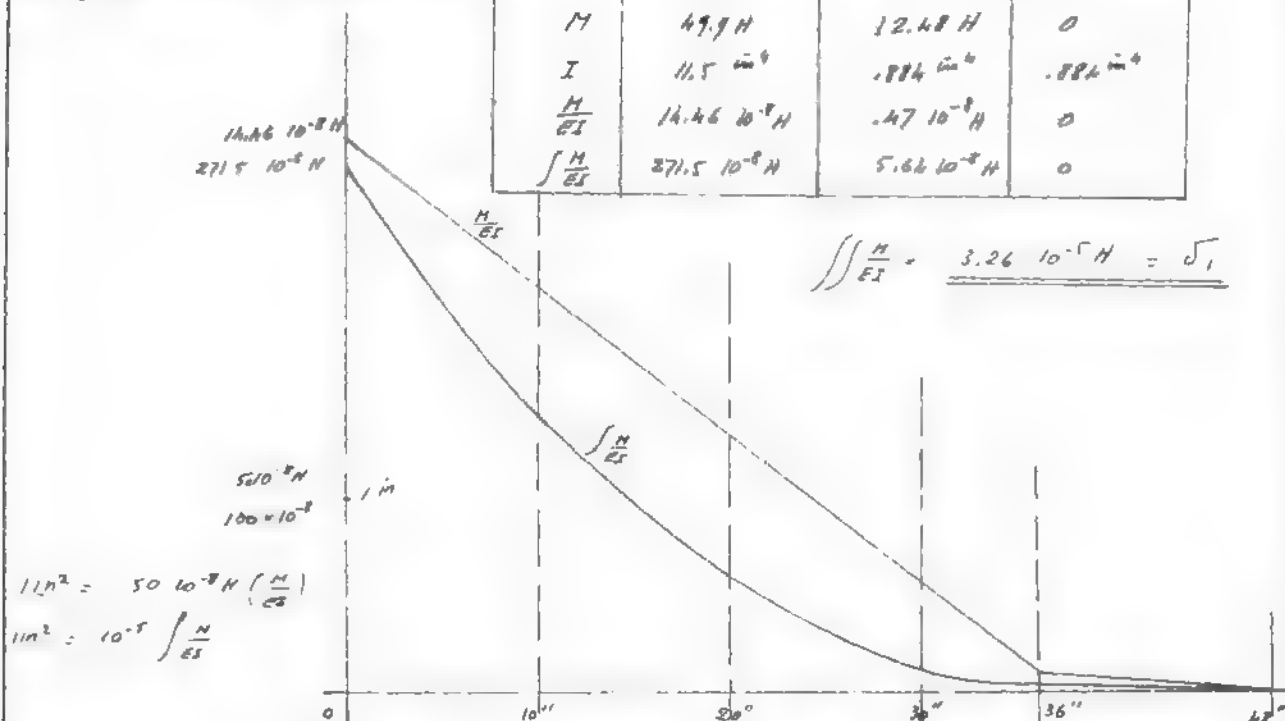
DEFLECTION OF MODEL MOUNT UNDER A DRAG LOAD AT MODEL CENTER.
HORIZONTAL.

The incidence control arm has a vanasse moment of inertia along its length



Reflection Calculated
by integrating twice $\frac{17}{25}$
along the length of the beam

	C	B	A
ℓ	48	12	0
M	49.9 H	12.48 H	0
I	11.5 m^4	.884 m^4	.884 m^4
$\frac{M}{ES}$	14.46 10^{-8} H	.47 10^{-8} H	0
$\int \frac{M}{ES}$	271.5 10^{-8} H	5.66 10^{-8} H	0



WRITTEN BY

G. Jaegeri

CHECKED BY

1-2-4

DATE _____

DECLA
Sept. 19 1977

ISSUE

AIRCRAFT

DECLASSIFIED

AYRO EA 3710

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL -9-0DEFLECTIONS9-3DEFLECTION OF MODEL SUPPORT STRUCTURE-9-3-2DEFLECTION OF MODEL MOUNT UNDER A DRAG LOAD AT MODEL CENTER - CONT'D.
HORIZONTAL.

$$\delta_1 = 3.26 \cdot 10^{-5} H \quad \therefore \delta_2 = 3.26 \cdot 10^{-5} \frac{50}{48} H = 3.39 \cdot 10^{-5} H$$

BENDING DEFLECTION OF VERTICAL MEMBER

$$\delta_3 = \frac{H l^3}{3EI} \quad \text{where } l = 50" \text{ \& } I = 33.75 \text{ in}^4$$

$$\delta_3 = H \frac{50^3}{3 \times 30 \cdot 10^6 \times 33.75} = 4.12 \cdot 10^{-5} H$$

TOTAL HORIZONTAL DEFLECTION OF THE MODEL CENTER:

$$1.525 \cdot 10^{-5} H + 3.39 \cdot 10^{-5} H + 4.12 \cdot 10^{-5} H = 9.035 \cdot 10^{-5} H$$

$$\text{SAY: } \underline{\underline{10^{-4} H = \Delta}}$$

Thus, for a drag load of $\underline{200}^{\text{lb}}$, the deflection is

$$2 \cdot 10^{-4+2} = 2 \cdot 10^{-2} = \underline{\underline{.020''}}$$

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

1.1.1.1

DATE

Sept. 1957

ISSUE

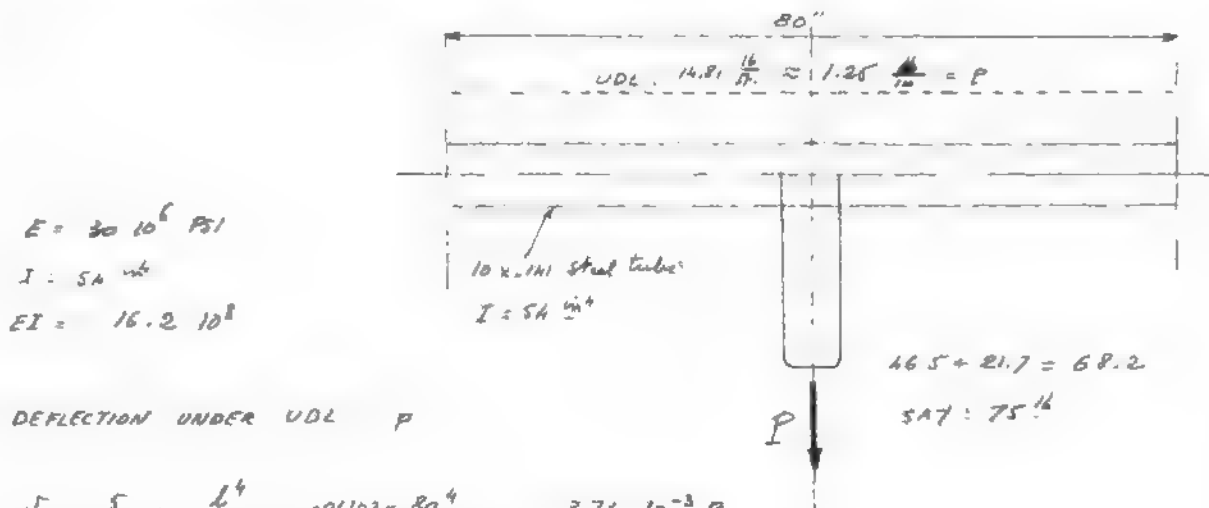
AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

159

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.9.0 DEFLECTIONS9-4 DEFLECTION OF FAIRING9-4-1DEFLECTION OF FAIRING TUBE UNDER STATIC LOAD. VERTICAL

$$E = 30 \cdot 10^6 \text{ PSI}$$

$$I = 54 \text{ in}^4$$

$$EI = 16.2 \cdot 10^8$$

DEFLECTION UNDER UDL P

$$\delta_1 = \frac{5}{384} P \frac{L^4}{EI} = \frac{.01302 \times 80^4}{16.2 \cdot 10^8} P = 3.71 \cdot 10^{-3} P$$

DEFLECTION UNDER CONCENTRATED LOAD P

$$\delta_2 = \frac{P L^3}{48 EI} = P \frac{80^3}{48 \times 16.2 \cdot 10^8} = 7.34 \cdot 10^{-5} P$$

$$\text{TOTAL DEFLECTION: } \delta = \delta_1 + \delta_2 = 3.71 \cdot 10^{-3} P + 7.34 \cdot 10^{-5} P$$

$$\delta = 3.71 \cdot 10^{-3} \times 1.25 + 7.34 \cdot 10^{-5} \times 75 = .00468 + .000558$$

$$= .005238 \text{ in}$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger		Sept. 1957		

~~SECRET~~

~~SECRET~~STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL9-0 DEFLECTIONS9-4 DEFLECTION OF FAIRING9-4.2.DEFLECTION OF FAIRING TUBE UNDER AIR LOAD. - HORIZONTAL.

The characteristics are similar to the static load case
with a UCL: $25 \frac{lb}{ft}$; $2.08 \frac{lb}{in}$ say, $2.10 \frac{lb}{in}$
and a drag load of $80.5 \frac{lb}{ft}$ from the fairing of the Vertical arm

Hence. Deflection

$$\delta = 5.71 \cdot 10^{-3} \times 2.10 + 7.34 \cdot 10^{-6} \times 80.5 =$$

$$7.79 \cdot 10^{-3} + 5.92 \cdot 10^{-4} = \underline{\underline{.008382''}}$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	1st	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

161

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.9-0 DEFLECTIONS9-5. CONCLUSION.

In view of the clearance provided the deflection under load of this structure is insignificant.

We can see that the smallest clearance is .10" just above the surface of the model. In the static condition, the model mount sinks .0142" while the fairing sinks .0052" hence the relative motion is:

$.0142 - .0052 = .0090"$. Thus approximately 10% of the clearance provided.

Considering the effect of model lift, a critical case is the -10° case with a total down load of 546 lb i.e. an extra 346 lb on the static case which would induce an additional deflection: $1.525 \times 10^{-5} \times 346 = .00527"$

Then, the relative motion becomes:

$.009 + .00527 = .01427"$ about 14% of the clearance provided.

All other clearances are larger hence less critical than the above.

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger	10/1	Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED 162

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.10-0 CALIBRATION10-0-1 INTRODUCTION

In this section, the symbols and sign convention used in the rest of the report have been replaced by those of report AVRO/SPG/TR 98 "Test Specifications for $\frac{1}{12}$ scale Hovering and Transition Model".

In 10-1-1, the basic gage equations from section 6-3 have been repeated using the new symbols. It should be noted that the equations apply only when the model suspension rod is engaged. When the rod is disengaged, the load distribution on the gages changes to that calculated on 6-1 3 page.

The basic equations from 10-1-1 can be simplified for calibration purposes by noting that:

- 1/ angle $\alpha = 0$
- 2/ Pressure and suction are off

The reduced equations are given in 10-1-2

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaques		Sept. 1957		

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL10-0 CALIBRATION10-1 GAGE EQUATIONS FOR CALIBRATION.10-1-1 BASIC GAGE EQUATION.

REF SECTION 6-1.3 & 6.3

GAGE	A	B	C	D	
WEIGHT	$.196 W(1-\cos \alpha)$	$.182 W(1-\cos \alpha)$	$.182 W(1-\cos \alpha)$	$-W \sin \alpha$	
PRESSURE	$4.47(P_s - P_a)$	$4.03(P_s - P_a)$	$4.03(P_s - P_a)$	0	$A_p = 22.6 \text{ in}^2$
SUCTION	$2.27(P_s - P_a)$	$2.625(P_s - P_a)$	$2.625(P_s - P_a)$	0	$A_s = 14.5 \text{ in}^2$
NORMAL LOAD	$-.196 N$	$-.182 N$	$-.182 N$	0	
DRAW LOAD	$-.760(F - W_{\text{wind}})$	$+.380(F - W_{\text{wind}})$	$+.380(F - W_{\text{wind}})$	F	
SIDE LOAD	0	$-.626 Y$	$+.626 Y$	0	
PITCHING M_y	$-.1575 M_p$	$+.07875 M_p$	$+.07875 M_p$	0	
ROLLING M_x	0	$.130 M_R$	$-.130 M_R$	0	

POSITIVE GAGE LOAD IS TENSION.

NOTE

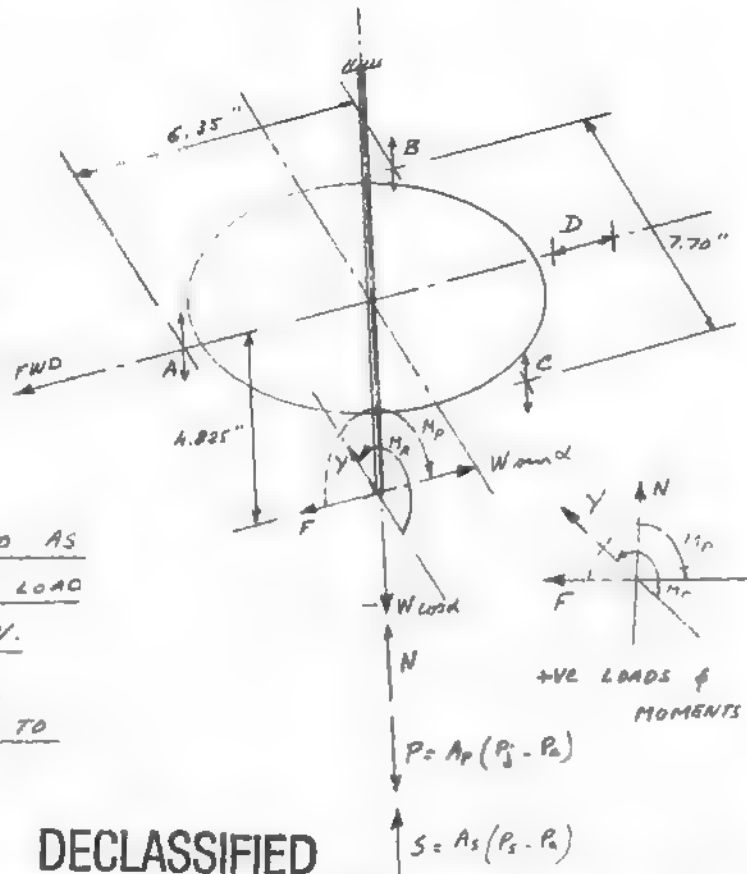
Pressure $(P_s - P_a)$
and $(P_s - P_a)$ in PSI.

TOTAL LOAD ON EACH GAGE

IS THE SUM OF THE
CORRESPONDING COLUMN

NOTE: ABOVE VALUES ARE VALID AS
LONG AS THE TOTAL NORMAL LOAD
DOES NOT EXCEED $+2.27B W$.

NORMAL LOADS OF THIS
MAGNITUDE ARE NOT EXPECTED TO
OCCUR DURING TESTS



DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaeger		Sept 1957		

~~SECRET~~

DECLASSIFIED

164

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL10-0 CALIBRATION10-1 GAGE EQUATIONS FOR CALIBRATION10-1-2 GAGE EQUATIONS & MAX. APPLIED LOADS.VERTICAL LOAD AT WHICH VERTICAL SUSPENSION ROD
WILL DISCONNECT.From Section 6-1-3 : Rod deflection: $\delta_r = 2.42 \times 10^{-5} W$ Gage system deflection: $\delta_g = 1.895 \times 10^{-5} W$

From the equation $\Delta W = W_1 + 1.278 W_1 = 2.278 W_1$,
 where W_1 is the weight of the model and $\Delta W = N$.
 we have

$$N = 2.278 \times 200 = 456 \text{ lb}$$

MAX. & MIN. LOADS APPLICABLE ON THE SYSTEM TO
REACH RATED GAGE LOADSNORMAL LOAD N.

GAGE A: Equations: $-800 \leq -0.35(N-200) \leq 800$ $N \geq 456$
COMPR. TENS.

$-800 \leq -0.196 N \leq 800$ $N \leq 456$
COMPR. TENS.

Gage load at $N = 456 \text{ lb}$

$$G_1 = -0.35 \times (456 - 200) = -0.35 \times 256 = -89.6 \text{ lb}$$

$$G_2 = -0.196 \times 456 = -89.6 \text{ lb}$$

at Min Gage load. $G = -0.196 N$

$$N = \frac{800}{-0.196} = -4080 \text{ lb}$$

at Max Gage load $G = -0.35(N-200)$

$$N = (-800 / -0.35) + 200 = 2485 \text{ lb}$$

WRITTEN BY

G. Jaeger

CHECKED BY

1

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL.10-0 CALIBRATION10-1 GAGE EQUATIONS FOR CALIBRATION10-1-2 GAGE EQUATIONS & MAX. APPLIED LOADS.MAX. & MIN. LOADS APPLICABLE ON THE SYSTEM TO REACH RATED
GAGE LOADS - CONT'D.GAGE B & C

$$\text{Equations: } -350 \leq -.325(N-200) \Big/ N \geq 456 \leq 350$$

$$-350 \leq -.182 N \Big/ N \leq 456 \leq 350$$

Gage load at $N = 456^{16}$

$$G_1 = -.325(456-200) = -.325 \times 256 = -83.2^{16}$$

$$G_1 = -.182 \times 456 = -83.2^{16}$$

at min. Gage load

$$G = -.182 N$$

$$\therefore N = \frac{350}{-.182} = -1925^{16}$$

at Max. Gage load $G = -.325(N-200)$

$$\therefore N = \frac{350}{-.325} + 200 = \underline{\underline{1275^{16}}}$$

PITCHING MOMENT M_p .GAGE A:

$$\text{Equation: } .1575 M_p = G_A = \pm 800^{16}$$

$$\therefore M_p = \frac{\pm 800}{.1575} = \pm 5080^{16}$$

GAGE B & C:

$$\text{Equation: } .07975 M_p = G_B = \pm 350^{16}$$

$$\therefore M_p = \frac{\pm 350}{.07975} = \pm 4400^{16}$$

WRITTEN BY

G. Jacques

CHECKED BY

P. J. S.

DATE

Sept. 1957

ISSUEAIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

166

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.10-0 CALIBRATION10-1 GAGE EQUATIONS FOR CALIBRATION10-1-2 GAGE EQUATIONS & MAX. APPLIED LOADS.MAX. & MIN. LOADS APPLICABLE ON THE SYSTEM TO REACH
RATED GAGE LOADS - CONT'D.ROLLING MOMENT M_R .GAGE B & C ONLY.

Equation: $\pm .130 M_R = G$

$$\therefore \frac{350}{\pm .130} = \underline{\underline{\pm 2690 \text{ in/lb}}}$$

SUMMARY-

The max. and min loads and moments that can be applied on the system must not exceed those which will produce the rated load of the weaker gage. Thus, gage B & C are limiting these loads and moments to the values underlined on the text and summarized below

F $F_{\text{up}} \text{ up}$ $\pm 150 \text{ lb}$
 Y : Side $\pm 50 \text{ lb}$
 N : up: 1275 lb down -1925 lb
 M_p : Pitching M_t $\pm 4440 \text{ in/lb}$
 M_R : Rolling M_t $\pm 2690 \text{ in/lb}$

NOTE: F & Y are limited by design consideration rather than gage strength

WRITTEN BY

J. Jaeger

CHECKED BY

/

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

167

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.10 - 0 CALIBRATION10 - 1 GAGE EQUATIONS FOR CALIBRATION.10-1-2 GAGE EQUATIONS & MAX. APPLIED LOADSGAGE EQUATIONS IN TERMS OF F, Y, N, MP & MR FOR $\alpha = 0$ Under calibration loads, F_s , F_a and $\alpha = 0$ then eq. given in 10-1-1

become

GAGE A

$$-800 \leq -.35(N+W)^{N \geq 2.278W} \quad -.76 F \quad -.1575 M_P \leq 800 \quad (\text{rod disengaged})$$

$$-800 \leq -.196 N^{N \leq 2.278W} \quad -.76 F \quad -.1575 M_P \leq 800 \quad (\text{rod engaged})$$

GAGE B & C

$$-350 \leq -.325(N+W)^{N \geq 2.278W} + .38 F \quad \pm .626 Y \quad + .07875 M_P \pm .130 M_R \leq 350 \quad (\text{rod disengaged})$$

$$-350 \leq -.182 N^{N \leq 2.278W} + .38 F \quad \pm .626 Y \quad + .07875 M_P \pm .130 M_R \leq 350 \quad (\text{rod engaged})$$

GAGE D

$$-150 \leq F \leq 150$$

MAX VALUES OF APPLIED LOADS & MOMENTS

F - FORE/AFT	$\pm 150 \text{ lb}$
Y - SIDE	$\pm 50 \text{ lb}$
N - UP/DOWN	$+ 1275 \text{ lb}$ to -1925 lb
M _P - PITCHING MT	$\pm 4440 \text{ in-lb}$
M _R - ROLLING MT	$\pm 2690 \text{ in-lb}$

NOTE. 1- Above loads (max.) apply singly when all other loads = 0

2- N may be sum of: normal load, pressure and suction load.

3- Gage readings will not differentiate between rolling Mt due to Y and M_RWRITTEN BY

G. J. Jorgensen

CHECKED BY

1

DATE

Sept. 1957

ISSUEAIRCRAFT~~SECRET~~

DECLASSIFIED

DECLASSIFIED

~~SECRET~~

AVRO/SPG/TR 112

168

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL10-0 CALIBRATION10-1 GAGE EQUATIONS FOR CALIBRATION10-1-2 GAGE EQUATIONS & MAX. APPLIED LOADSGAGE EQUATIONS & LIMITS - ASSUMING $W = -200$ GAGE A

$$-800 \leq -.35(N-200) \left/ \begin{array}{l} N=1875 \\ N=456 \end{array} \right. - .76 F \left/ \begin{array}{l} F=+150 \\ F=-150 \end{array} \right. - .1575 M_P \left/ \begin{array}{l} M_P=+4440 \\ M_P=-4440 \end{array} \right. \leq 800$$

$$-800 \leq -.136 N \left/ \begin{array}{l} N=456 \\ N=-1925 \end{array} \right. - .76 F \left/ \begin{array}{l} F=+150 \\ F=-150 \end{array} \right. - .1575 M_P \left/ \begin{array}{l} M_P=+4440 \\ M_P=-4440 \end{array} \right. \leq 800$$

GAGE B & C

$$-350 \leq -.325(N-200) \left/ \begin{array}{l} N=1275 \\ N=456 \end{array} \right. + .38 F \left/ \begin{array}{l} F=+150 \\ F=-150 \end{array} \right. \mp .626 Y \left/ \begin{array}{l} Y=+50 \\ Y=-50 \end{array} \right. + .07875 M_P \left/ \begin{array}{l} M_P=+4440 \\ M_P=-4440 \end{array} \right.$$

$$\pm .13 M_R \left/ \begin{array}{l} M_R=+2690 \\ M_R=-2690 \end{array} \right. \leq 350$$

$$-350 \leq -.182 N \left/ \begin{array}{l} N=456 \\ N=-1925 \end{array} \right. + .38 F \left/ \begin{array}{l} F=+150 \\ F=-150 \end{array} \right. \mp .626 Y \left/ \begin{array}{l} Y=+50 \\ Y=-50 \end{array} \right. + .07875 M_P \left/ \begin{array}{l} M_P=+4440 \\ M_P=-4440 \end{array} \right.$$

$$\pm .13 M_R \left/ \begin{array}{l} M_R=+2690 \\ M_R=-2690 \end{array} \right. \leq 350$$

GAGE D

$$-150 \leq F \left/ \begin{array}{l} F=+150 \\ F=-150 \end{array} \right. \leq 150$$

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacques		Sept. 1957		

~~SECRET~~

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL10-0 CALIBRATION10-2-0 CALIBRATION PROCEDURE.

The equations on page give the relations between gage loading and the applied loads N, F & Y and the moments M_x & M_z . These equations will hold only when there is no other interaction between the gages. The purpose of calibration is to find out any such interaction which may exist and provide means of adjusting these equations accordingly.

The calibration tests will be carried out in 4 series:

- Series 1 - Each load or moment applied singly.
- Series 2 - Loads N, F & moment M_x in combinations
- Series 3 - Loads N, F, Y & moments M_x & M_z in combinations
- Series 4 - Cases representing expected loading as calculated in the stress analysis report

SERIES 1 - Each load or moment applied singly

Table 1 & 2 indicate the loads to be applied on the calibration rig. These loads should be applied in steps from 0 to max. to 0 and from 0 to min. to 0.

SERIES 2 & 3 Combined loading.

The general principle used for calibrating under combined loading is a system where the gage load is held at a definite value and the applied loads and moments adjusted in various combinations to produce the same gage load. Thus, by using values of the applied loads and moments which should theoretically give a chosen gage load, it will be possible to estimate the error on the

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jaques	111	Sept. 1957		

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERING & TRANSITION MODEL -10-0 CALIBRATION10-2-0 CALIBRATION PROCEDURE - CONT'D.

gauge reading at various gauge loading level. A minimum of 5 different combinations should be tested at each gauge level for both 2 or more applied loads or moments combinations

Series 2 - All possible combinations of N, F & M are shown graphically on charts 3 & 4 for gauge A and on charts 5 & 6 for gauges B & C

Series 3 - All possible combinations of N, F, Y , M & M_R are shown graphically on charts 7 & 8 for gauges B & C

It should be noted that gauge A is not theoretically affected by Y or M_R . However, it will be necessary to assume its reading during calibration of gauges B & C

SERIES 4 - Straining Cases.

This series is an attempt to represent approximately the conditions of the model tests. It is felt that this series of calibration tests will give some information on the behaviour of the balance in a range close to that we may expect in operation. Loads to be applied on the calibration rig for each case stressed in this report are given on table 3

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. J. [Signature]	1.	Sept. 1957		

UNCLASSIFIED

AVRO/SPG/TR. 112

STRESS ANALYSIS OF $\frac{1}{2}$ SCALE HOVERCRAFT & TRANSITION
MODEL

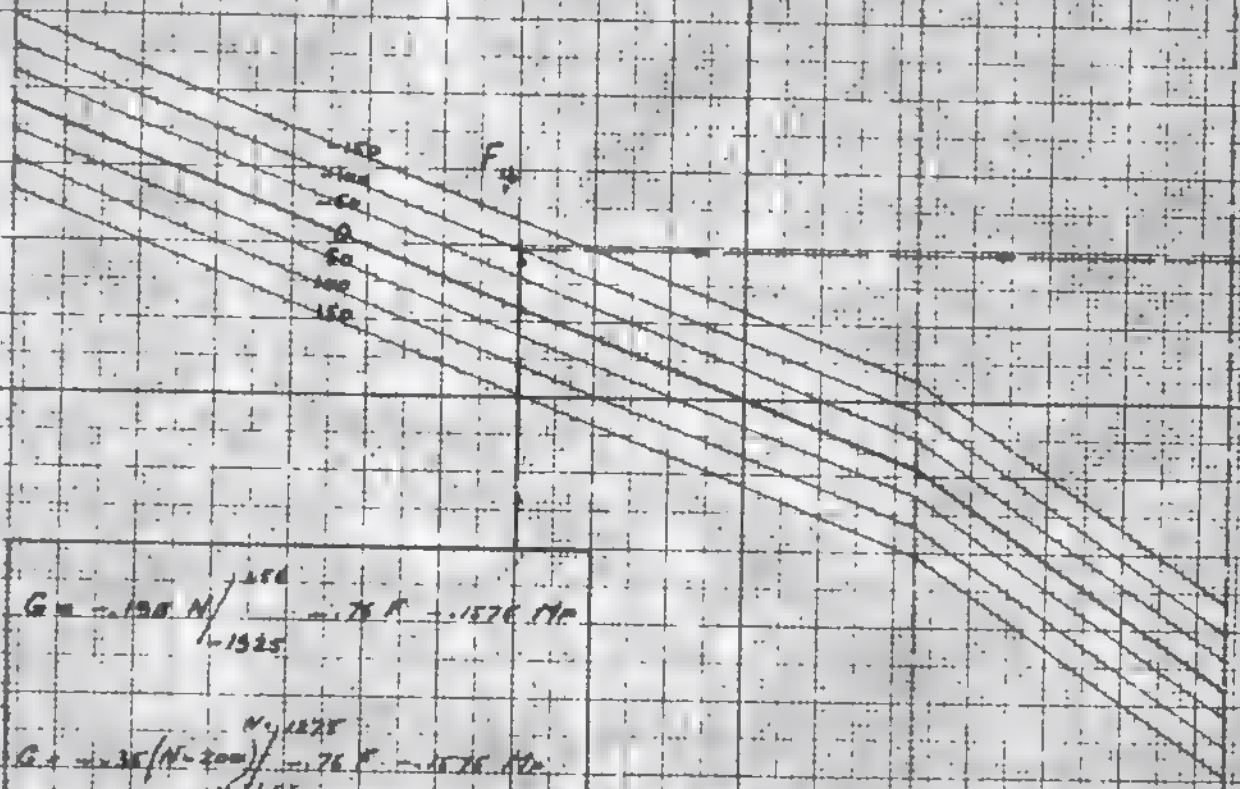
GAGE CALIBRATION

10-0 CALIBRATION

10-1 GAGE EQUATIONS FOR CALIBRATION

GRAPHICAL SOLUTION

10-1-2 GAGE EQUATIONS & MAX. APPLIED LOADS



-1525

$N/1500$

0

456

1575

EXAMPLE $N = 600$ $F = 100$ $M = 2000$

THE GAGE A SLOPE TENSION

UNCLASSIFIED

UNCLASSIFIED

171

ATIONS

GAGE - A -

CHART N° 1



5. 7/15/57

5. 7/15/57

UNCLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

10-0 CALIBRATION

10-2 CALIBRATION RIG.

10-2-2 LOADS ON CALIBRATION RIG.

TABLE 3

TEST CASES WITH NO ROLLING MOMENT OR SIDE LOAD.									
LOADS ON RIG									
APPLIED LOADS	1			2			3		
	CASE	N _{1b}	F _{1b}	M _p _{1b}	OUT	UP	DOWN	OUT	UP
HOVERING HORIZONTAL		-1.6	0	0			41		41
HOVERING 20°		-18.5	-3.8	-85.3			47.1	3.8	47.1
HIGH DRAG		-18.2	-10.2	-140			47.4	11.4	47.4
MAX. THRUST		-4.86	+141	0	141		121.5		121.5
TRANSITION -10° 30 PSF		-54	+29.2	-430	29.2		136.5		136.5
TRANSITION 20° 30 PSF		-20.2	-27	+15.5		30.85	7.55	27	7.55
TRANSITION 35° 30 PSF		+15.6	+21.2	+2735	21.2	107.4	39		39
TRANSITION 45° 18 PSF		-21	-3.8	+4320		102.75	5.25	38	5.25

WRITTEN BY

g. Jaeger

CHECKED BY

1

DATE

Sept. 1957

ISSUE

DECLASSIFIED

AIRCRAFT

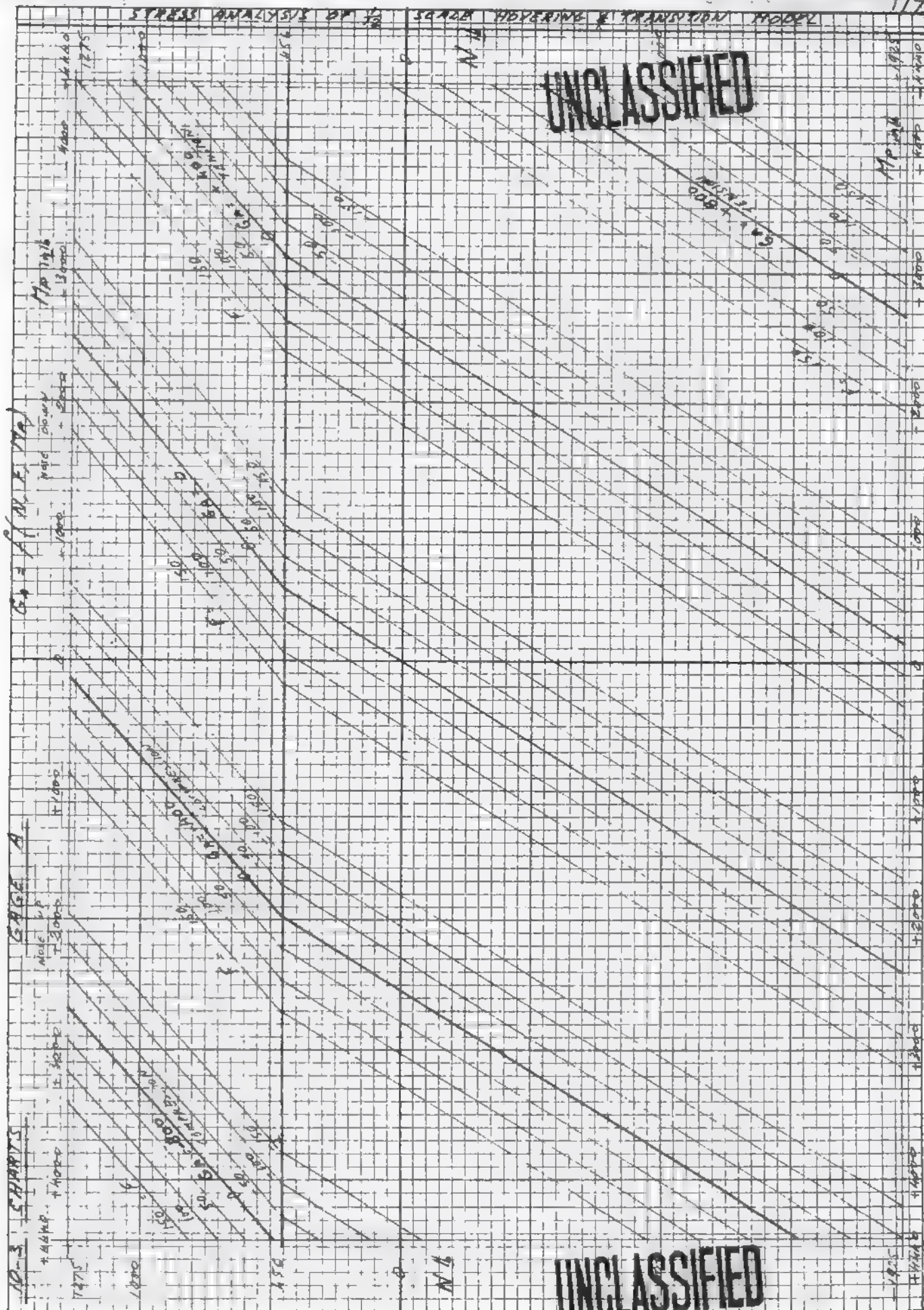
~~SECRET~~

3442A	HYPERTENS	TRANSITION	MODE
-------	-----------	------------	------

UNCLASSIFIED

CHART N° 3

UNCLASSIFIED



5. ~~7-7-7~~

Sept. 1957

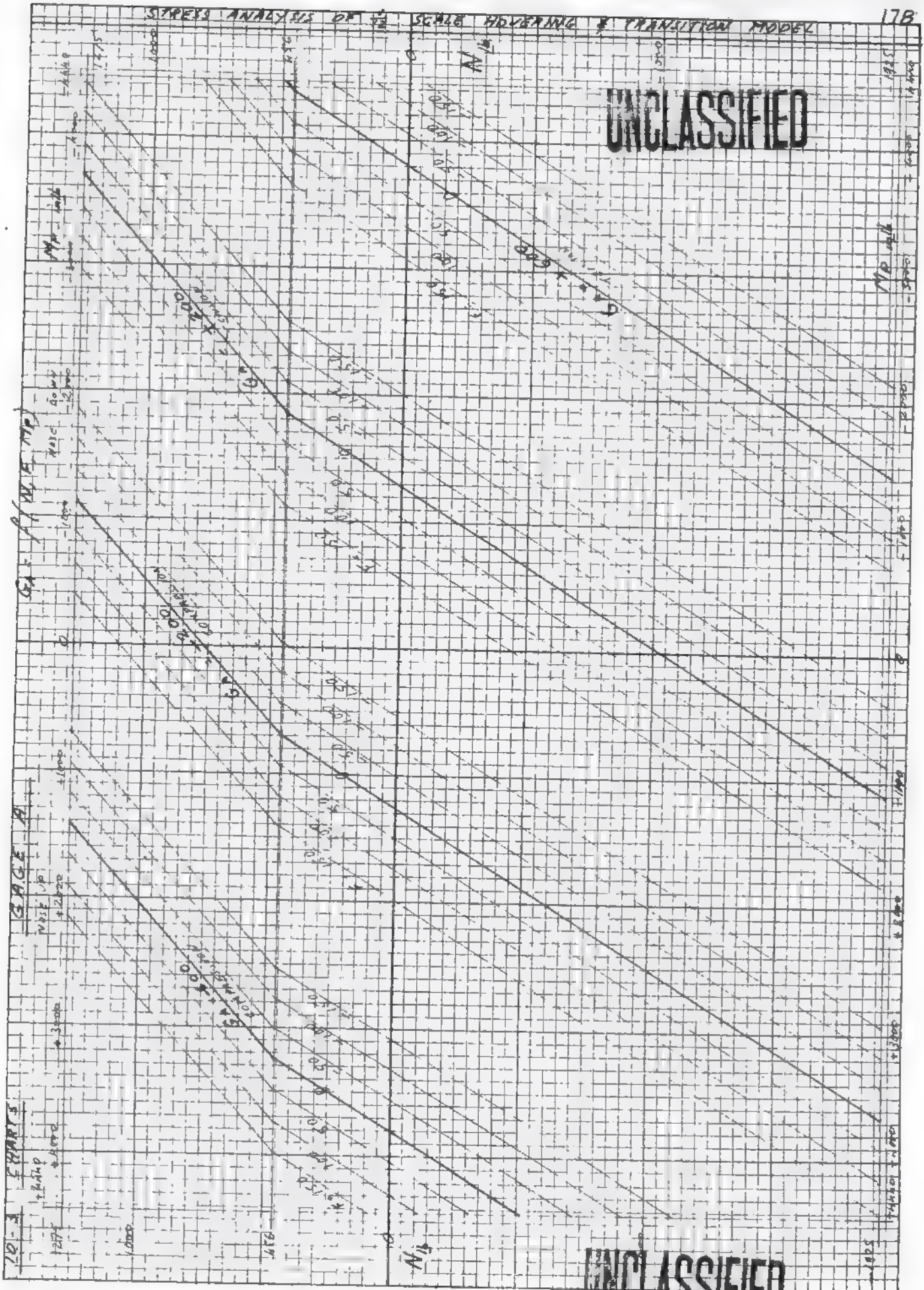
WHEELER & WHEELER
ATTORNEYS AT LAW
10, K. 10 to the north

STRESS ANALYSIS OF THE SCALB HOVERING & TRANSITION MODEL

17B

UNCLASSIFIED

CHART N° 4



G. J. J. J.

Sept. 1957

UNCLASSIFIED

STRESS ANALYSIS OF 1/2 SCALE HOVERCRAFT & TRANSITION MODELS

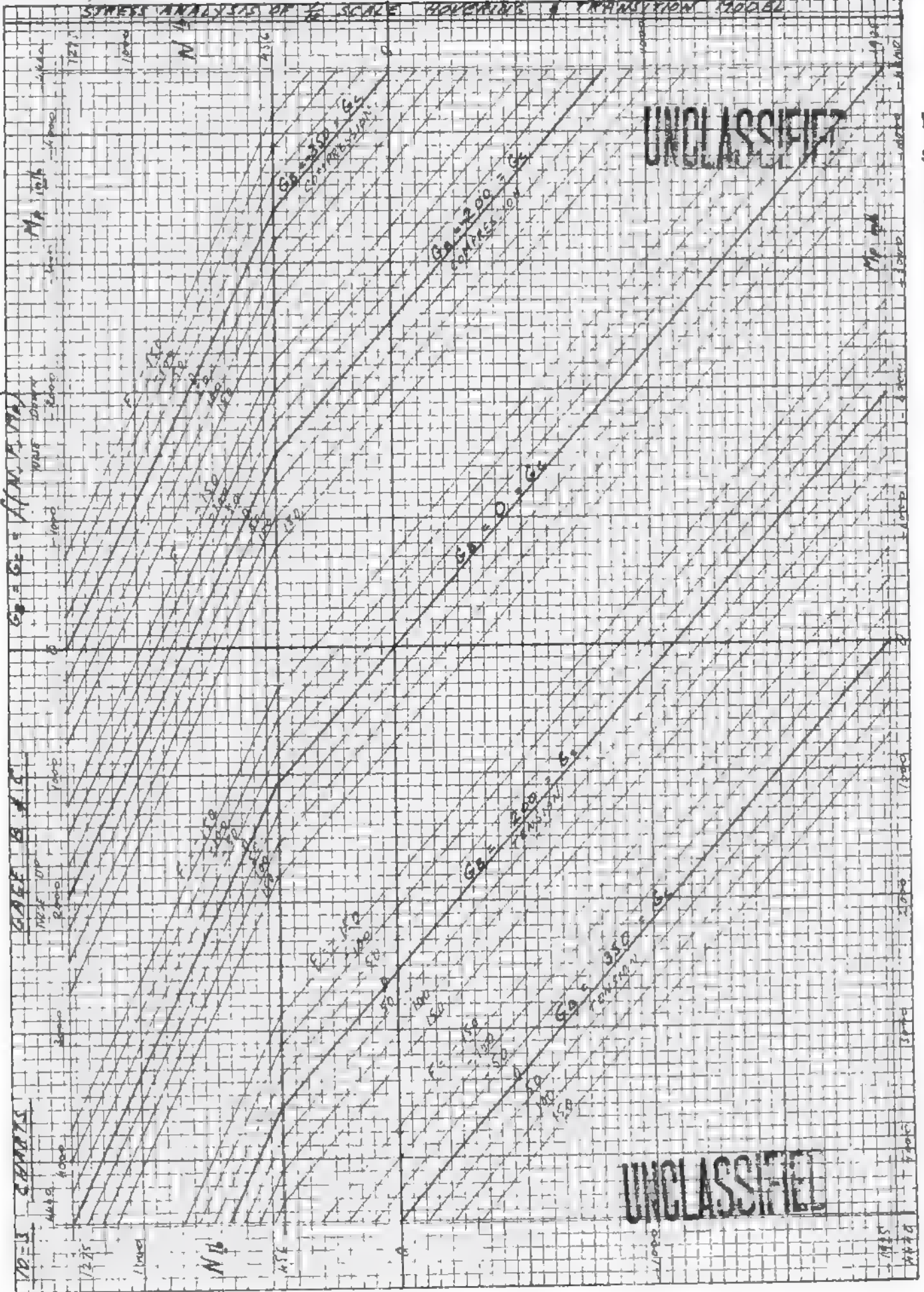


CHART N° 5

G. Jaeger

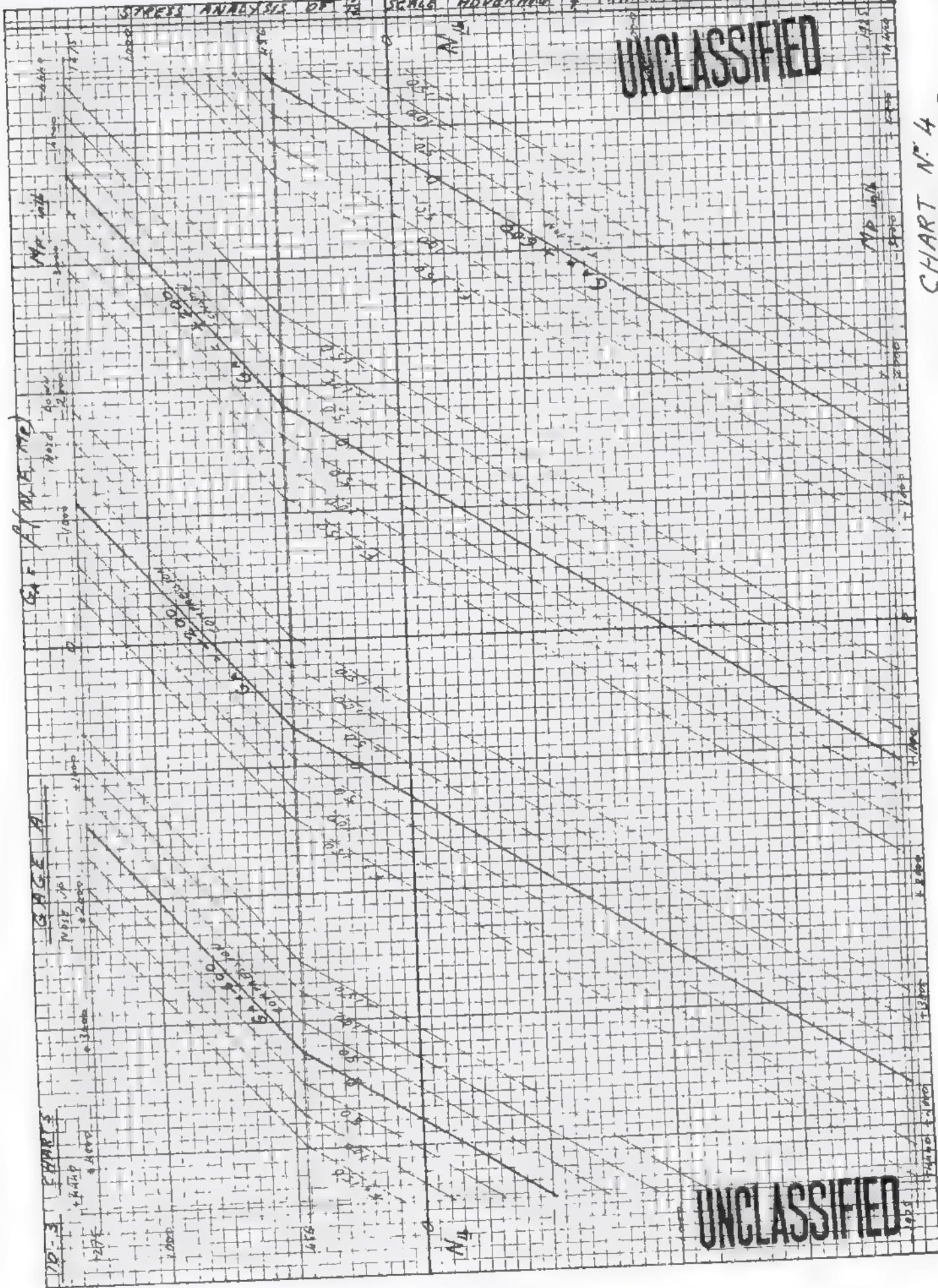
Sept. 1957

STRESS ANALYSIS OF SCALE HOVERING & TRANSITION MODEL

UNCLASSIFIED

CHART N° 4

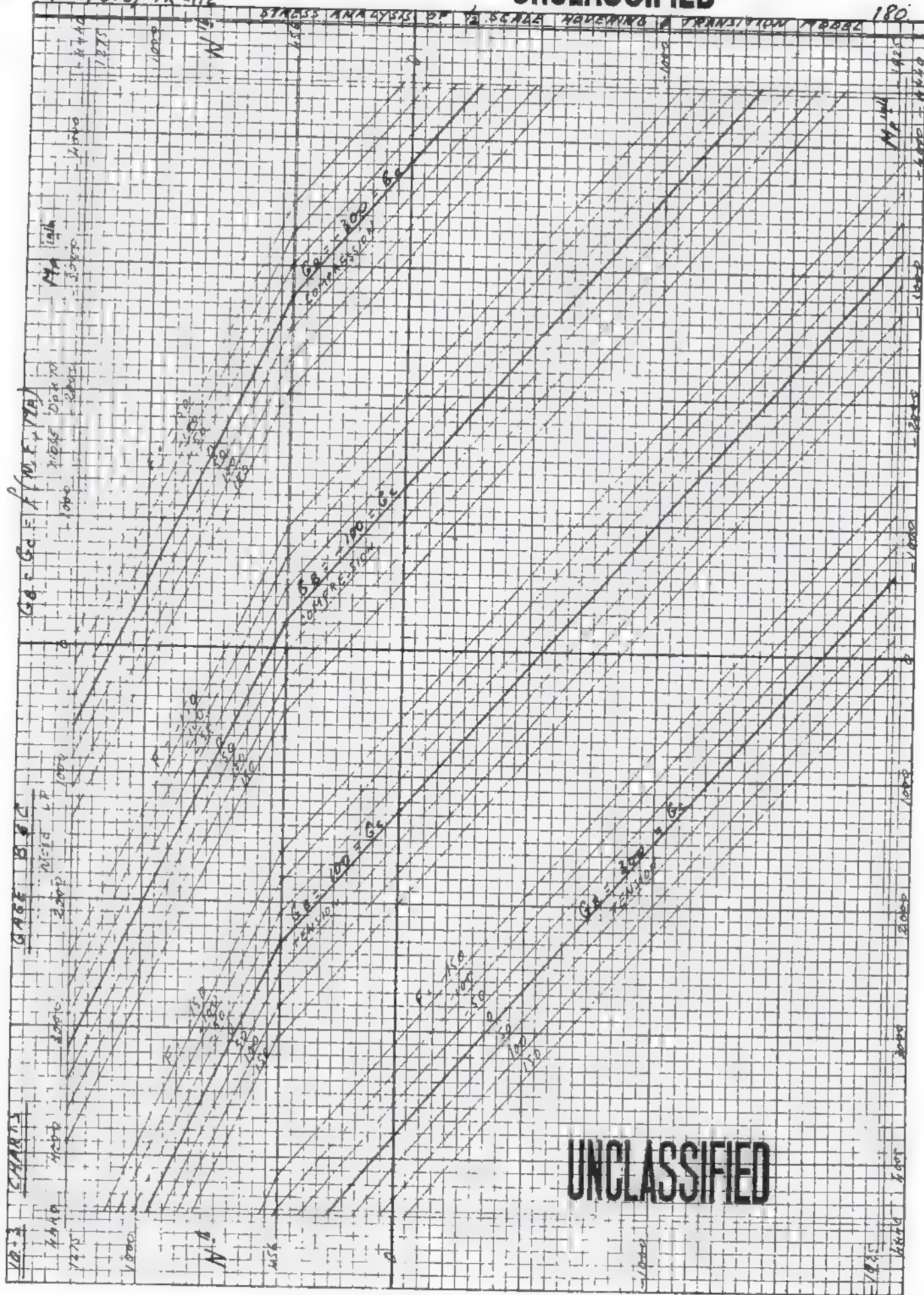
UNCLASSIFIED



UNCLASSIFIED

CHART N° 6

180



9.9 ~~_____~~

Sept. 1957

MADE IN U.S.A.
10 X 10 for 4 pin. jump.
KENTLETT & EBBELIN S.C.

~~SECRET~~

AVRO/SPG/TA 112

STRESS ANALYSIS OF 1/2 SCALE NONRIGID TRANSITION MODEL

DECLASSIFIED

121

CHART N: 7

18-D CANADIAN

7/11/87 P. 6/1

PAGE 81C

1870

DECLASSIFIED

[illegible]

AVRO/SPE/TRA 112

STRESS ANALYSIS OF $\frac{1}{10}$ SCALE NAVARINO & TRANSITION MODEL

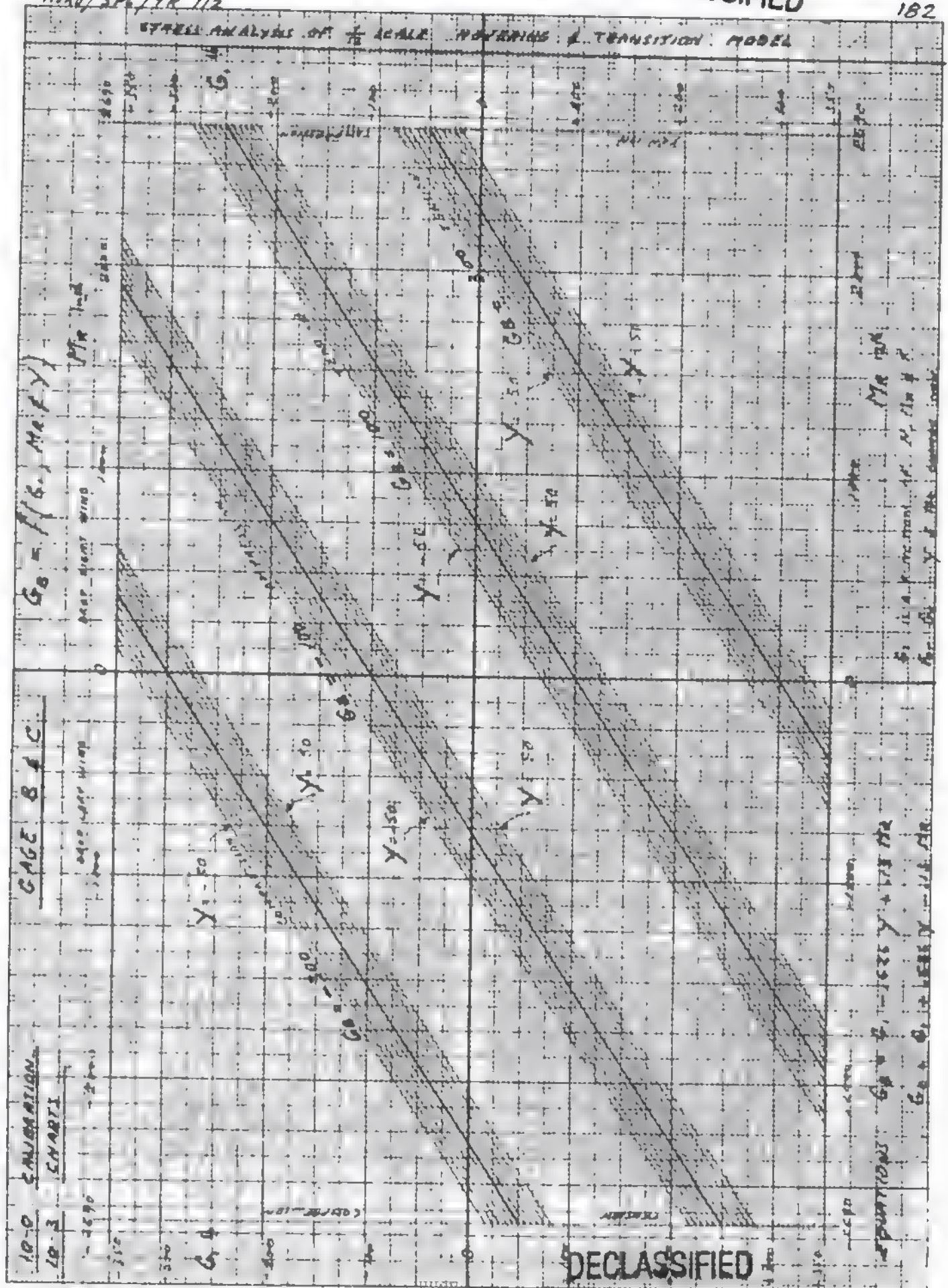


CHART N° 8

DECLASSIFIED

Sept 1957

~~SECRET~~

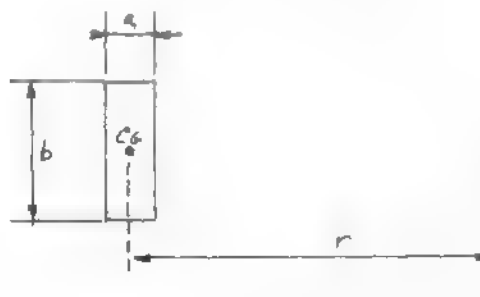
DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHT.A-1 - WEIGHT OF MODELA-1-1 GENERAL.

Volume of an annulus: Sectional area \times path of the CG

$$V = a b 2\pi r$$

$$W = S a b 2\pi r$$



Using Simpson's rule we can find

$$a = .25"$$

$$S = .283 \frac{lb}{in^3}$$

hence: the term $2\pi a S = 2 \times \pi \times .25 \times .283 = .445$

Hence: the weight of one element: $dW = .445 b r$

and the total weight of one annular part is

$$W = .445 \sum b r$$

Values of $b r$ are tabulated for each part.

DECLASSIFIED

WRITTEN BY

G. Jacques

CHECKED BY

1 -

DATE

Sept. 1957

ISSUE

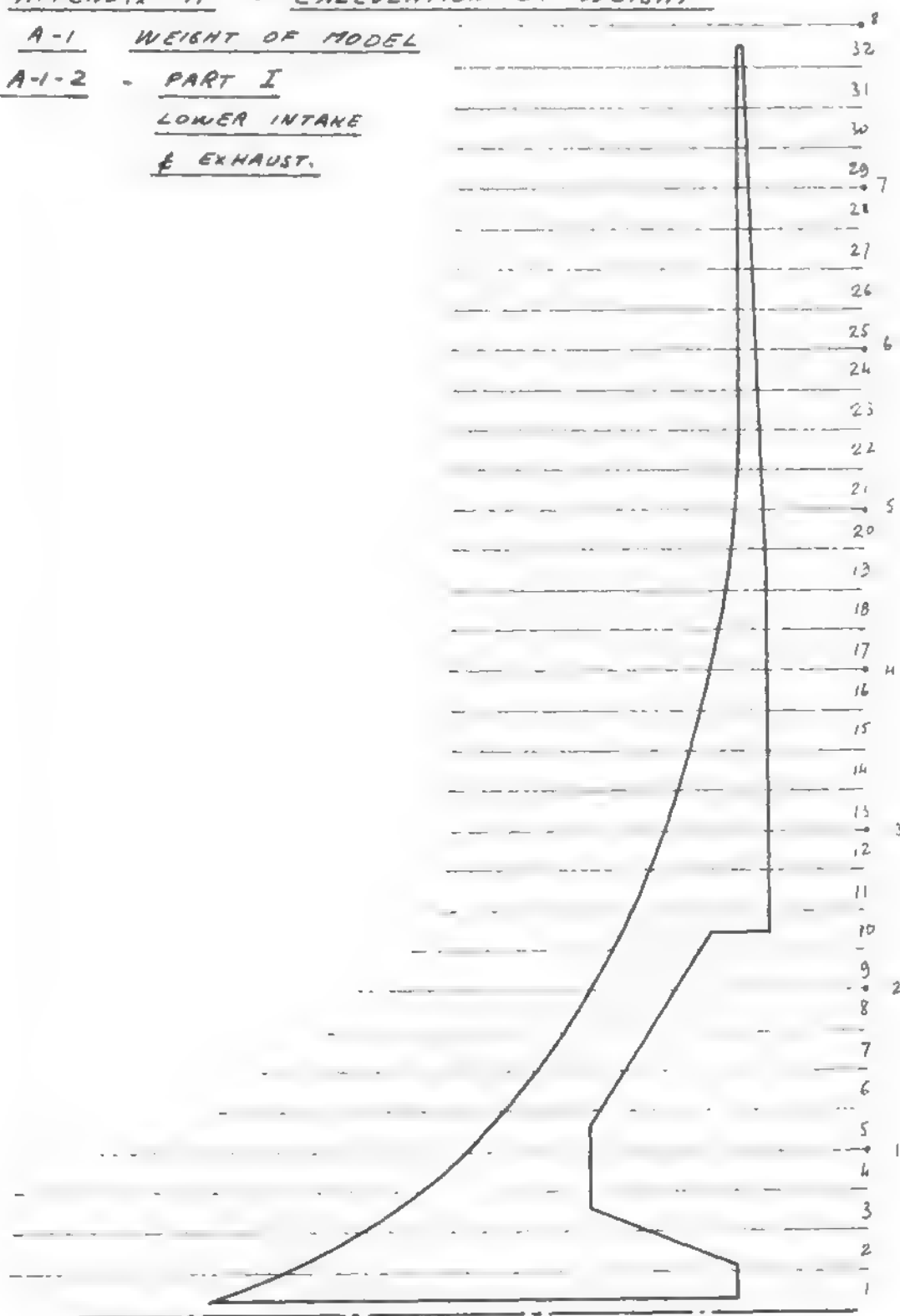
AIRCRAFT

~~SECRET~~

~~SECRET~~

DECLASSIFIED

184

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.APPENDIX A - CALCULATION OF WEIGHTA-1 WEIGHT OF MODELA-1-2 - PART ILOWER INTAKE& EXHAUST.

WRITTEN BY

G. J. J. J.

CHECKED BY

11

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

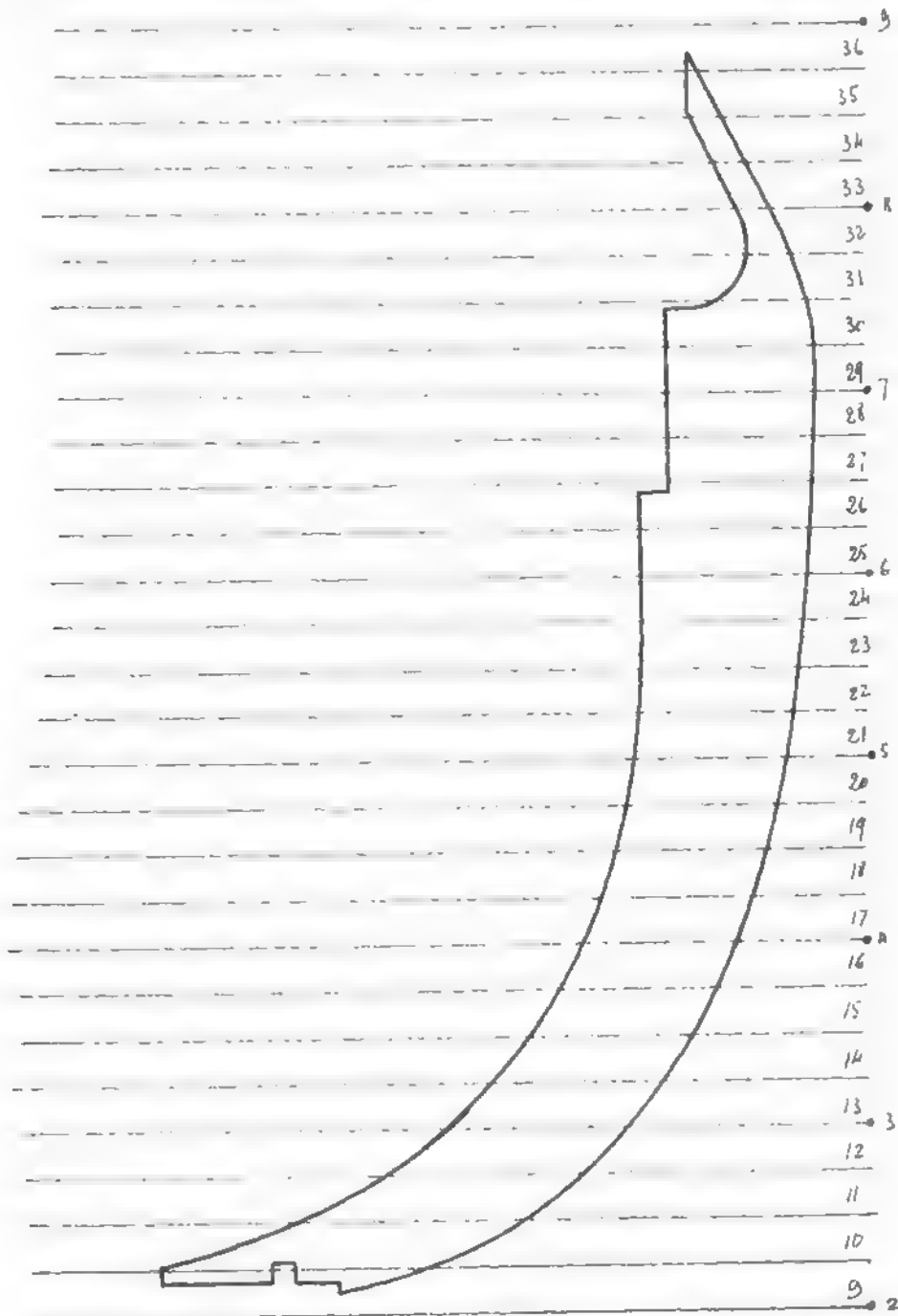
DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

APPENDIX A - CALCULATION OF WEIGHT

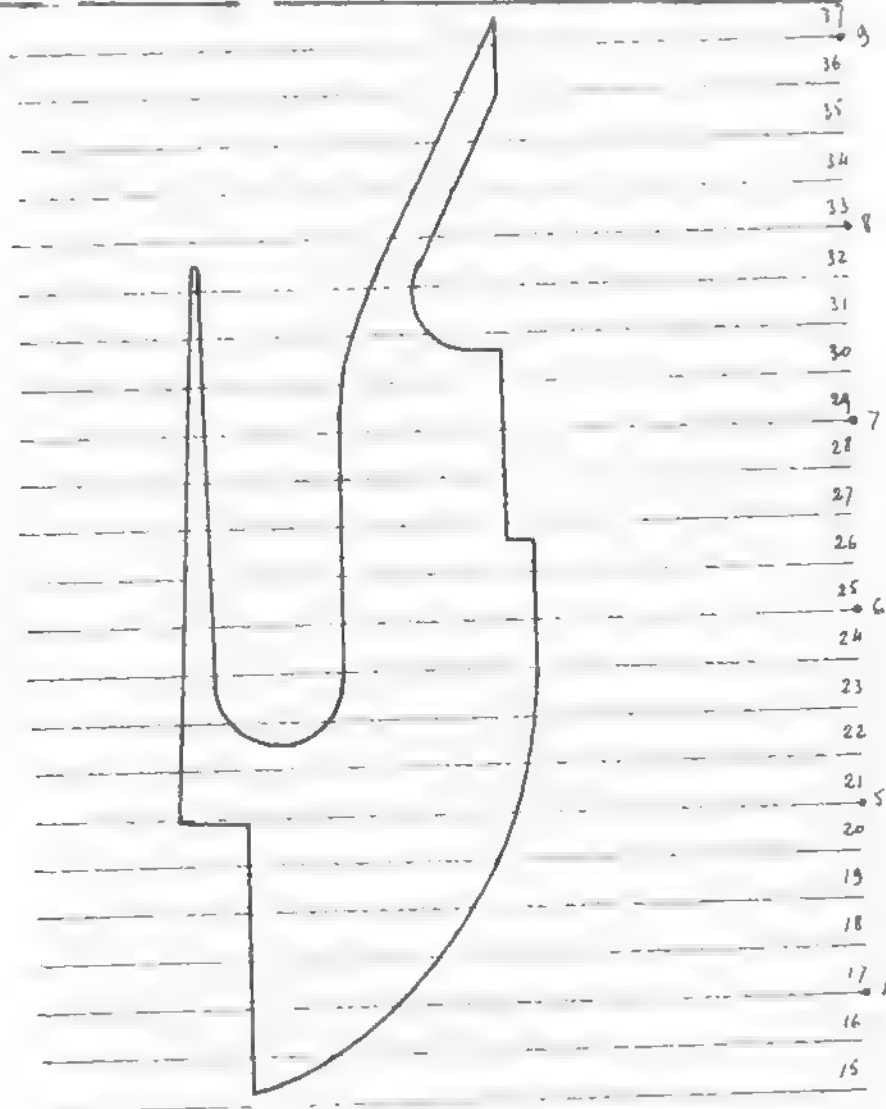
A-1 WEIGHT OF MODEL

A-1-3 PART II LOWER RAMP.



DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
<i>G. Jaeger</i>		Sept. 1957		

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-1 WEIGHT OF MODELA-1-4 PART III UPPER FALSE INTAKE & RAMP

DECLASSIFIED

WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. Jacquemin		Sept. 1957		

AVRO/SR/79 112

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{8}$ SCALE HOVERING MODEL

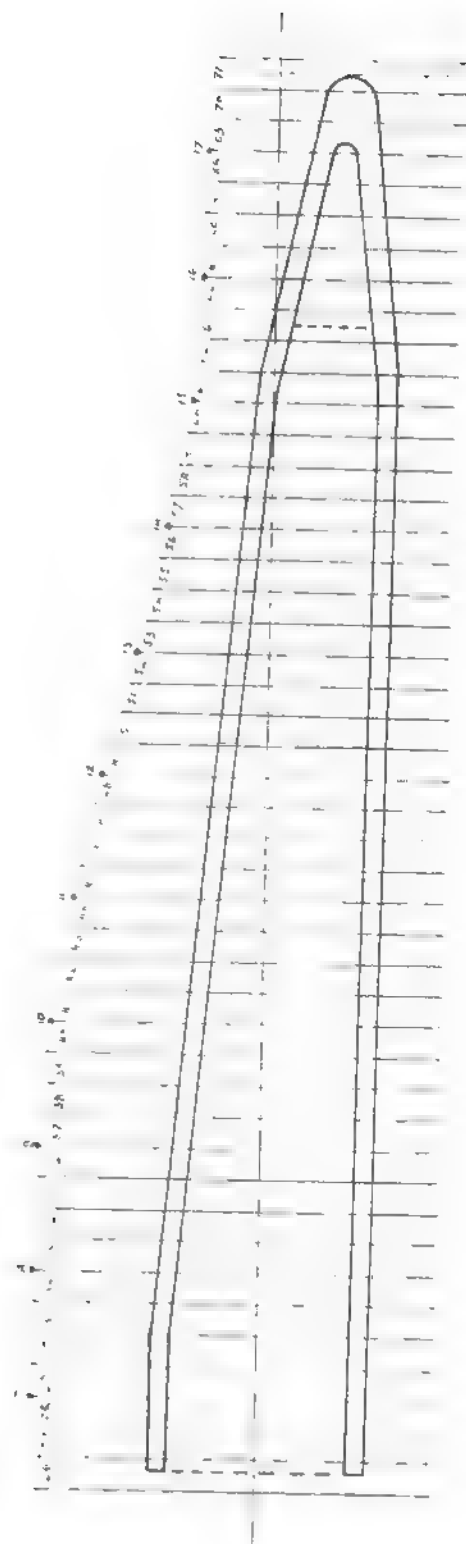
APPENDIX A - CALCULATION OF WEIGHT

A-1 WEIGHT OF MODEL

A-1-S PART II - WING

1. Temperature

Sept 1917



DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL
4-1-5 WEIGHT OF MODEL COMPONENTS.

188

ITEM	PART I			PART II			PART III			DECLASSIFIED
	r in	b in	rb in ²	r in	b in	rb in ²	r in	b in	rb in ²	
1	.125	.3	.375							
2	.375	.3	.465							
3	.625	.3	.615							
4	.875	.3	.785							
5	1.125	.3	.955							
6	1.375	.3	1.125							
7	1.625	.3	1.295							
8	1.875	.3	1.465							
9	2.125	.3	1.635							
10	2.375	.3	1.805							
11	2.625	.3	1.975							
12	2.875	.3	2.145							
13	3.125	.3	2.315							
14	3.375	.3	2.485							
15	3.625	.3	2.655							
16	3.875	.3	2.825							
17	4.125	.3	2.995							
18	4.375	.3	3.165							
19	4.625	.3	3.335							
20	4.875	.3	3.505							
21	5.125	.3	3.675							
22	5.375	.3	3.845							
23	5.625	.3	4.015							
24	5.875	.3	4.185							
25	6.125	.3	4.355							
26	6.375	.3	4.525							
27	6.625	.3	4.695							
28	6.875	.3	4.865							
29	7.125	.3	5.035							
30	7.375	.3	5.205							
31	7.625	.3	5.375							
32	7.875	.3	5.545							
33	8.125	.3	5.715							
34	8.375	.3	5.885							
35	8.625	.3	6.055							
36	8.875	.3	6.225							
37	9.125	.3	6.395							
38	9.375	.3	6.565							
39	9.625	.3	6.735							
40	9.875	.3	6.905							
41	10.125	.3	7.075							
42	10.375	.3	7.245							
43	10.625	.3	7.415							
44	10.875	.3	7.585							
45	11.125	.3	7.755							
46	11.375	.3	7.925							
47	11.625	.3	8.095							
48	11.875	.3	8.265							
49	12.125	.3	8.435							
50	12.375	.3	8.605							
51	12.625	.3	8.775							
52	12.875	.3	8.945							
53	13.125	.3	9.115							
54	13.375	.3	9.285							
55	13.625	.3	9.455							
56	13.875	.3	9.625							
57	14.125	.3	9.795							
58	14.375	.3	9.965							
59	14.625	.3	10.135							
60	14.875	.3	10.305							
61	15.125	.3	10.475							
62	15.375	.3	10.645							
63	15.625	.3	10.815							
64	15.875	.3	10.985							
65	16.125	.3	11.155							
66	16.375	.3	11.325							
67	16.625	.3	11.495							
68	16.875	.3	11.665							
69	17.125	.3	11.835							
70	17.375	.3	12.005							
71	17.625	.3	12.175							
72	17.875	.3	12.345							
73	18.125	.3	12.515							
74	18.375	.3	12.685							
75	18.625	.3	12.855							
76	18.875	.3	13.025							
77	19.125	.3	13.195							
78	19.375	.3	13.365							
79	19.625	.3	13.535							
80	19.875	.3	13.705							
81	20.125	.3	13.875							
82	20.375	.3	14.045							
83	20.625	.3	14.215							
84	20.875	.3	14.385							
85	21.125	.3	14.555							
86	21.375	.3	14.725							
87	21.625	.3	14.895							
88	21.875	.3	15.065							
89	22.125	.3	15.235							
90	22.375	.3	15.405							
91	22.625	.3	15.575							
92	22.875	.3	15.745							
93	23.125	.3	15.915							
94	23.375	.3	16.085							
95	23.625	.3	16.255							
96	23.875	.3	16.425							
97	24.125	.3	16.595							
98	24.375	.3	16.765							
99	24.625	.3	16.935							
100	24.875	.3	17.105							

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL
H-1-S WEIGHT OF MODEL COMPONENTS

189

PART IV				PART IV			
ITEM	r	b	rb	ITEM	r	b	rb
	in	in	in ²		in	in	in ²
	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{64}$		$\frac{1}{8}$	$\frac{1}{8}$	$\frac{1}{64}$
26	6.450	.300	.193	56	12.875	.300	.386
27	5.25	.300	.158	57	12.875	.300	.386
28	5.25	.300	.158	58	12.875	.300	.386
29	7.125	.300	.214	59	12.875	.300	.386
30	7.125	.300	.214	60	14.875	.300	.445
31	7.125	.300	.214	61	15.125	.300	.452
32	7.125	.300	.214	62	15.375	.300	.461
33	8.125	.300	.244	63	15.625	.300	.470
34	8.125	.300	.244	64	15.875	.300	.479
35	8.625	.300	.259	65	16.125	.300	.488
36	8.875	.300	.266	66	16.375	.300	.497
37	9.125	.300	.275	67	16.625	.300	.506
38	9.375	.300	.284	68	16.875	.300	.515
39	9.625	.300	.291	69	17.125	.300	.524
40	9.875	.300	.299	70	17.375	.300	.533
41	10.125	.300	.306	71	17.625	.300	.542
42	10.375	.300	.313				
43	10.625	.300	.320				
44	10.875	.300	.327				
45	11.125	.300	.334				
46	11.375	.300	.341				
47	11.625	.300	.348				
48	11.875	.300	.355				
49	12.125	.300	.362				
50	12.375	.300	.369				
51	12.625	.300	.376				
52	12.875	.300	.383				
53	13.125	.300	.390				
54	13.375	.300	.397				
55	13.625	.300	.404				

~~SECRET~~
DECLASSIFIED

$$\Sigma RL = 163.55$$

$$\text{Item 46: } 2.05 \times .08 \times 1.28 \times 1.28 = .274$$

$$\text{Item 47: } 2.05 \times .08 \times 1.28 \times 1.28 = .274$$

$$163.55 + .274 + .274 = 164.1$$

TOTAL WEIGHT OF MODEL: $104.3 + 73.5 = 177.8$ lb

DECLASSIFIED

~~SECRET~~STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL4-1-5 WEIGHT OF MODEL COMPONENTS

Weight of ribs

$$\text{Side area: } \frac{7.5}{2} (.82 + 1.45) + (.95 \times 1.45) + \frac{.625}{2} (.65 + .82) =$$

$$8.5 + 1.375 + .46 = 10.338 \text{ in}^2$$

$$\text{Weight per rib: } .283 \times 10.338 \times .30 = .887 \text{ lb}$$

Total weight of ribs: 24 ribs:

$$.887 \times 24 = 21.30 \text{ lb}$$

4-1-6 TOTAL WEIGHT OF MODEL.

TOTAL WEIGHT OF MODEL WITHOUT DEDUCTION OF HOLES:

$$177.8 + 21.30 = 199.1 \text{ lb}$$

The holes will remove about 10 lb. However, instrumentation inside the model will add to the total and we can expect other variations due to tolerances etc.

TOTAL WEIGHT OF THE MODEL IS TAKEN AT: 200 lb

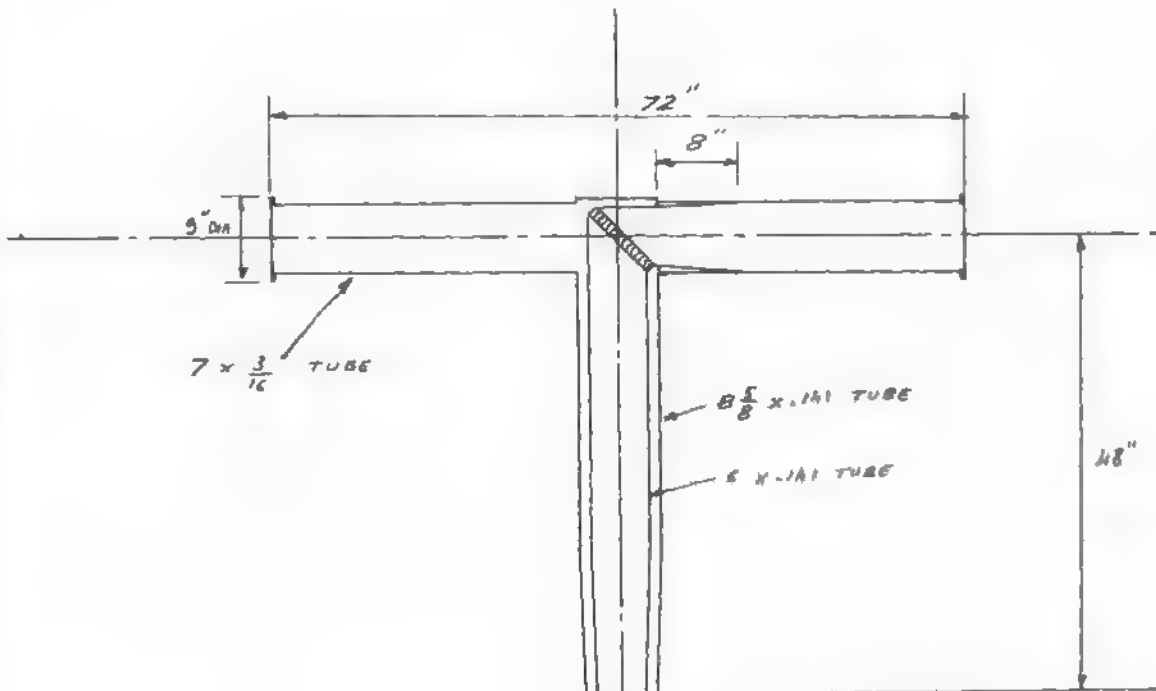
WRITTEN BY	CHECKED BY	DATE	ISSUE	AIRCRAFT
G. J. J. J.		Sept. 1957		

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.APPENDIX A - CALCULATION OF WEIGHT.A-2 - WEIGHT OF MODEL SUPPORT STRUCTURE.A-2-1 - MAIN TUBES.

Weight of Steel pipe: Ref. ARMCO Welded Steel Pipe. Catalog.

O.D.	WALL THK.	WEIGHT/ft
6 "	.141 "	8.80 $\frac{16}{100}$
6.625 "	.141 "	12.74 $\frac{16}{100}$

Tube $7 \times \frac{3}{16}$ is available from stock: item: HT. 1015
cold drawn seamless tube.

Weight per foot at $.283 \frac{lb}{in^3}$

$$.283 \times 12 \times \frac{\pi}{4} (7^2 - 6.625^2) = 13.32 \frac{lb}{ft}$$

WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

192

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHT.A-2 WEIGHT OF MODEL SUPPORT STRUCTUREA-2-1 MAIN TUBES.Weight of horizontal main tube: $13.32 \frac{72}{12} = 80 \frac{1}{2}$ *Weight of $8 \frac{5}{8}$ Vertical tube: $12.74 \frac{48+8}{12} = 59.5 \frac{1}{2}$ *Weight of 6" Vertical tube: $8.80 \frac{48}{12} = 35.20 \frac{1}{2}$ *Tapered entry to 6" tube: assume approx. equal to 1 ft. of
tube $6 \frac{5}{8}$ OD x .141 Wall: $9.74 \frac{1}{2}$ say. $10 \frac{1}{2}$ *Weight of cascade: assume $2 \frac{1}{2}$ *

End rings.

$$2 \times .283 \times .375 \times \frac{\pi}{4} (9^2 - 7^2) = 5.33 \frac{1}{2}$$
 *

Total weight of model mounting not including incidence arm and
gase mounting

$$80 + 59.5 + 35.2 + 10 + 2 + 5.33 = 192 \frac{1}{2}$$
 **

$$\text{Weight of vertical tubes: } 59.5 - 35.2 = 24.3 \frac{1}{2}$$

WRITTEN BY

G. Jacques

CHECKED BY

1.

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

193

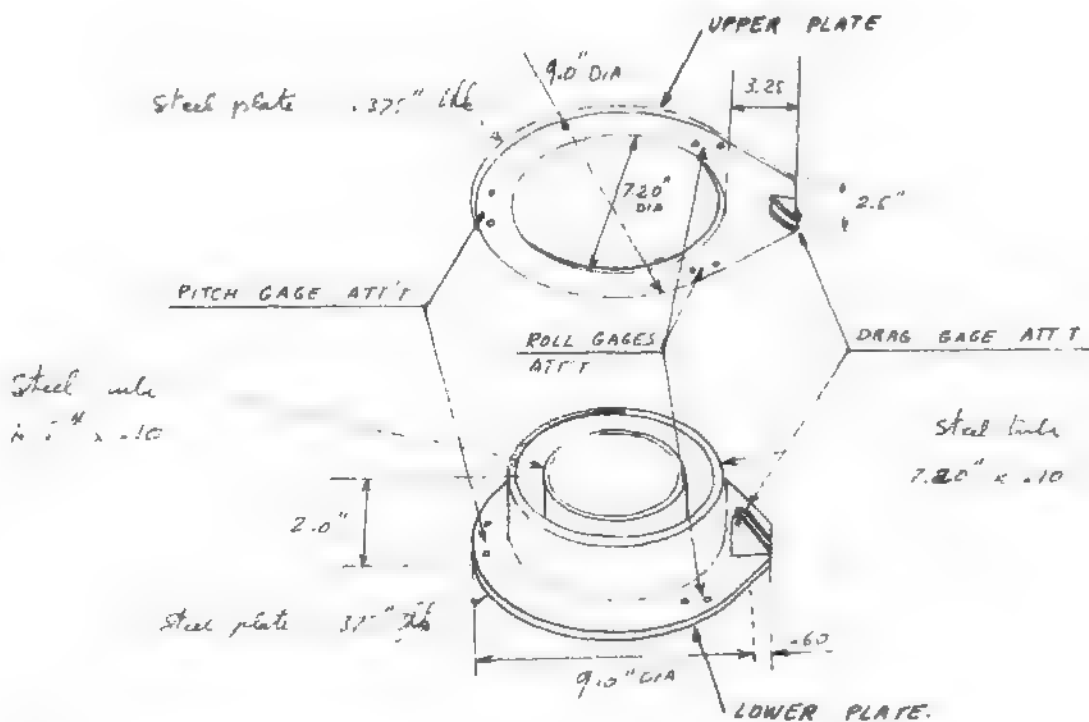
STRESS ANALYSIS OF $\frac{1}{12}$ SCALE MOVING & TRANSITION MODEL

APPENDIX A - CALCULATION OF WEIGHT

A-2 WEIGHT OF MODEL SUPPORT STRUCTURE

A-2-2

LOAD GAGES ASS'Y.



UPPER PLATE

Area: measured on dup. 37.68 in^2

Weight of plate. $.293 \times .375 \times 37.68 = 4.0 \text{ lb}$

LOWER PLATE

Area measured on drawing: 28.18 in^2

Weight of plate: $.283 \times .375 \times 28.18 = 3.00$ lb

WRITTEN BY

G. Jacquarini

CHECKED BY

122

DATE _____

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

AYRO EA 3110

~~SECRET~~

~~SECRET~~STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-2 WEIGHT OF MODEL SUPPORT STRUCTUREA-2-2.LOAD GAGE ASS'Y - CONT'D.

Tubes:

$$\text{Larger tube: Weight } .283 \times 2.0 \frac{\pi}{4} (7.2^2 - 7.0^2) = 1.33 \text{ lb}$$

$$\text{Smaller tube: Weight: } .283 \times 2.5 \frac{\pi}{4} (4.5^2 - 4.1^2) = .62 \text{ lb}$$

Drag gage Brackets

Weight estimated at 1 lb

Total weight:

$$4 + 3 + 1.33 + .62 + 1 = 9.95 \text{ lb}$$

add 10% for welds, bolts etc...

$$9.95 \times 1.1 = 10.95 \text{ lb say } 11 \text{ lb}$$

WEIGHT OF RING GAGES.GAGE A. 800 lb RATED LOAD.

$$W = .283 \left[\frac{\pi}{4} (D^2 - d^2) b + 2 b_f t_f L_f + 2 b_p t_p L_p \right]$$

substituting $d = D - 2t$

$$W = .283 \left[\pi b t (D - t) + 2 b_f t_f L_f + 2 b_p t_p L_p \right]$$

$$= .283 \left[\left(\pi \times .625 \times .22 (3 - .22) \right) + (2 \times .50 \times .08 \times .55) + (2 \times .50 \times .20 \times 1.50) \right]$$

$$= .436 \text{ lb}$$

WRITTEN BY

G. Jaeger

CHECKED BY

1

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-2 WEIGHT OF MODEL SUPPORT STRUCTUREA-2-2 LOAD GAGE ASS'YWEIGHT OF RING GAGES - CONT'DGAGES B & C : RATED LOAD : 350^{lb}

$$\begin{aligned}
 W &= .283 \left[\pi b t (D-t) + 2 b_f t_f L_f + 2 b_p t_p L_p \right] \\
 &= .283 \left[\pi \times .50 \times .165 (3 - .165) + (2 \times .375 \times .047 \times .55) + (2 \times .50 \times .26 \times 1.50) \right] \\
 &= .298 \text{ }^{\text{lb}} \text{ per gage} \qquad \qquad \qquad .596 \text{ }^{\text{lb}} \text{ for the 2 gages} \quad \times
 \end{aligned}$$

GAGE D : RATED LOAD : 150^{lb}

$$\begin{aligned}
 W &= .283 \left[\pi b t (D-t) + 2 b_f t_f L_f + 2 b_p t_p L_p \right] \\
 &= .283 \left[\pi \times .40 \times .10 (2 - .10) + (2 \times .25 \times .030 \times .35) + (2 \times .375 \times .375 \times .50) \right] \\
 &= .109 \text{ }^{\text{lb}} \quad \times
 \end{aligned}$$

TOTAL WEIGHT OF GAGES:

$$.436 + .596 + .109 = 1.141 \text{ }^{\text{lb}}$$

add 10% for bolts heads, wiring etc:

$$1.141 \times 1.1 = \approx 1.3 \text{ }^{\text{lb}} \quad \times$$

Total weight of vertical pipes

$$94.7 + 11.0 + 1.3 = 107 \text{ }^{\text{lb}}$$

WRITTEN BY

G. Jacques

CHECKED BYDATE

Sept. 1957

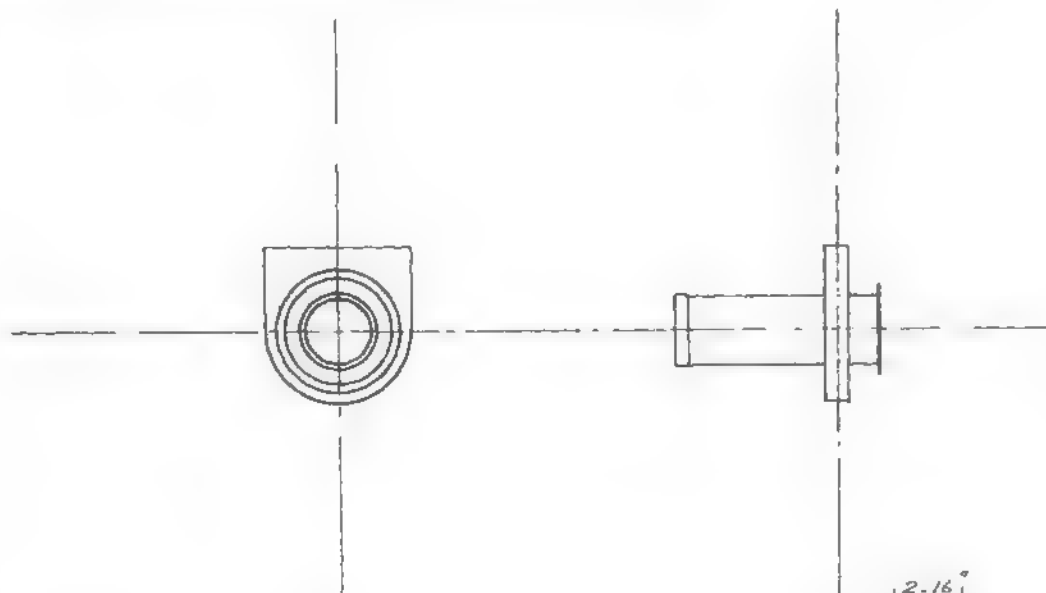
ISSUEAIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

196

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-2 WEIGHT OF MODEL SUPPORT STRUCTUREA-2-3-WEIGHT OF ATTACHMENT TO BALANCE STRUTS.BALL-BEARING. SKF- 6238-M

Weight of balls: $V = \frac{\pi D^3}{6}$
 $15 \times .283 \times \pi \frac{1.875^3}{6} = 14.68^{lb}$

Outer race.

Mean dia: $13.38 - .70 = 12.68$

Sectional area: $2.16 \times .70 = 1.51^{in^2}$

Weight: $.283 \times 11.7 \times 12.68^{in} = 17.12^{lb}$

Inner race.

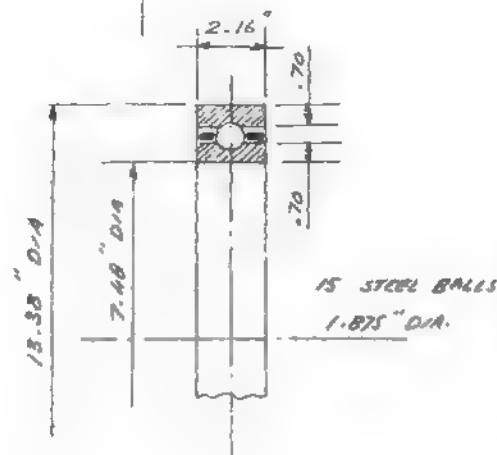
Mean dia: $6.47 + .70 = 7.17$

Sectional area: $2.16 \times .70 = 1.51^{in^2}$

Weight: $.283 \times 11.7 \times 7.17^{in} = 10.95^{lb}$

Weight of Bearing: $14.68 + 17.12 + 10.95 = 42.75^{lb}$

Note: By not removing the weight of the grooves, that of the retainers is taken care off.



WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

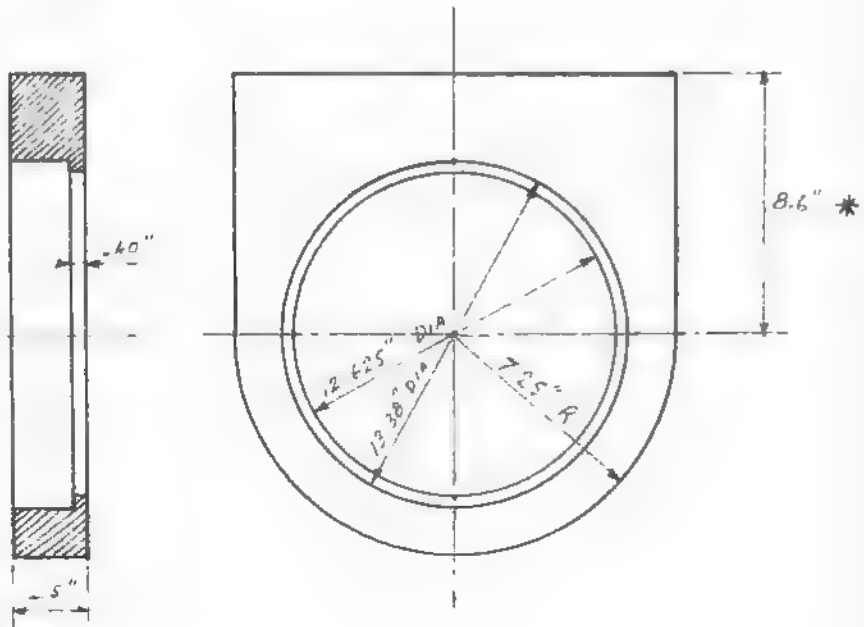
AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHT.A-2 WEIGHT OF MODEL SUPPORT STRUCTUREA-2-3ATTACHMENT TO BALANCE STRUTS. CONT'D.BEARING HOUSING.

Side area

$$(14.5 \times 8.6) + \left(7.25^2 \frac{\pi}{2} \right) - \left(12.38^2 \frac{\pi}{2} \right) = 124.8 + 83 - 141 = 66.8 \text{ in}^2$$

$$\text{Wt.} = 66.8 \times .25 \times 280 = 47.3 \text{ lb}$$

Hole housing

$$.283 \times .40 \times \frac{\pi}{4} (12.38^2 - 12.625^2) = 1.70 \text{ lb}$$

$$\text{Total weight} = 47.3 + 1.70 = 49 \text{ lb}$$

* NOTE

Dimension 8.6" is now 17.26" However, a number of large holes have been cut in the rectangular part of this component
Exact weight has not be computed again

WRITTEN BY

G. Jaques

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

198

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-2 WEIGHT OF MODEL SUPPORT STRUCTUREA-2-3ATTACHMENT TO BALANCE STRUTS - CONT'D.TUBE, FLANGE & OTHER RINGS.

Tube length - 21.50" $7 \times \frac{3}{16}$ Tube. Steel
weight. 13.32 $\frac{lb}{ft}$

Tube weight: $13.32 \times \frac{21.5}{12} = 23.9 \frac{lb}{ft}$

Flange 5.33 $\frac{lb}{ft}$ (Ref page 8 - 1)

Ball bearing mounting ring. assumed 12 $\frac{lb}{ft}$

End rings assumed 6 $\frac{lb}{ft}$

Total weight $23.9 + 5.33 + 12 + 6 = 47.23 \frac{lb}{ft}$

add 12% for welds, bolts, etc

$47.23 \times 1.12 = 52.9 \frac{lb}{ft}$

WRITTEN BY

G. Jasperson

CHECKED BY

1

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

~~SECRET~~

DECLASSIFIED

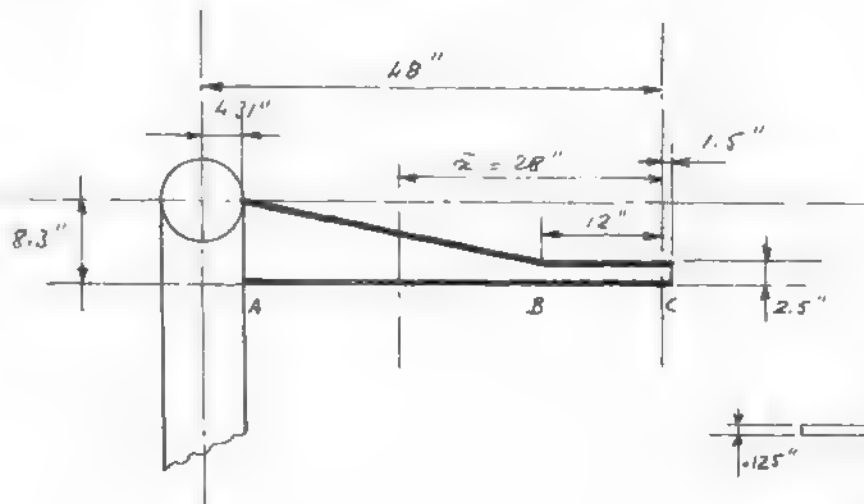
199

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

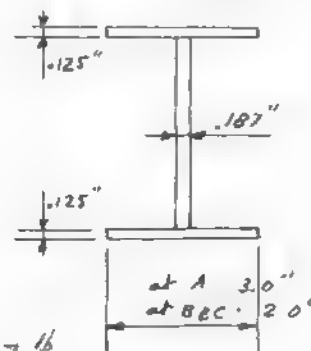
APPENDIX A - CALCULATION OF WEIGHT

A-2 WEIGHT OF MODEL SUPPORT STRUCTURE

A-2-4 - INCIDENCE CONTROL ARM.



TYPICAL ARM SECTION



FLANGES

Total length of tapered flange $31.7 + 30.3 = 64"$ Weight of tapered flange: $64 \times 2.5 \times .125 \times .283 = 5.67^{lb}$ Total length of constant width flange $(12 + 1.5) \times 2 = 27"$ Weight of constant width flange: $27 \times 2 \times .125 \times .283 = 1.91^{lb}$

WEB

Rectangular part: Side area $(2.5 - .25) (12 + 1.5) = 30.4 \text{ in}^2$ weight: $30.4 \times .187 \times .283 = 1.6^{lb}$ Trapezoidal part: Side area: $\left(\frac{8.05 + 2.25}{2} \right) \frac{48 - 12 - 4.31}{2} = 163.5 \text{ in}^2$ weight: $163.5 \times .187 \times .283 = 8.65^{lb}$ Weight of web: $(163.5 + 30.4) \times .187 \times .283 = 10.25^{lb}$ Total weight of arm $10.25 + 1.91 + 5.67 = 17.83^{lb}$ then $\bar{x} = \frac{(33 \times 14.32) + (6 \times 3.51)}{17.83} = 28"$ Weight of rear balance strut connecting link $\approx 3.5^{lb}$ Total weight of arm: $17.83 + 3.5 = 21.35$ say 21.50^{lb} add 10% for welds: 23.70^{lb} say 24.0^{lb}

WRITTEN BY

G. Jacques

CHECKED BY

1

DATE

Sept. 1957

ISSUE

AIRCRAFT

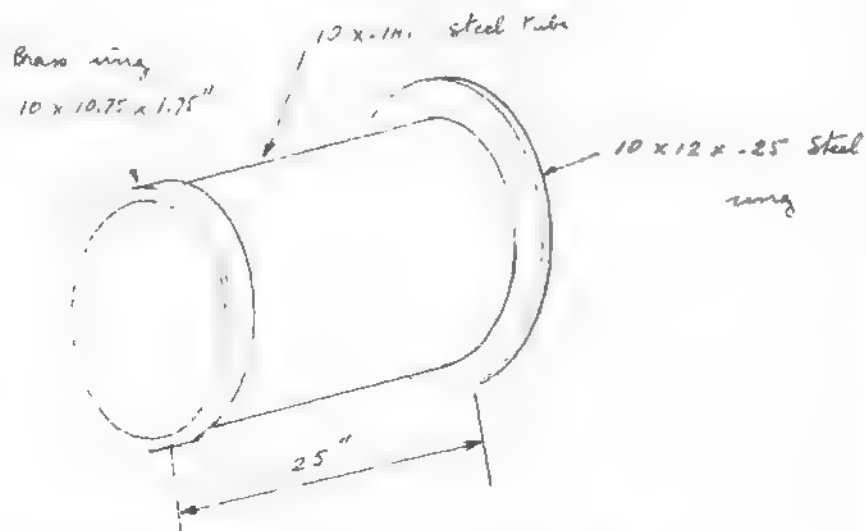
~~SECRET~~

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

200

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL.APPENDIX A - CALCULATION OF WEIGHTA-3 WEIGHT OF FAIRING.A-3-1FAIRING - OUTER SECTION.

Weight of 10" tube: Ref. Grunco catalog 14.81 $\frac{16}{ft.}$

Weight of tube: $14.81 \frac{25}{12} = 30.9 \frac{16}{ft.}$

Weight of steel ring:
 $.283 \times .25 \frac{\pi}{4} (12^2 - 10^2) = 2.44 \frac{16}{ft.}$

Weight of brass ring
 $30 \times 1.15 \frac{\pi}{4} (10.75^2 - 10^2) = 6.53 \frac{16}{ft.}$

Total weight: $30.9 + 2.44 + 6.53 = 39.87 \frac{16}{ft.}$

Add 10% for welds, bolts, etc....

$39.87 \times 1.10 = 43.85 \frac{16}{ft.}$

WRITTEN BY

G. Jaquemin

CHECKED BY

DATE

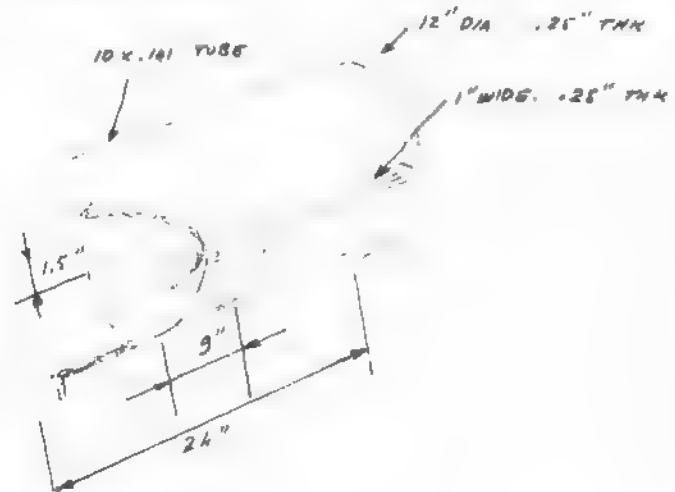
Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-3 WEIGHT OF FAIRINGA-3-2FAIRING - CENTER SECTION - CYLINDRICAL PART.

Weight of tube: Ref. ARMO CATALOG. Size 10 x .141. $14.81 \frac{lb}{ft}$

Weight of uncut tube: $14.81 \frac{24}{12} = 29.62 \frac{lb}{ft}$

Weight removed by cut arc 165°

$$14.81 \frac{9}{12} \frac{165}{360} = 5.10 \frac{lb}{ft}$$

Total weight of tube $29.62 - 5.10 = 24.52 \frac{lb}{ft}$

Weight of rings $2 \times .283 \times \frac{\pi}{4} (12^2 - 10^2) .25 = 4.87 \frac{lb}{ft}$

Weight of side strips $4 \times .283 \times 1.0 \times .25 \times 23.5 = 6.65 \frac{lb}{ft}$

Total weight of component

$$24.52 + 4.87 + 6.65 = 36.04 \frac{lb}{ft}$$

add 10% for welds, bolts, etc: $36.04 \times 1.1 = 39.7 \frac{lb}{ft}$

WRITTEN BY

G. Jacques

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED 202

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODEL

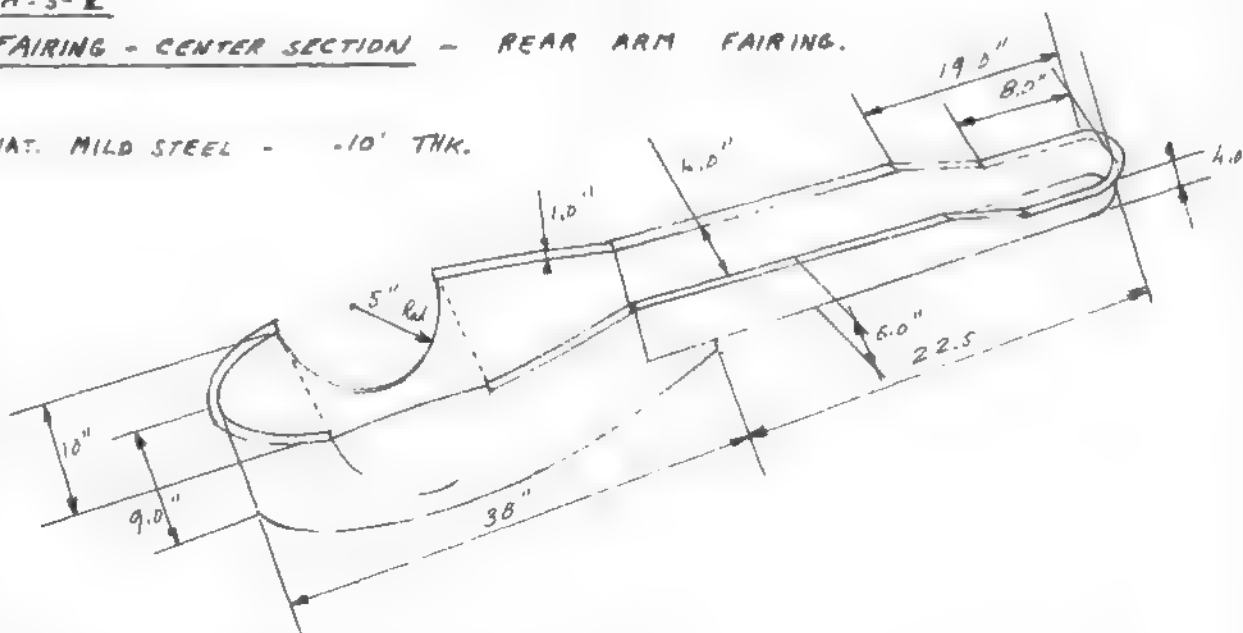
APPENDIX A - CALCULATION OF WEIGHT

A-3 WEIGHT OF FAIRING

A-3-2

FAIRING - CENTER SECTION - REAR ARM FAIRING.

MAT. MILD STEEL - .10" THK.



Developed length of streamlined part. 82"

$$\text{Lateral area of developed part: } (82 \times 9.0) - \pi \times 5^2 = 738 - 78.5 = 659.5 \text{ in}^2$$

Arm fairing:

$$\text{Sides: area: } 6.0 (2 \times 22.5 + 4.0) = 294 \text{ in}^2$$

$$\text{Bottom: } 22.5 \times 6 = 135 \text{ in}^2$$

Edge: 1.0" wide. Total length measured on drawing 105"

$$\text{Area: } 105 \text{ in}^2$$

Cover plates Front plate. $\approx \frac{1}{2}$ circle rad 3.0" 14 in²

$$\text{Rear plate } \approx \frac{25 \times 12}{2} = 150 \text{ in}^2$$

$$+ 25 \times 6 = 150 \text{ in}^2$$

$$\text{Total area of plate: } 659.5 + 294 + 135 + 105 + 150 + 150 = 1493.5 \text{ in}^2$$

$$\text{Weight of plate: } .283 \times .10 \times 1493.5 = 42.3 \text{ lb}$$

add 10% for welds, bolts, etc.

$$42.3 \times 1.1 = 46.50 \text{ lb}$$

WRITTEN BY

G. Jaeger

CHECKED BY

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-3 WEIGHT OF FAIRING.A-3-2.FAIRING - CENTER SECTION - ALUMINUM PART.

MAT. 24 ST. AL. ALL : .064" THK @ .10 $\frac{lb}{in^3}$

Developed length of contour 82"

Lateral area of sheet:

$$82 \times 40 = 3280 \text{ in}^2$$

$$\text{Volume: } 3280 \times .064 = 210 \text{ in}^3$$

Weight of sides

$$210 \times .10 = 21 \text{ lb}$$

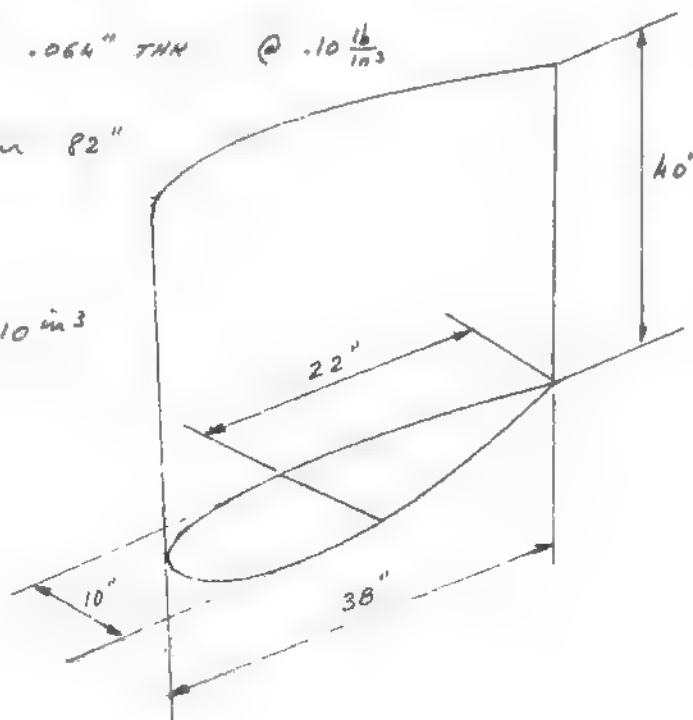
Bottom part:

approx area:

$$10 \times \frac{22}{2} = 110 \text{ in}^2$$

$$\text{Weight: } .10 \times .064 \times 110 = .70 \text{ lb}$$

$$\text{Total weight of aluminum fairing: } 21 + .70 = 21.70 \text{ lb}$$



WRITTEN BY

G. Jacques

CHECKED BY

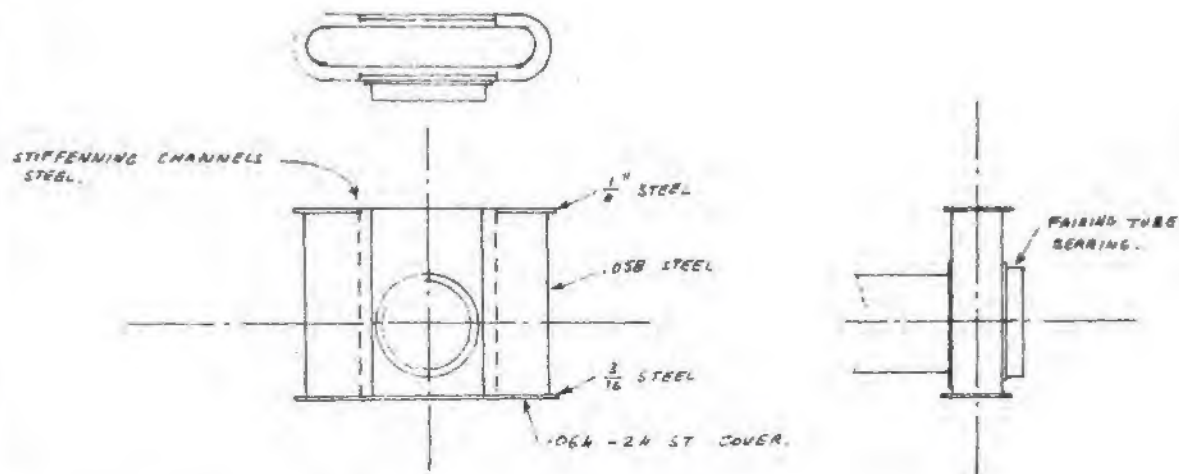
1.

DATE

Sept. 1957

ISSUE

AIRCRAFT

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-3 WEIGHT OF FAIRINGA-3-3ATTACHMENT TO BALANCE STRUTS - FAIRING -LOWER BORDER. $\frac{3}{16}$ STEEL.

thickness: .197" - width: .875" mean length: 54"

weight: $.283 \times .197 \times .875 \times 54 = 2.5 \text{ lb}$

UPPER BORDER. $\frac{1}{4}$ STEEL.

thickness: .250" width: .875" mean length: 31.2"

Weight: $.283 \times .25 \times .875 \times 31.2 = 1.93 \text{ lb}$

STIFFENING CHANNELS.

Thickness: .058" - developed width: 2.4" length: $19 \times 4 = 76"$

Weight: $.283 \times .058 \times 2.4 \times 76 = 2.99 \text{ lb}$

WRITTEN BY

G. Jaeger

CHECKED BY

1

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED

205

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-3 WEIGHT OF FAIRINGA-3-3ATTACHMENT TO BALANCE STRUTS - FAIRING - CONT'D.LOWER COVER PLATE. .064" 24 ST.

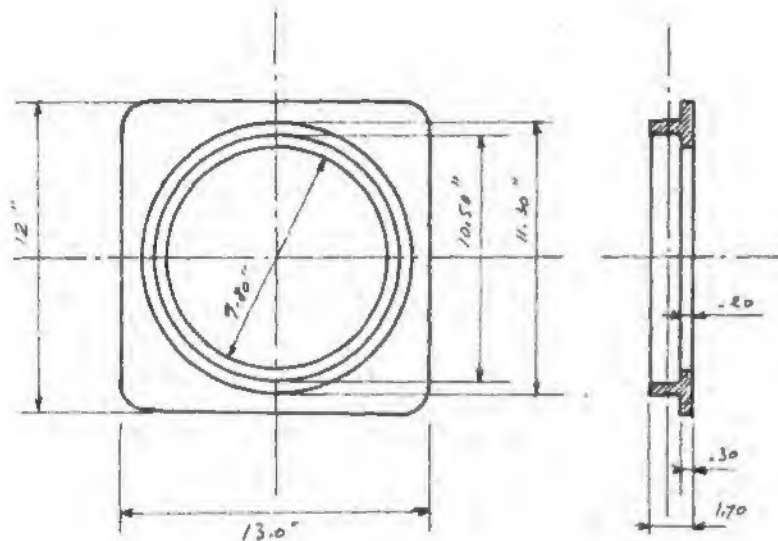
Thickness: .064" - width: 5.5" mean length: 11.60" x 2

Weight: $10 \times .064 \times 5.5 \times 23.2 = .81 \text{ lb}$ *FRONT & REAR SHEETING. .058" STEEL

Thickness: .058" developed width: 16.8" length: 19"

Weight: $2 \times .283 \times .058 \times 16.8 \times 19 = 10.5 \text{ lb}$ *SIDE SHEETING. .072" STEELThickness: .072" Side area: $(13 \times 19) - \left(\frac{\pi}{4} 10^2\right) = 169 \text{ in}^2$ Weight: $2 \times .283 \times .072 \times 169 = 6.9 \text{ lb}$ *FAIRING TUBE BEARING.

MAT. STEEL.



WRITTEN BY

G. Jacques

CHECKED BY

12

DATE

Sept. 1957

ISSUE

DECLASSIFIED

AIRCRAFT

~~SECRET~~

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-3 WEIGHT OF FAIRING.A-3.3ATTACHMENT TO BALANCE STRUTS - FAIRINGS - CONT'D.FAIRING TUBE BEARING - CONT'D.

Plate thickness: .30

$$\text{Area: } (12 \times 13) = \frac{\pi}{4} (10.50)^2 = 69 \text{ in}^2$$

$$\text{Weight: } .283 \times .30 \times 69 = 5.86 \text{ lb}$$

Cylinder:

$$\text{Weight: } .283 \frac{\pi}{4} (11.30^2 - 10.50^2) 1.50 = 6.02 \text{ lb}$$

Retainer ring

$$\text{Weight: } .283 \frac{\pi}{4} (10.50^2 - 9.5^2) .20 = .622 \text{ lb}$$

Retainer ring - external:

$$\text{Weight: } .283 \frac{\pi}{4} (11.30^2 - 9.30^2) .187 = 1.33 \text{ lb}$$

$$\text{Total weight: } 5.86 + 6.02 + .622 + 1.33 = 13.83 \text{ lb}$$

add 10% for bolts, welds, etc.

$$13.83 \times 1.10 = 15.25 \text{ lb}$$

TOTAL WEIGHT OF FAIRING.

$$2.5 + 1.93 + 2.99 + .81 + 10.5 + 6.9 + 13.83 = 39.46 \text{ lb}$$

add 10% for welds, bolts, etc:

$$1.10 \times 39.46 = 43.50 \text{ lb}$$

WRITTEN BY

G. Jacques

CHECKED BY

R. J.

DATE

Sept. 1957

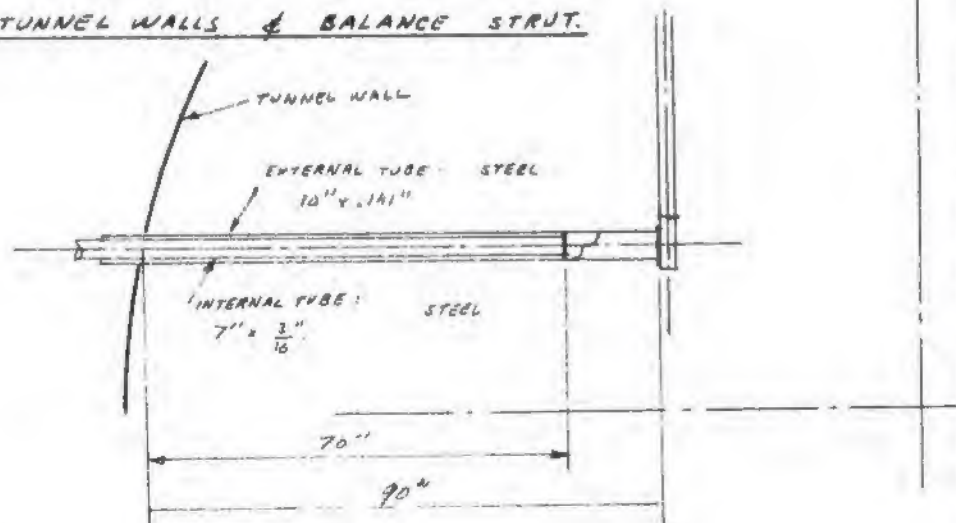
ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~

DECLASSIFIED 207

STRESS ANALYSIS OF $\frac{1}{12}$ SCALE HOVERING & TRANSITION MODELAPPENDIX A - CALCULATION OF WEIGHTA-3 WEIGHT OF FAIRINGA-3-4TUBES BETWEEN TUNNEL WALLS & BALANCE STRUT.

EXTERNAL TUBE: 14.81 $\frac{lb}{ft}$

Weight: $\frac{90}{12} \times 14.81 = 111 \frac{lb}{ft}$

INTERNAL TUBE: 13.32 $\frac{lb}{ft}$

Weight: $\frac{70}{12} \times 13.32 = 77.7 \frac{lb}{ft}$

TOTAL WEIGHT OF TUBES.

$111 + 77.7 = 188.7 \frac{lb}{ft}$

Assume $\frac{1}{2}$ the total weight is applied on the strut fairing + 10 $\frac{lb}{ft}$ for miscellaneous parts:

$94.35 + 10 = 104.35$ say 105 $\frac{lb}{ft}$

WRITTEN BY

G. Jaques

CHECKED BY

10

DATE

Sept. 1957

ISSUE

AIRCRAFT

DECLASSIFIED

~~SECRET~~